

### 3.2 MATHEMATICS ALT B (122)

In the year 2012 Mathematics Alt B was tested in two papers. **Paper 1 (122/1)** and **Paper 2 (122/2)**. Each paper consisted of two sections: Section 1 (50 marks) short answer questions of not more than four marks each and Section II (50 marks), a choice of eight questions of 10 marks each where candidates answer any five. Paper 1 (122/1) tested mainly Forms 1 and 2 work while Paper 2 (121/2) tested mainly forms 3 and 4 work of the syllabus.

This report is based on an analysis of performance of candidates who sat the year 2012 KCSE Mathematics Alt B.

#### 3.2.1 CANDIDATES' GENERAL PERFORMANCE

*Table 9: Candidates' Performance in Mathematics Alternative B in the years 2010 - 2012*

Year	Paper	Candidature	Maximum score	Mean Score	Standard Deviation
2010	1	1221	100	20.40	16.85
	2		100	17.96	15.91
2011	1	1247	100	12.11	12.75
	2		100	14.65	15.43
	<b>Overall</b>		<b>200</b>	<b>26.64</b>	<b>26.89</b>
2012	1	1281	100	9.27	12.48
	2		100	9.77	13.48
	<b>Overall</b>		<b>200</b>	<b>18.99</b>	<b>25.19</b>

From the table the following observations can be made:

- (i) The subject registered a decline in performance when compared to the previous year's performance.
- (ii) The mean score of the papers was quite low.

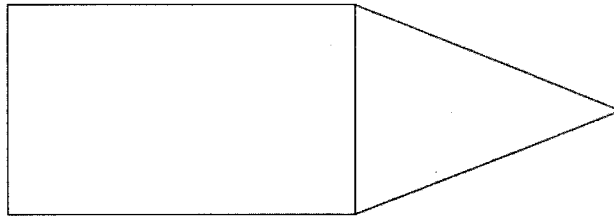
#### INDIVIDUAL QUESTION ANALYSIS

Mathematics Alt B has continued to have a dismal performance since its inception in 2010. With this kind of performance, most questions were poorly performed. The questions discussed below are those considered to be dismally performed.

**3.2.2 Mathematics Alt. B Paper 1 (122/1)**

**Question 9**

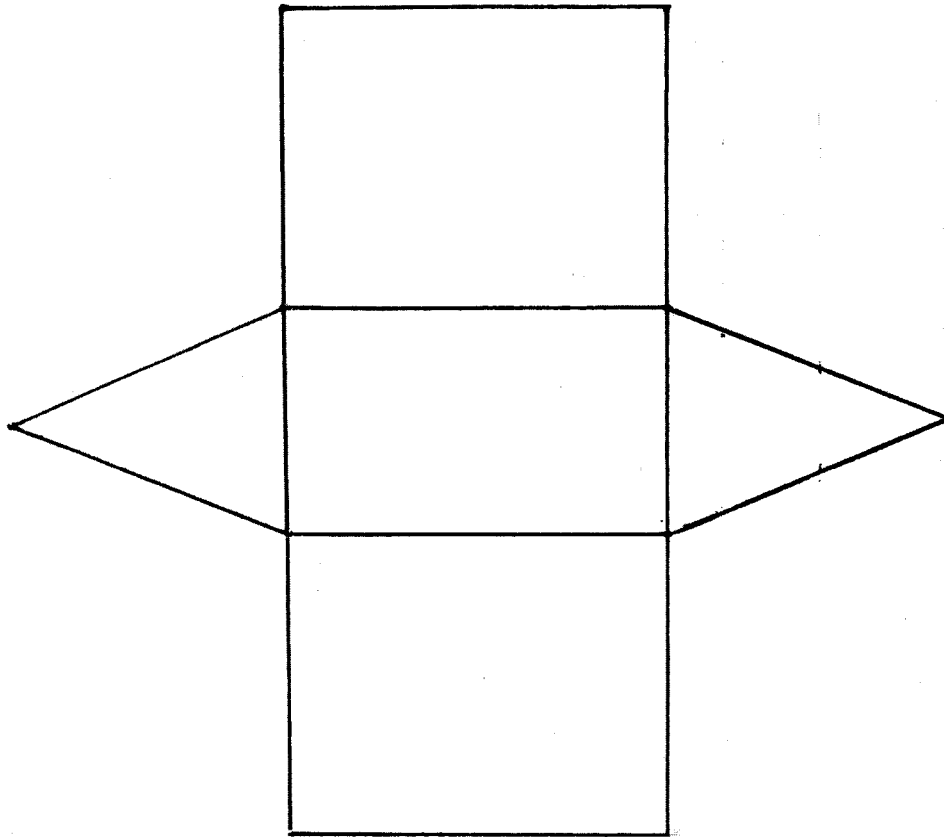
*The figure below is part of a net of a triangular prism. Complete the net. (3 marks)*



