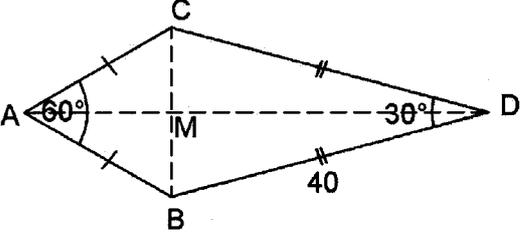


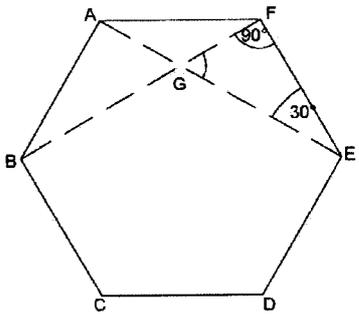
4.4 MATHEMATICS ALTERNATIVE B (122)

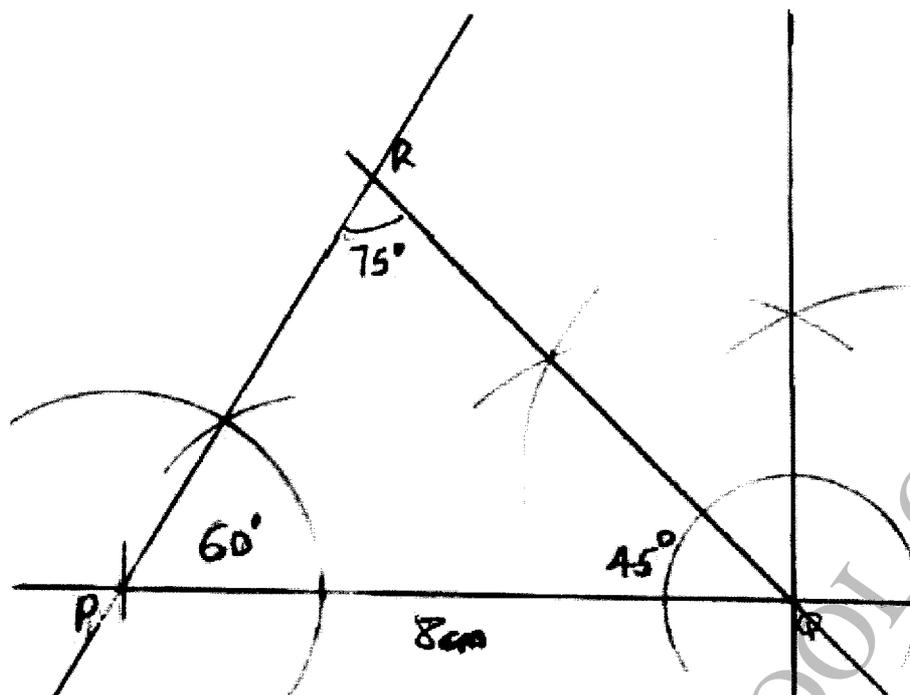
4.4.1 Mathematics Alternative B (122/1)

No	Marking scheme	Marks	Comments																		
1	(a) $4732 = 2^2 \times 7 \times 13^2$	B1																			
	(b) $2^2 \times 7 \times 13^2 \times 7 = 2^2 \times 7^2 \times 13^2$ is a perfect square. □ Smallest factor is 7	B1 2																			
2	Time taken: Juma $\frac{3120}{48} = 65$ min, Weru $\frac{3120}{120} = 26$ min, Njeri = $\frac{3120}{156} = 20$ min	M1	or equivalent																		
	LCM of 65, 26, 20	M1																			
	<table border="1" style="margin-left: auto; margin-right: auto;"> <tr><td>5</td><td>65</td><td>26</td><td>20</td></tr> <tr><td>13</td><td>13</td><td>26</td><td>4</td></tr> <tr><td>2</td><td>1</td><td>2</td><td>4</td></tr> <tr><td>2</td><td>1</td><td>1</td><td>2</td></tr> <tr><td></td><td>1</td><td>1</td><td>1</td></tr> </table> <p style="text-align: center;">LCM = 260 min or 4h 20 mins</p> <p style="text-align: center;">Time together is 1120h</p>	5		65	26	20	13	13	26	4	2	1	2	4	2	1	1	2		1	1
5	65	26	20																		
13	13	26	4																		
2	1	2	4																		
2	1	1	2																		
	1	1	1																		
3	$\frac{-9 \div + 3 \times + 4 - - 2}{(+15 - - 5) \div - 4} = \frac{-10}{-5}$ $= 2$	M1	correct numerator																		
		M1	correct denominator																		
		A1 3																			

