

29.3.2 Mathematics Paper 2

Name Index Number /

121/2
MATHEMATICS
Paper 2
Oct./Nov. 2008
 2½ hours

Candidate's Signature

Date

THE KENYA NATIONAL EXAMINATIONS COUNCIL

Kenya Certificate of Secondary Education

MATHEMATICS

Paper 2

2½ hours

Instructions to candidates

1. Write your name and index number in the spaces provided above.
2. Sign and write the date of examination in the spaces provided above.
3. The paper contains **two** sections: **Section I** and **Section II**.
4. Answer **all** the questions in **Section I** and any **five** questions from **Section II**.
5. All answers and working must be written on the question paper in the spaces provided below each question.
6. **Show all the steps in your calculations, giving your answers at each stage in the spaces below each question.**
7. Marks may be given for correct working even if the answer is wrong.
8. Non-programmable silent electronic calculators and KNEC Mathematical tables may be used, except where stated otherwise.

For Examiner's use only.

Section I

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | Total |
|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|-------|
| | | | | | | | | | | | | | | | | |

Section II

| 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | Total |
|----|----|----|----|----|----|----|----|-------|
| | | | | | | | | |

Grand Total

| |
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| |
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This paper consists of 20 printed pages.

Candidates should check the question paper to ascertain that all the pages are printed as indicated and no questions are missing.

SECTION I (50 marks)

Answer all the questions in this section in the spaces provided.

- 1 In this question, show all the steps in your calculations, giving the answer at each stage. Use logarithms correct to 4 decimal places, to evaluate

$$\frac{6.373 \log 4.948}{\sqrt{0.004636}}$$

(3 marks)

- 2 Make h the subject of the formula

$$q = \frac{1+rh}{1-hr}$$

(2 marks)

- 3 Line AB given below is one side of triangle ABC. Using a ruler and a pair of compasses only:



- (i) Complete the triangle ABC such that $BC = 5$ cm and $\angle ABC = 45^\circ$. (1 mark)
(ii) On the same diagram construct a circle touching sides AC, BA produced and BC produced. (2 marks)

- 4 The position vectors of points A and B are $\begin{pmatrix} 3 \\ -1 \\ -4 \end{pmatrix}$ and $\begin{pmatrix} 8 \\ -6 \\ 6 \end{pmatrix}$ respectively. A point P divides AB in the ratio 2:3.

Find the position vector of point P.

(3 marks)

- 5 The top of a table is a regular hexagon. Each side of the hexagon measures 50.0 cm. Find the maximum percentage error in calculating the perimeter of the top of the table. (3 marks)

- 6 A student at a certain college has a 60% chance of passing an examination at the first attempt. Each time a student fails and repeats the examination, his chances of passing are increased by 15%. Calculate the probability that a student in the college passes an examination at the second or at the third attempt. (3 marks)

- 7 An aeroplane flies at an average speed of 500 knots due East from a point P(53.4°N , 40°E) to another point Q. It takes $2\frac{1}{4}$ hours to reach point Q.

Calculate:

- (i) the distance in nautical miles it travelled; (1 mark)
(ii) the longitude of point Q to 2 decimal places. (2 marks)

- 8 (a) Expand and simplify the expression

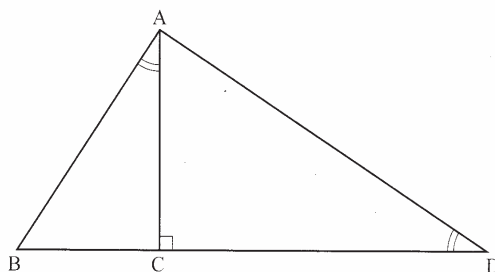
$$\left(10 + \frac{2}{x}\right)^5.$$

(2 marks)

- (b) Use the expansion in (a) above to find the value of 14^5 .

(2 marks)

- 9 In the figure below, angles BAC and ADC are equal. Angle ACD is a right angle. The ratio of the sides AC : BC = 4 : 3.



Given that the area of triangle ABC is 24 cm^2 , find the area of triangle ACD.

(3 marks)

- 10 Points A(2,2) and B(4,3) are mapped onto A'(2,8) and B'(4,15) respectively by a transformation T.

Find the matrix of T.

(4 marks)

- 11 The equation of a circle is given by $4x^2 + 4y^2 - 8x + 20y - 7 = 0$.

Determine the coordinates of the centre of the circle.