**Weaknesses**

Most candidates could not draw the net accurately. Some drew the nets of a rectangular pyramid

**Expected response**



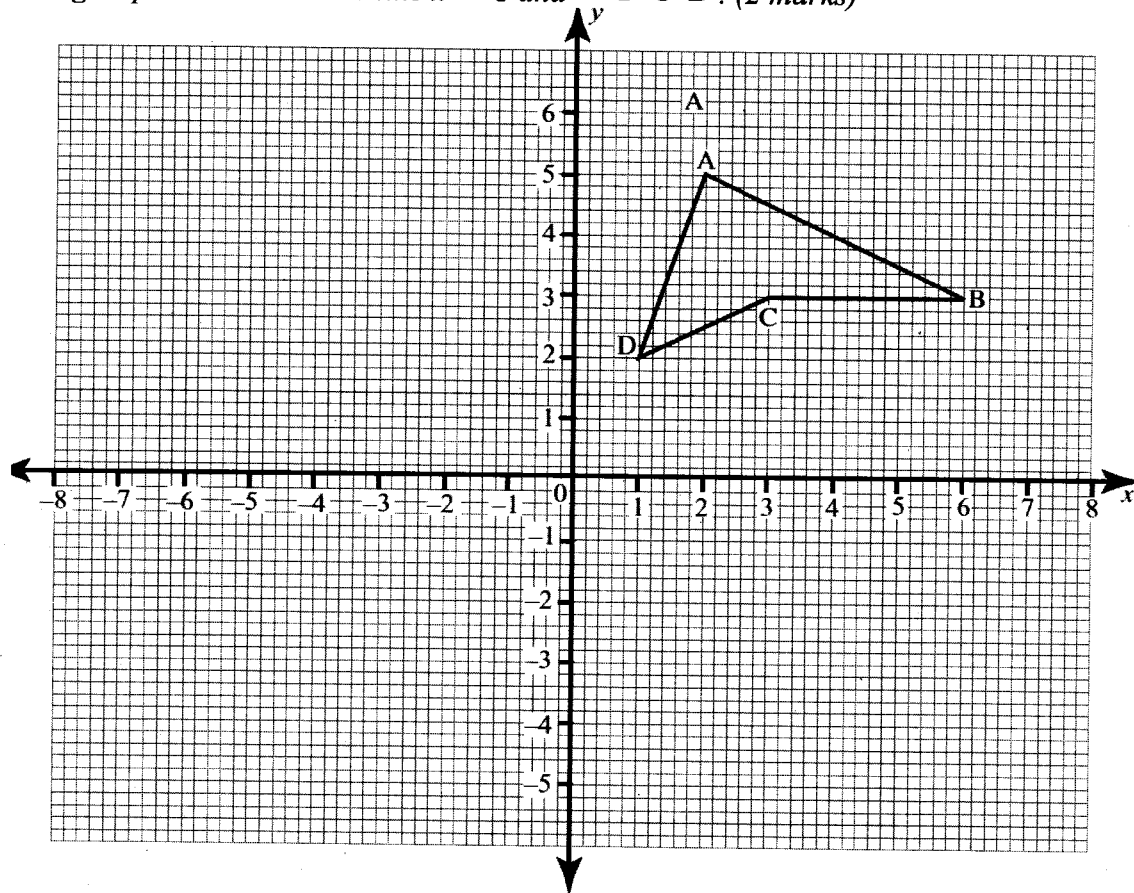
**Advice to teachers**

Teach different types of solids and their corresponding nets.