4	$\frac{3}{4} \text{ of } 8\frac{1}{5} - 4\frac{1}{2} = \frac{3}{4} \times \frac{41}{5} - \frac{9}{2}$ $1\frac{1}{4} \div 1\frac{7}{8} \times 3\frac{3}{10} = \frac{5}{4} \times \frac{8}{15} \times \frac{33}{10}$ $\frac{123-90}{11} = \frac{20}{11}$ $= \frac{33}{20} \times \frac{5}{11}$ $= \frac{3}{4}$	M1 M1 A1 3	numerator denominator												
5	<table style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th style="text-align: left; width: 50%;">No</th> <th style="text-align: left; width: 50%;">Log</th> </tr> </thead> <tbody> <tr> <td>84.56</td> <td>1.9272</td> </tr> <tr> <td>$(0.0027)^{1/3}$</td> <td>$\bar{3}.4314 \div 3 \rightarrow +\bar{1}.1438$</td> </tr> <tr> <td></td> <td><u>1.0710</u></td> </tr> <tr> <td><u>0.045</u></td> <td>$-\bar{1}.6532$</td> </tr> <tr> <td>261.7</td> <td><u>2.4178</u></td> </tr> </tbody> </table>	No	Log	84.56	1.9272	$(0.0027)^{1/3}$	$\bar{3}.4314 \div 3 \rightarrow +\bar{1}.1438$		<u>1.0710</u>	<u>0.045</u>	$-\bar{1}.6532$	261.7	<u>2.4178</u>	M1 M1 M1 A1 4	All logs correct Correct cube root Correct multiplication and division
No	Log														
84.56	1.9272														
$(0.0027)^{1/3}$	$\bar{3}.4314 \div 3 \rightarrow +\bar{1}.1438$														
	<u>1.0710</u>														
<u>0.045</u>	$-\bar{1}.6532$														
261.7	<u>2.4178</u>														
6	$4 \times 10 \times 10 + 2 \times (10 \times 10 - x^2)$ $= 400 + 200 - 2x^2$ $= 600 - 2x^2$	M1 M1 A1 3													
7	$\frac{22}{7} \times 0.7 \times 0.7 \times h = 3.234$ $1.54 h = 3.254$ $h = \frac{3.234}{1.54}$ $= 2.1\text{m}$	M1 M1 A1 3	Conversion from l to m ³												