(3 marks)

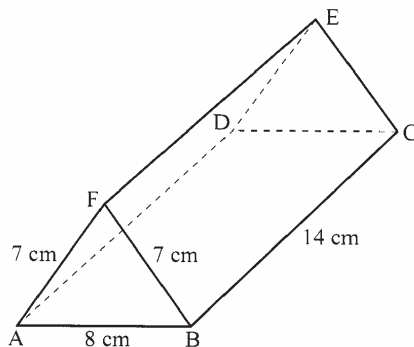
- 12 Solve for y in the equation $\log_{10}(3y + 2) - 1 = \log_{10}(y - 4)$.

(3 marks)

- 13 Without using a calculator or mathematical tables, express $\frac{\sqrt{3}}{1 - \cos 30^\circ}$ in surd form and simplify.

(3 marks)

- 14 The figure below represents a triangular prism. The faces ABCD, ADEF and CBFE are rectangles. AB = 8 cm, BC = 14 cm, BF = 7 cm and AF = 7 cm.



Calculate the angle between faces BCEF and ABCD.

(3 marks)

- 15 A particle moves in a straight line from a fixed point. Its velocity $V \text{ m s}^{-1}$ after t seconds is given by $V = 9t^2 - 4t + 1$
Calculate the distance travelled by the particle during the third second. (3 marks)

- 16 Find in radians, the values of x in the interval $0^\circ \leq x \leq 2\pi^\circ$ for which $2 \cos^2 x - \sin x = 1$.
(Leave the answers in terms of π) (4 marks)

SECTION II (50 marks)

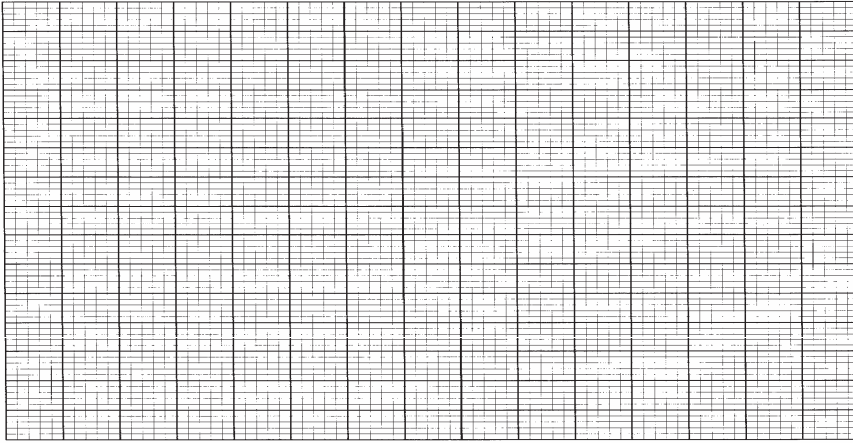
Answer *any five* questions in this section.

- 17 A trader deals in two types of rice; type A and type B. Type A costs Ksh 400 per bag and type B costs Ksh 350 per bag.
- (a) The trader mixes 30 bags of type A with 50 bags of type B. If he sells the mixture at a profit of 20%, calculate the selling price of one bag of the mixture. (4 marks)
- (b) The trader now mixes type A with type B in the ratio $x : y$ respectively. If the cost of the mixture is Ksh 383.50 per bag, find the ratio $x : y$. (4 marks)
- (c) The trader mixes one bag of the mixture in part (a) with one bag of the mixture in part (b) above. Calculate the ratio of type A rice to type B rice in this mixture. (2 marks)
- 18 Three variables p , q and r are such that p varies directly as q and inversely as the square of r .
- (a) When $p = 9$, $q = 12$ and $r = 2$.
Find p when $q = 15$ and $r = 5$. (4 marks)
- (b) Express q in terms of p and r . (1 mark)
- (c) If p is increased by 20% and r is decreased by 10%, find:
- (i) a simplified expression for the change in q in terms of p and r ; (3 marks)
- (ii) the percentage change in q . (2 marks)
- 19 (a) Complete the table below, giving the values correct to 2 decimal places.

| | | | | | | | | | | | | | |
|---------------|---|------|------|----|-------|-----|-----|-------|------|-----|------|-----|-----|
| x° | 0 | 30 | 60 | 90 | 120 | 150 | 180 | 210 | 240 | 270 | 300 | 330 | 360 |
| $\sin 2x$ | 0 | | 0.87 | | -0.87 | | 0 | 0.87 | 0.87 | | | | 0 |
| $3\cos x - 2$ | 1 | 0.60 | | -2 | -3.5 | | | -4.60 | | | -0.5 | | 1 |