### Question 11

Quadrilateral ABCD shown below, whose vertices are A (2, 5), B (6, 3), C (3, 3) and D (1, 2) is mapped onto A' B' C' D' by a reflection in the line  $x = -1$ .

(a) On the grid provided draw the line  $x = -1$  and A' B' C' D'. (2 marks)

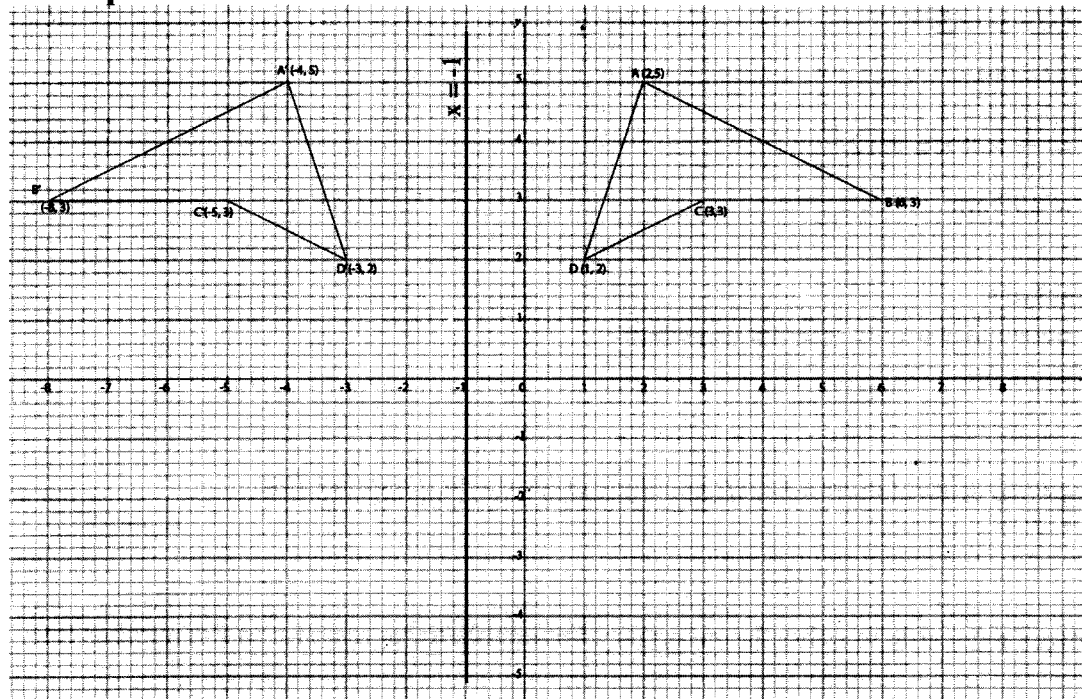


(b) State the type of congruence between quadrilateral ABCD and A' B' C' D'. (1 mark)

#### Weaknesses

Many candidates could not draw the line  $x = -1$  and instead drew  $y = -1$ . Majority also didn't know the type of congruence.

**Expected response**

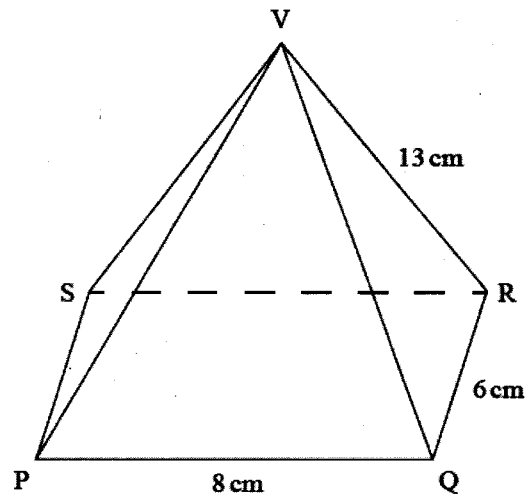


**Advice to teachers**

Give more exercises and help students differentiate between the lines  $x = a$  and  $y = b$ .

**Question 14**

The figure below represents a rectangular based pyramid  $VPQRS$ .  $PQ = 8$  cm,  $QR = 6$  cm and  $VP = VQ = VR = VS = 13$  cm.