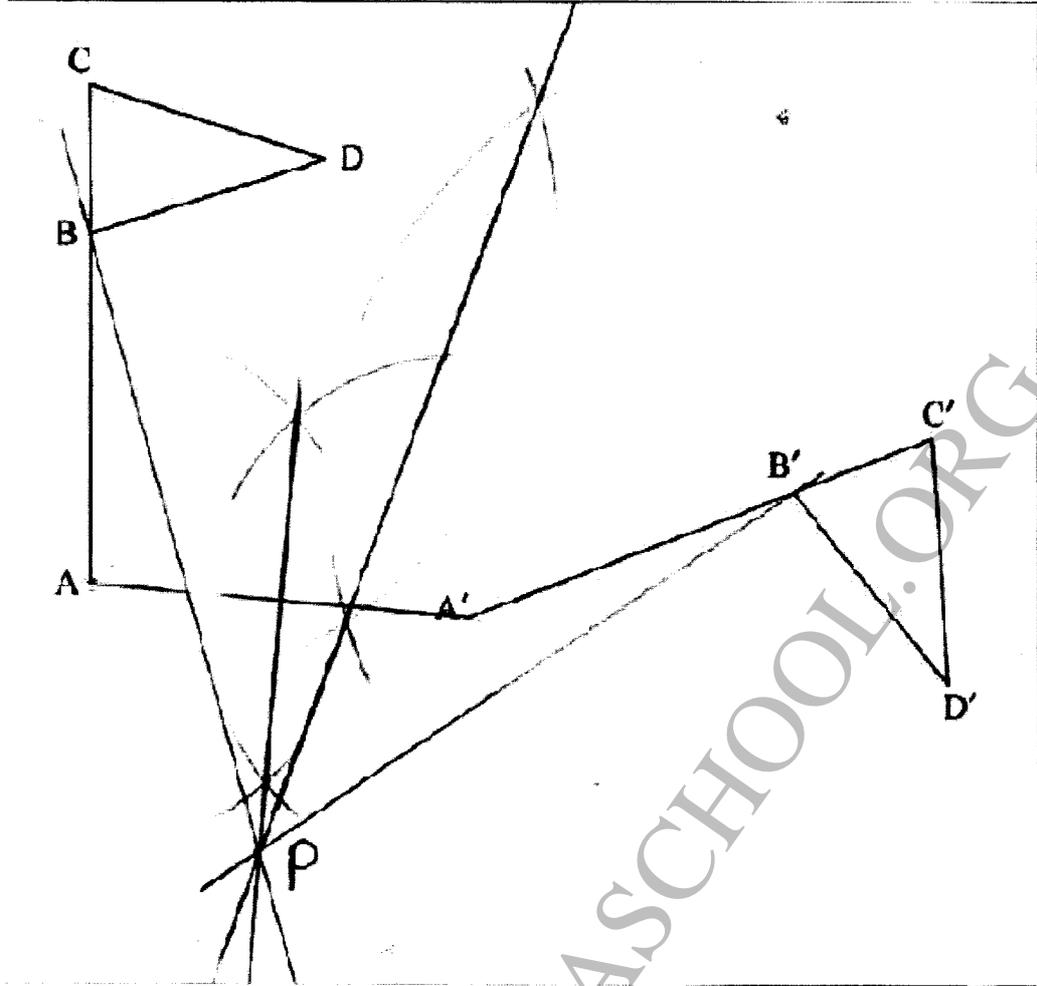
8	$\frac{BM}{40} = \sin 15^\circ \Rightarrow BM = 40 \sin 15^\circ$ $BC = 2 \times 40 \sin 15^\circ$ $= 20.71 \text{ cm}$ <p>Area of the quadrilateral</p> $= \frac{1}{2} \times (20.71)^2 \times \sin 60 + \frac{1}{2} \times 40^2 \times \sin 30$ $= 185.7 + 400$ $= 585.7 \text{ cm}^2$	M1 M1 M1 A1 4	 <p>Area of $\triangle ABC$ Area of $\triangle BDC$</p>
9	$\frac{135}{360} \times \frac{22}{7} \times r^2 = 36.96$ $r^2 = \frac{36.96 \times 360 \times 7}{135 \times 22}$ $r = \sqrt{31.36}$ $= 5.6 \text{ cm}$	M1 M1 A1 3	
10	$\frac{r^2 + \sqrt[3]{r}}{t - 3\frac{2}{3}} = \frac{27^2 + \sqrt[3]{27}}{5 - 3\frac{2}{3}}$ $= \frac{729 + 3}{1\frac{1}{3}}$ $= 549$	M1 A1 2	

11	<p>Let Njoka's salary be x, and Okoth's salary be y</p> $\frac{1}{4}x + \frac{1}{6}y = 16000$ $\frac{4}{9}x + \frac{1}{3}y = 30000$ $3x + 2y = 192000$ $4x + 3y = 270000$ $9x + 6y = 576000$ $8x + 6y = 540000$ <hr/> $x = 36000$ $y = 42000$ <p>Njoka's sh36000 and Okoth's sh42000</p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>3</p>	
12	$x - 8 \leq -x \qquad -x \geq 4 - 3x$ $2x \leq 8 \qquad 2x \geq 4$ $x \leq 4 \qquad x \geq 2$ $2 \leq x \leq 4$ 	<p>M1</p> <p>M1</p> <p>A1</p> <p>B1</p> <p>4</p>	
13	<p>$\angle BAF = 120^\circ$ interior angle of a regular hexagon</p> $\angle AEF = \angle FAE = \frac{180 - 120}{2} = 30^\circ$ <p>In $\triangle EFG$, $\angle EFG = 120 - 30 = 90^\circ$</p> $\therefore \angle FGE = 180 - (90 + 30) = 60^\circ$	<p>B1</p> <p>B1</p> <p>B1</p> <p>3</p>	