(2 marks)

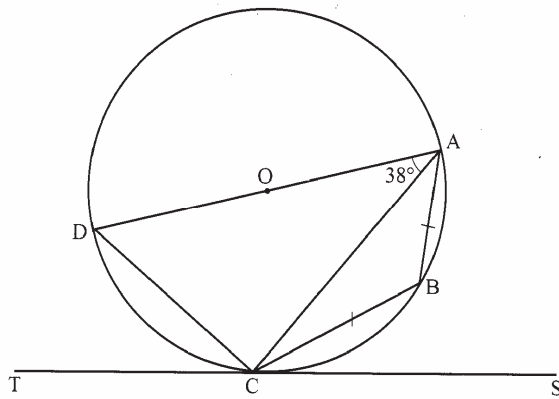
- (b) On the grid provided, draw the graphs of $y = \sin 2x$ and $y = 3\cos x - 2$ for $0^\circ \leq x \leq 360^\circ$ on the same axes. Use a scale of 1 cm to represent 30° on the x -axis and 2 cm to represent 1 unit on the y -axis. (5 marks)



(c) Use the graph in (b) above to solve the equation $3\cos x - \sin 2x = 2$. (2 marks)

(d) State the amplitude of $y = 3\cos x - 2$. (1 mark)

20 In the figure below DA is a diameter of the circle ABCD centre O, radius 10 cm. TCS is a tangent to the circle at C, AB = BC and angle DAC = 38° .



(a) Find the size of the angle:
 (i) ACS; (2 marks)

(ii) BCA. (2 marks)

(b) Calculate the length of:
 (i) AC; (2 marks)

(ii) AB. (4 marks)

21 Two policemen were together at a road junction. Each had a *walkie talkie*. The maximum distance at which one could communicate with the other was 2.5 km.

One of the policemen walked due East at 3.2 km/h while the other walked due North at 2.4 km/h.

The policeman who headed East travelled for x km while the one who headed North travelled for y km before they were unable to communicate.

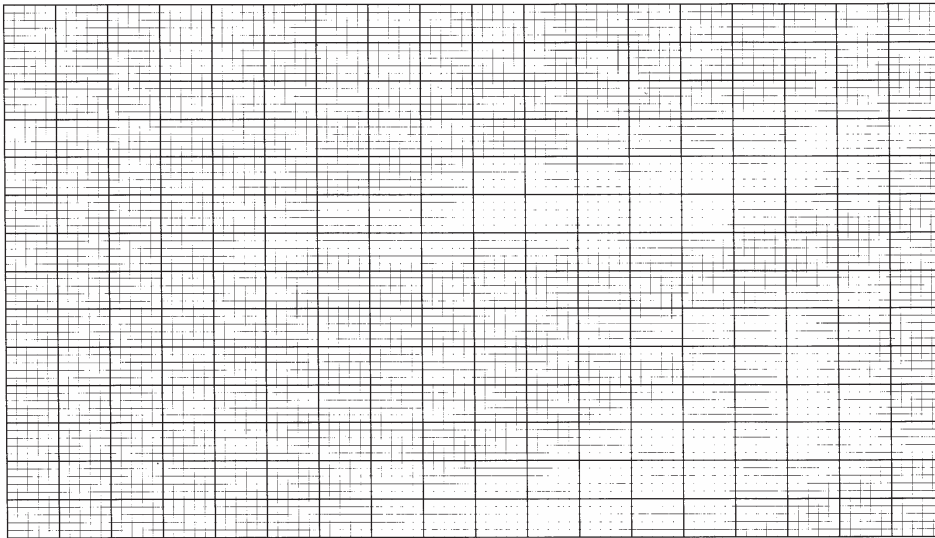
(a) Draw a sketch to represent the relative positions of the policemen. (1 mark)

- (b) (i) From the information above form two simultaneous equations in x and y . (2 marks)
- (ii) Find the values of x and y . (5 marks)
- (iii) Calculate the time taken before the policemen were unable to communicate. (2 marks)

22 The table below shows the distribution of marks scored by 60 pupils in a test.

| Marks | 11–20 | 21–30 | 31–40 | 41–50 | 51–60 | 61–70 | 71–80 | 81–90 |
|-----------|-------|-------|-------|-------|-------|-------|-------|-------|
| Frequency | 2 | 5 | 6 | 10 | 14 | 11 | 9 | 3 |

- (a) On the grid provided, draw an ogive that represents the above information. (4 marks)



- (b) Use the graph to estimate the interquartile range of this information. (3 marks)
- (c) In order to pass the test, a pupil had to score more than 48 marks. Calculate the percentage of pupils who passed the test. (3 marks)

23 Halima deposited Ksh 109 375 in a financial institution which paid simple interest at the rate of 8% p.a. At the end of 2 years, she withdrew all the money. She then invested the money in shares. The value of the shares depreciated at 4% p.a. during the first year of investment. In the next 3 years, the value of the shares appreciated at the rate of 6% every four months.