Calculate:

- (a) the vertical height of the pyramid; (2 marks)
- (b) the volume of the pyramid. (2 marks)

**Weaknesses**

Candidates were unable to use the Pythagoras theorem to obtain the height of the pyramid, hence could not find the volume.

**Expected response**

(a) height =  $\sqrt{13^2 - 5^2}$   
= 12 cm

(b) volume =  $\frac{1}{3} \times 8 \times 6 \times 12$   
= 192 cm<sup>3</sup>

**Advice to teachers**

Teach more thoroughly on the volume of prisms.

**Question 15**

Solve the inequality given below and represent the solution on a number line.

$-5x - 3 > 2x + 4$

(2 marks)

**Weaknesses**

Many candidates were able to solve the inequality but unable to represent it in the number line.

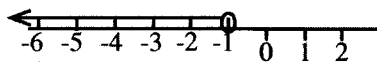
**Expected response**

$-5x - 3 > 2x + 4$

$-5x - 2x - 3 > 4$

$-7x > 7$

$x < -1$

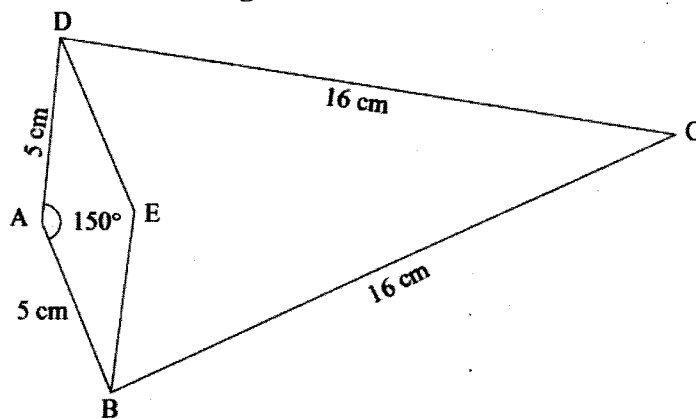


**Advice to teachers**

Teach more on the representation of the inequalities on the number line.

**Question 18**

The figure below shows a kite ABCD and a rhombus ABED. AB = AD = 5 cm, BC = DC = 16 cm and angle DAB = 150°.



Calculate:

(a) the area of the rhombus ABED; (2 marks)

(b) (i) the length of diagonal BD, correct to one decimal place; (2 marks)

(ii) the area of triangle BCD. (3 marks)

(c) the area of the kite ABCD. (3 marks)

## Weaknesses

Calculation of the length BD was a challenge to most candidates

### Expected response

$$\begin{aligned} \text{a) } 2 \times \frac{1}{2} \times 5 \times 5 \sin 150^\circ \\ = 12.5 \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{b) (i) } \frac{\frac{1}{2}BD}{5} &= \sin 75^\circ \\ BD &= 9.7 \end{aligned}$$

(ii) Area of  $\Delta BCD$

$$S = \frac{1}{2}(9.7 + 16 + 16) = 20.85$$

$$\begin{aligned} A &= \sqrt{20.85(20.85 - 9.7)(20.85 - 16)^2} \\ &= \sqrt{20.85 \times 11.15 \times (4.85)^2} \\ &= 73.95 \end{aligned}$$

c) Area of kite ABCD

$$\begin{aligned} \frac{1}{2} \times 12.5 + 73.95 \\ = 80.2 \text{ cm}^2 \end{aligned}$$

### Advice to teachers

Give more questions on application to trigonometry

### Question 24

A room measuring  $4x$  metres by  $(2x + 2)$  metres is to be carpeted leaving a uniform margin all around the walls. The dimensions of the carpet are  $(3x + 1)$  metres by  $2x$  metres.