14	 <p>PR = 5.9 ± 0.1cm</p>	<p>B1</p> <p>B1</p> <p>B1</p> <p>B1</p>	<p>PQ = 8 and $\angle 60^\circ$ constructed</p> <p>75° or 45° constructed</p> <p>Complete Δ</p>
15		<p>M1</p> <p>M1</p> <p>A1</p>	

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16



Centre P
Angle of rotation, -71°

B1 at least 2 perpendicular bisector

B1

B1

3

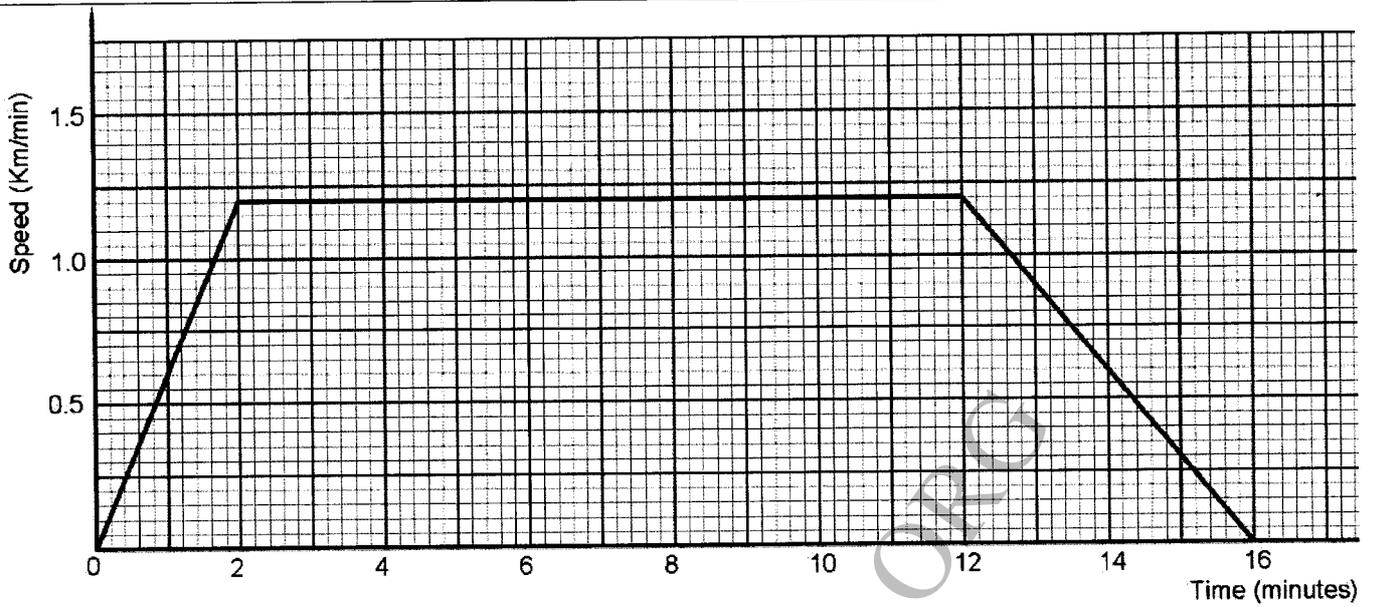
17	<p>(a)</p> $\frac{4}{100} \times (400000 - 250000) +$ $\frac{7.5}{100} \times (525000 - 400000) + 60000$ $= 6000 + 9375 + 60000$ $= \text{Ksh } 75\,375$ <p>(b) $94500 = 60000 + 6000 + x$</p> $x = 28500$ <p>Value of goods for commission of Ksh 28500</p> $= \frac{28500}{7.5} \times 100$ $= \text{Ksh } 380\,000$ <p>Total sale = $250000 + 150000 + 380000$</p> $= \text{Ksh } 780\,000$	<p>M1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p>	
		10	

