

## UNIVERSITY EXAMINATION 2015/2016

# SCHOOL OF PURE AND APPLIED SCIENCES DEPARTMENT OF MATHEMATICS, STATISTICS AND ACTUARIAL SCIENCE

### BED (SCIENCE), BED (ARTS) AND BSNE SCHOOL BASED

UNIT CODE: BMA2108

Mount Kenya

UNIT TITLE: ORDINARY DIFFERENTIAL

**EQUATION 1** 

**DATE: DECEMBER 2015** 

MAIN EXAM

TIME: 2 HOURS

Instructions: Answer question one and any other two

#### Question one (30 marks)

a) Define and give an example of an ordinary differential equation.

(3 Marks)

b) Solve 
$$\frac{dy}{dx} = \frac{2x^2}{y^3}$$

(3 Marks)

c) Show that 
$$(3x^2 + 4xy)dx + (2x^2 + 2y)dy = 0$$
 is exact

(3 Marks)

(4 Marks)

d) Show that 
$$y = e^{4t}$$
 is a solution to the differential equation  $y^1 - 4y = 0$ 

(3 Marks)

e) Solve 
$$x \frac{dy}{dx} + y = x^2$$

(5 Marks)

f) Solve 
$$\frac{d^3y}{dx^3} + 10\frac{dy}{dx} + 25y = 0$$

(3 Marks)

Question two (20 marks)

a) Define homogenous equation of first order.

(3 Marks)

- b) Show that  $\frac{xy}{x^2 + y^2}$  is a homogenous function in x and y (3 Marks)
  - ii) Using the method of separation of variables solve the equation in 2(b) I above (6 Marks)
- c) Suppose that a differential equation has a regular singular point  $x_0 = 0$  and has indicial roots and r=2 suppose further that the recurrence relation for the coefficients for the first solution y1 is as follows  $a_n = \frac{-(n+1)}{n(n+3)}a_n 1$ . Let  $Q_0 = 1$  and find y1 (8 Marks)

Question three (20 marks)

a) Define Bernoulli equation

$$\frac{1}{1} \frac{17}{12} = 7 = 10$$

(2 Marks)

b) Solve  $\frac{dy}{dx} + 4y^5 \Rightarrow \frac{dy}{dx} - y = 4y^5$ 

(8 Marks)

c) Solve the equation 
$$\frac{d^4y}{dx^4} + 2\frac{d^3y}{dx^3} + \frac{d^2y}{dx^2} = \sin 3x$$

(10 Marks)

Question four (20 marks)

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a) The point xo=0 is an ordinary point of the differential equation  $(1-x^2)y^{11}-2y^1+3y=0$ . Begin the process of finding a series solution for this

differential equation. Find the recurrence relation for the coefficient a<sub>n</sub>.

(10 Marks)

b) Solve the initial value problem 
$$\frac{dy}{dx} = \frac{y^2 + 4x^2}{4xy}$$
,  $y(1) = 2$ 

(10 Marks)

#### Question five (20 marks)

a) Show  $y_1 = x^2$  is a solution to the differential equation  $x^2y^{11} - (x^2 + 4x)y^1 + (2x + 6)y = 0$ .

Also find a second independent solution in y2

(10 Marks)

b) Solve the following equation 
$$xy^1 + 4y = x^3y^2$$

(10 Marks)