(a) Write an expression for the area of the carpet. (1 mark)

(b) If the area of the margin is 36 square metres, find:

(i) the value of  $x$ ; (3 marks)

(ii) the area of the carpet. (2 marks)

(c) The carpet costs Ksh 1600 per square metre. The cost of transport and labour is 2.5% of the cost of the carpet. Calculate the total cost of carpeting the room. (4 marks)

### Weaknesses

Candidates were unable to interpret the question to come up with the required quadratic equations

### Expected response

a)  $(3x + 1)2x = 6x^2 + 2x$

b) (i)  $(2x + 2)4x = 6x^2 + 2x + 36$

$$2x^2 + 6x - 36 = 0$$

$$(2x + 12)(x - 3) = 0$$

$$x = 3$$

(ii) area of carpet

$$= 3(3) + 1 + 2(3)$$

$$= 10 \times 6 = 60\text{m}^2$$

c) Cost of carpet

$$= 60 \times 1600$$

$$= 96000$$

Cost of labour

$$= 96000 \times 0.025$$

$$= 2400$$

Total cost

$$= 96000 + 2400$$

$$= 98400$$

### Advice to teachers

Give more questions on application to quadratic equations

### 3.2.2 Mathematics Alt. B Paper 2 (122/2)

#### Question 1

Round off each of the numbers in the expression  $169.2 + \frac{92.4 \times 4.9}{14.7}$  correct to one significant figure. Hence find the approximate value of the expression. (3 marks)

#### Weaknesses

Candidates confused significant figures with decimal place.

#### Expected response

$$200 + \frac{90 \times 5}{10} \\ = 245$$

#### Advice to teachers

Distinguish clearly between significant figures and decimal places when teaching.

#### Question 13

An agent was paid a commission of Ksh 50 000 per annum. The commission was increased by 10% annually. Calculate the total amount of money the agent was paid in 3 years. (3 marks)

#### Weaknesses

Most candidates could not recognize it is a G.P

#### Expected response

$$a = 50\,000; r = 1.1$$

$$s_n = 50\,000 \times \frac{(1.1)^3 - 1}{1.1 - 1} \\ = 165\,500$$

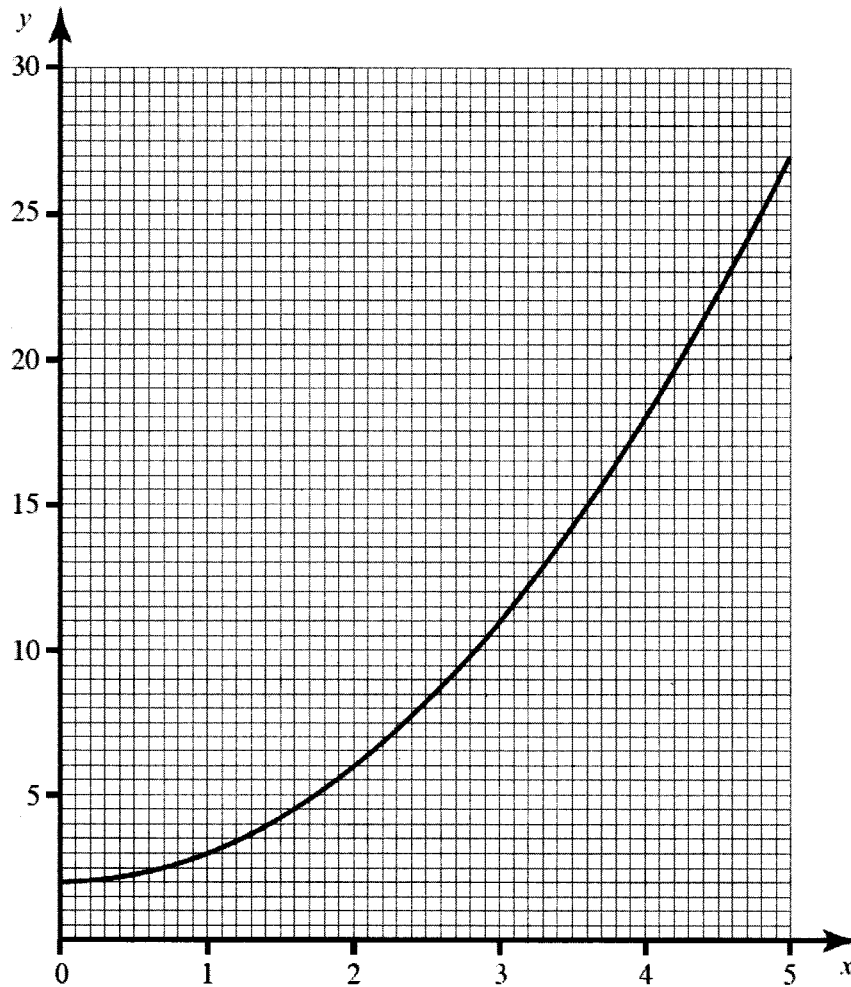
#### Advice to teachers

Give more examples on application of G.P



**Question 16**

The graph below represents a curve of an equation.