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18.	$y + 2x = 4$		
(a)	$-y + 3x = 1$ $5x = 5$ $x = 1$ $y + 2 = 4 \Rightarrow y = 2$	M1	
	T(1,2)	A1	
	Grad		
	$\frac{-2-2}{3-1} = \frac{-4}{2} = -2$	B1	
	$\frac{y-2}{x-1} = -2$	M1	
	$y = -2x + 4$	A1	
(b)	Grad = -2		
	$\frac{y-4}{x-5} = -2$	M1	
	$\Rightarrow y - 4 = -2x + 10$		
	$y = -2x + 14$	A1	
(c)	Grad = $\frac{1}{2}$	B1	
	$\frac{y-2}{x-1} = \frac{1}{2}$	M1	
	$y - 2 = \frac{1}{2}(x - 1)$		
	$2y - 4 = x - 1$	A1	
	$-x + 2y = 3$		
		10	

19.

(a)



Scale

Acceleration part

Constant acceleration.

Deceleration

(b)

(i) $\frac{1}{2} \times 4 \times 1.2 \times 1000\text{m}$
 $= 2400\text{m}$

(ii) $\frac{1}{2} \times 2 \times 1.2 + 1.2 \times 10 + \frac{1}{2} \times 4 \times 1.2\text{km}$
 $= 15.6\text{km}$