- (a) Calculate the amount Halima invested in shares. (3 marks)
- (b) Calculate the value of Halima's shares:
- (i) at the end of the first year; (2 marks)
- (ii) at the end of the fourth year, to the nearest shilling. (3 marks)
- (c) Calculate Halima's gain from the shares as a percentage. (2 marks)

- 24 The table below shows values of x and some values of y for the curve $y = x^3 + 3x^2 - 4x - 12$ in the range $-4 \leq x \leq 2$.

(a) Complete the table by filling in the missing values of y .

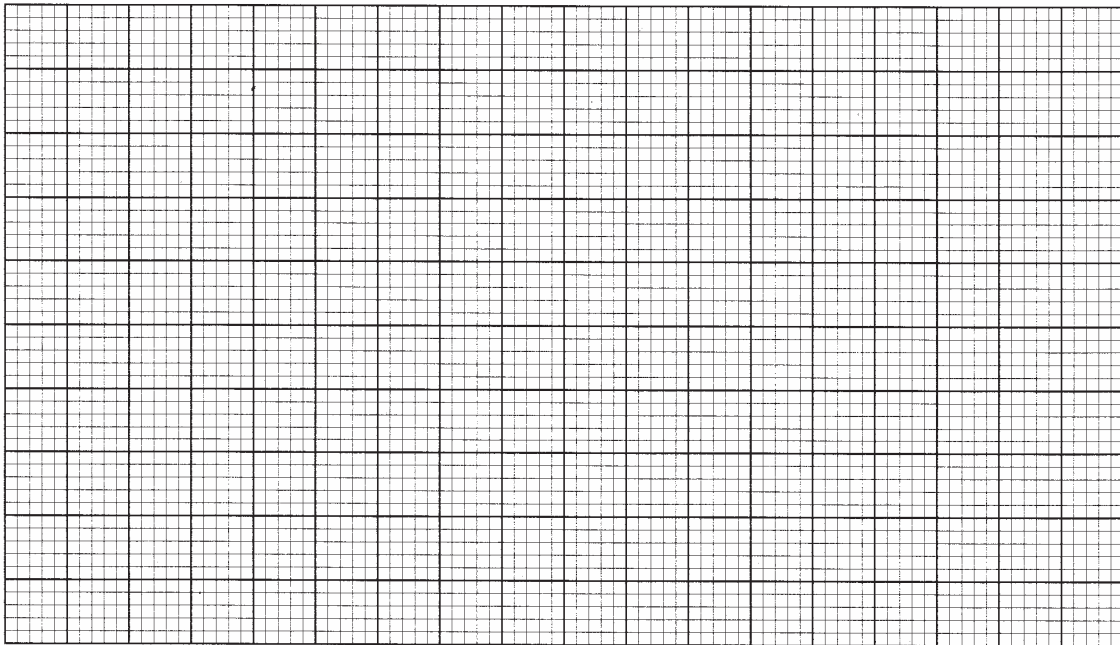
| | | | | | | | | | | | | | |
|-----|----|------|----|------|----|------|----|------|---|-------|---|------|-----|
| x | -4 | -3.5 | -3 | -2.5 | -2 | -1.5 | -1 | -0.5 | 0 | 0.5 | 1 | 1.5 | 2.0 |
| y | | -4.1 | | -1.1 | | -2.6 | | -9.4 | | -13.1 | | -7.9 | |

(2 marks)

- (b) On the grid provided, draw the graph $y = x^3 + 3x^2 - 4x - 12$ for $-4 \leq x \leq 2$.

Use the scale: Horizontal axis 2 cm for 1 unit and vertical axis 2 cm for 5 units.

(3 marks)



- (c) By drawing a suitable straight line, on the same grid as (b) above, solve the equation:

$$x^3 + 3x^2 - 5x - 6 = 0.$$

(5 marks)