Use the trapezium rule with 5 strips of equal width to estimate the area, in  $cm^2$ , bounded by the curve, the  $x$ -axis,  $x = 0$  and  $x = 5$ . (3 marks)

**Weaknesses**

Identifying the ordinates and use of the trapezium rule was a big challenge to the candidates.

**Expected response**

<b>x</b>	0	1	2	3	4	5
<b>y</b>	2	3	6	11	18	27

$$y = x^2 + 2$$

$$Area = \frac{1}{2} \{ (2 + 27) + 2(3 + 6 + 11 + 18) \} cm^2$$

$$\frac{1}{2} \{ 29 + 2 \times 38 \}$$

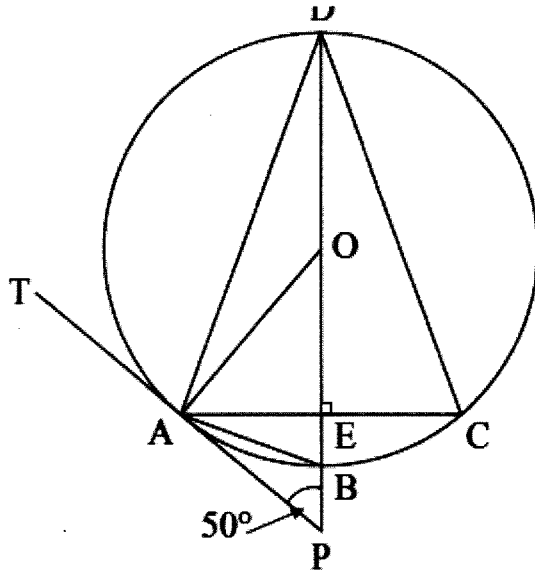
$$= 52.5 cm^2$$

### Advice to teachers

Give more practice to students on finding the area under a curve.

### Question 20

In the figure below,  $O$  is the centre of the circle of radius 2.5 cm.  $DOB$  is a straight line and is perpendicular to the chord  $AC$  at  $E$ . Line  $TP$  is a tangent to the circle at  $A$  and angle  $APD = 50^\circ$ .



(a) Calculate, correct to 2 decimal places, the length of:

(i)  $OP$ ;

(2 marks)

(ii)  $AP$ ;

(2 marks)

(iii)  $AC$ .

(2 marks)

(b) Determine the size of:

(i) angle  $ADC$ ;

(2 marks)

(ii) angle  $ACD$ .

(2 marks)

### Weaknesses

Applying trigonometric ratios to find the lengths was a challenge to the candidates

### Expected response

(a) (i)

$$\begin{aligned}OP &= \frac{2.5}{\sin 50^\circ} \\ &= 3.26 \text{ cm}\end{aligned}$$

(ii)

$$\begin{aligned}AP &= \frac{2.5 \sin 40^\circ}{\sin 50} \\ &= 2.10\end{aligned}$$

(iii)

$$\begin{aligned}AC &= 2 AE \\ &= 2 \times 2.5 \sin 40^\circ \\ &= 3.21\end{aligned}$$

(b) (i)

$$\begin{aligned}\angle PAC &= 40^\circ \\ &(\text{sum of } \angle\text{s in } \triangle AEP)\end{aligned}$$

$$\begin{aligned}\angle ADC &= 40^\circ \\ &(\text{angle in alt. segment})\end{aligned}$$

(ii)

$$\begin{aligned}\angle ACD &= \frac{1}{2}(180^\circ - 40^\circ) \\ &= 70^\circ\end{aligned}$$

### Advice to teachers

Give students more practice on angle properties of a circle and use of trigonometric ratios