(iii) Average speed = $\frac{15.6}{\frac{4}{15}\text{h}}$
 $= 58.5\text{km/h}$

S1

B1

B1

B1

M1

A1

M1

or equivalent

A1

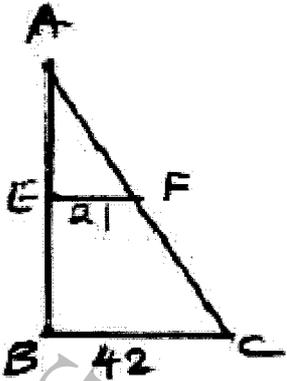
M1

A1

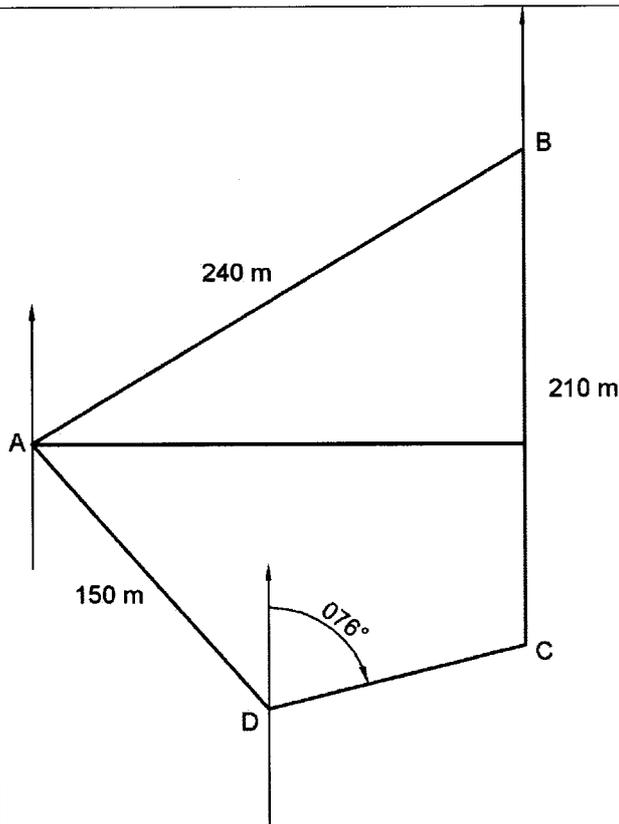
10

20. (a)			
(i)	Area of $A + C = (x - y)(x - y) + y^2$	B1	
(ii)	Area of $B + D = y(x - y) + y(x - y)$ $= 2y(x - y)$	M1 A1	
(iii)	$(x - y)^2 + y^2 + 2y(x - y)$ $= (x - y)(x - y) + y^2 + 2yx - 2y^2$ $= x^2 - 2yx + y^2 + y^2 + 2yx - 2y^2$ $= x^2$	M1 A1	
(b)	$2(x - 2) + 2(x - 2)$ $= 4x - 8$	M1 A1	
(c)	$25c^2 - 16 = (5c)^2 - 4^2$ $= (5c + 4)(5c - 4)$	B1	
(d)	$5024^2 - 4976^2 = (5024 + 4976)(5024 - 4976)$		
(i)	$= 10000 \times 48$ $= 480000$	B1	
(ii)	$8.96^2 - 1.04^2 = (8.96 + 1.04)(8.96 - 1.04)$ $= 10 \times 7.92$ $= 79.2$	B1	
		10	

21. (a)	<p>Area of the base of the cuboid</p> $= 8 \times 6\text{cm}^2 = 48\text{cm}^2$ <p>Area of 4 faces of the side of the cuboid</p> $= (2 \times 8 \times 3 + 2 \times 6 \times 3)\text{cm}^2$ $= 48 + 36\text{cm} = 84\text{cm}^2$ <p>Total $48 + 84 = 132\text{cm}^2$</p>	M1	
(b)	<p>Consider faces VEF and VHG use Hero's formula:-</p> $S = \frac{1}{2}(13 + 13 + 8) = 17\text{cm}$ <p>Area of VEF and VHG</p> $= 2\sqrt{17(17-13)(17-13)(17-8)}\text{cm}$ $= 2\sqrt{17 \times 4 \times 4 \times 9}$ $= 98.96\text{cm}^2$ <p>Consider faces VFG and VEH</p> $S = \frac{1}{2}(13 + 13 + 6) = 16\text{cm}$ <p>Area of VFG</p> $= 2\sqrt{16(16-13)(16-13)(16-6)}$ $= 2\sqrt{16 \times 3 \times 3 \times 10}$ $= 75.90\text{cm}^2$ <p>Area of triangular faces</p> $98.96 + 75.90$ $= 174.86\text{cm}^2$	B1	
(c)	<p>Surface area of the solid</p> $= 132 + 174.86$ $= 306.86\text{cm}^2$	M1	
		A1	
			10

<p>22. (a)</p>	<p>Vertical height of small cone:</p> $\frac{AE}{40} = \frac{21}{42} \Rightarrow AE = 20\text{cm}$ <p>Volume of frustum</p> $= \frac{1}{3} \times \frac{22}{7} \times 42^2 \times 40 - \frac{1}{3} \times \frac{22}{7} \times 21^2 \times 20$ $= 73920 - 9240$ $= 64680\text{cm}^3$	<p>B1</p> <p>M1 M1</p> <p>M1</p> <p>A1</p>	
<p>(b)</p>	<p>Volume of cylindrical part</p> $= \frac{22}{7} \times 21^2 \times 30$ $= 41580\text{cm}^3$	<p>M1</p> <p>A1</p>	
<p>(c)</p>	<p>Volume of hemispherical part</p> $= \frac{1}{2} \times \frac{4}{3} \times \frac{22}{7} \times 21^3$ $= 19404\text{cm}^3$ <p>Total volume</p> $= 64680 + 41580 + 19404$ $= 125\,664\text{ cm}^3$	<p>M1</p> <p>A1</p> <p>B1</p> <p>10</p>	

23. (a)



(b)

(i) Distance $CD = 3.7 \times 30$
 $= 111 \text{ km}$
 Bearing of C from D $= 076^\circ$

(ii) Distance of A to the west of B
 $= 6.9 \times 30$
 $= 207 \text{ km}$

(c)

$$\tan \theta = \frac{18}{150}$$

$$= 0.12$$

$$\theta = \tan^{-1} 0.12$$

$$= 6.84^\circ$$

B1

Position of B

B1

Position of C

B1

Position of D

B1

Complete Diagram
 ABCD

B1

B1

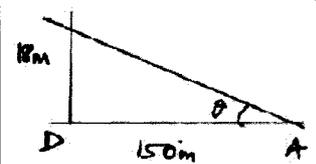
M1

A1

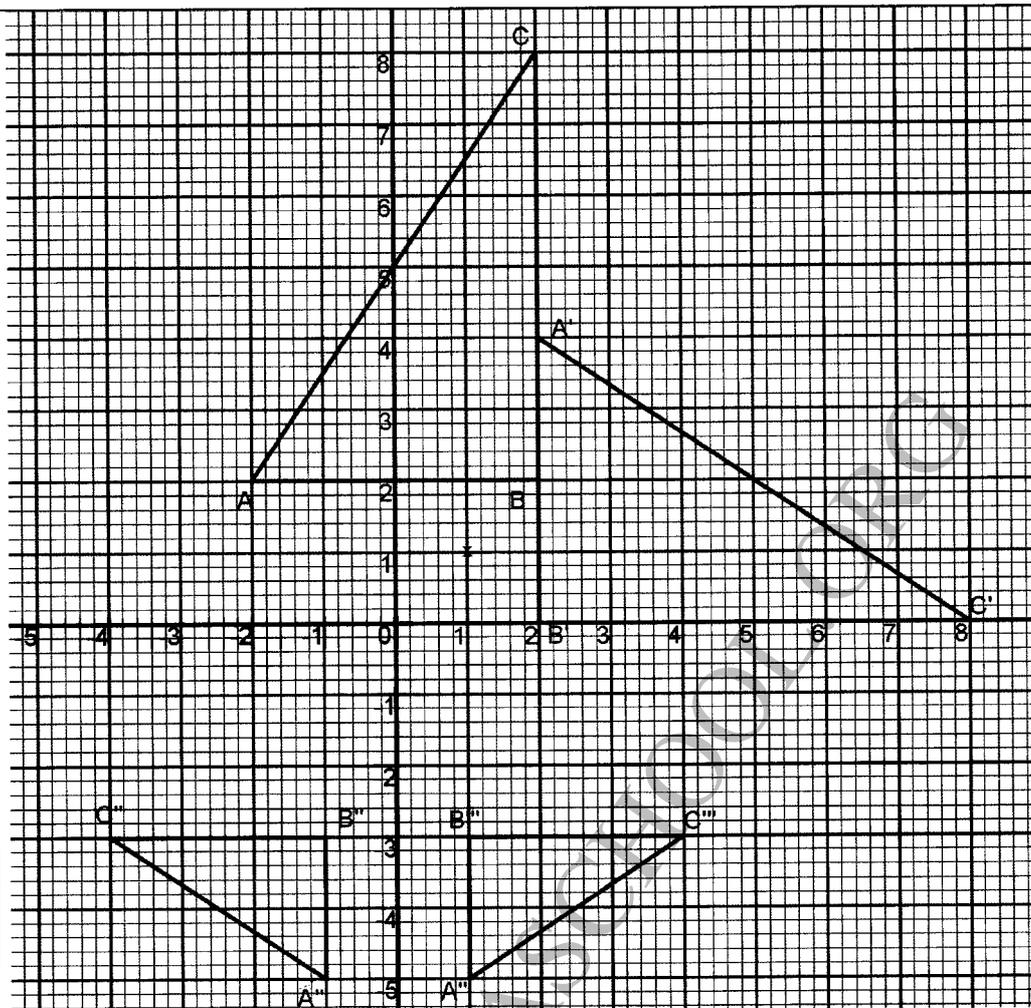
M1

A1

10



24
(a)



ΔABC correctly drawn
 $A'B'C'$ correctly plotted
 $\Delta A'B'C'$ drawn

(b)(i) $\Delta A''B''C''$ drawn
 (ii) enlargement
 scale factor, $-\frac{1}{2}$ centre $(0, 2)$

(c) $\Delta A'''B'''C'''$ drawn

(d)(i) Directly congruent
 (ii) Oppositely congruent

B1
 B1
 B1

B1
 B1
 B1
 B1

s.f
 centre

B1

B1
 B1

10