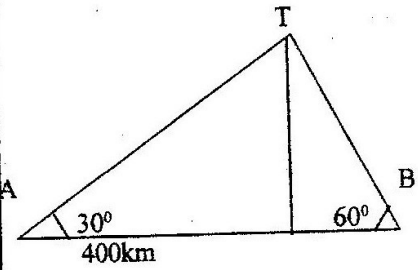


K.C.S.E 1997 MATHEMATICS PAPER 121/1 MARKING SCHEME

	SOLUTION	MARKS	ALTERNATIVE METHOD										
1.	<table style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th style="width: 30%;">NO</th> <th style="width: 70%;">LOG</th> </tr> </thead> <tbody> <tr> <td style="border: 1px solid black; padding: 5px;">1934</td> <td style="border: 1px solid black; padding: 5px;"> 3.2865×2 6.5730 </td> </tr> <tr> <td style="border: 1px solid black; padding: 5px;">0.0324</td> <td style="border: 1px solid black; padding: 5px;"> $3.5105 \div 2$ $4 + 4.5105$ 2 2.75525 </td> </tr> <tr> <td style="border: 1px solid black; padding: 5px;">436</td> <td style="border: 1px solid black; padding: 5px;"> $5.32825 -$ 2.63950 </td> </tr> <tr> <td style="border: 1px solid black; padding: 5px;">4.884</td> <td style="border: 1px solid black; padding: 5px;">2.6888</td> </tr> </tbody> </table> <p style="text-align: center;">= 488.4 OR 488.5✓</p>	NO	LOG	1934	3.2865×2 6.5730	0.0324	$3.5105 \div 2$ $4 + 4.5105$ 2 2.75525	436	$5.32825 -$ 2.63950	4.884	2.6888	M1 M1 M1 A1 <hr style="width: 50%; margin: 0 auto;"/> 4	all ✓ logs Multiplication and division Addition and subtraction
NO	LOG												
1934	3.2865×2 6.5730												
0.0324	$3.5105 \div 2$ $4 + 4.5105$ 2 2.75525												
436	$5.32825 -$ 2.63950												
4.884	2.6888												
2.	<p>G.C.F. = XY^2 ✓ $XY^2(x^2 - 4y^2)$ ✓ $xy^2(x - 2y)(x + 2y)$ ✓</p>	B1 B1 B1 <hr style="width: 50%; margin: 0 auto;"/> 3											
3.	<p>SR=RQ ∴ ∠QRS = 55° ∠SQP = 55° ALT to ∠RSQ ∠STQ = 90° - 55° = 35° OR 180° - (90° + 55°) ✓ = 35° ✓</p>	B1B1 <hr style="width: 50%; margin: 0 auto;"/> 2											
4.	<p>$\frac{ar^2}{a + ar} = \frac{16}{12} = \frac{4}{3}$ ✓</p> <p>$3r^2 - 4r - 4 = 0$ $3r^2 - 6r - 2r - 4 = 0$ ✓ $(3r + 2)(r - 2) = 0$ $r = \frac{-2}{3}$ or $r = 2$ $r = \frac{-2}{3}$ ✓</p>	B1 M1 A1											

SOLUTION	MARKS	ALTERNATIVE METHOD
 <p> $X = 400 \cos 60^\circ = 200\text{m}$ $H = 200 \sin 60^\circ$ $H = 200 \times 0.8660$ $= 173.2 \text{ m}$ </p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>3</p>	<p>For Sketch</p> <p>ALT. METHOD $\tan 30^\circ = \frac{h}{400 - x}$ $h = (400 - x) \tan 30^\circ$</p> <p>$\tan 60^\circ = \frac{h}{x} \therefore h = x \tan 60^\circ$ $1.732 x = 400 \times 0.5774 - 0.5774x$ $x = 230.96$ 2.3095 $h = 230.96 \times 1.7301 = 113.2\text{m}$</p>
<p>6. Volume of the cone = $\frac{1}{3} \times \frac{22}{7} \times 7 \times 7 \times 18 \checkmark$ $= 924 \text{ cm}^3$</p> <p>Let change in height be H Volume of water displaced = $\frac{22}{7} \times 14 \times 14 \times H$ $= 616 \text{ cm}^3$</p> <p>$\pi \times 14 \times 14 \times H = \frac{1}{3} \pi \times 7 \times 7 \times 18$ $H = \frac{49 \times 6}{14 \times 14} = 1.5 \checkmark$</p>	<p>M1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>4</p>	
<p>7. CR = $\frac{4000 \times 100}{24,000} = 1\frac{2}{3}$ or $1\frac{2}{3}\% \checkmark$</p> <p>commission = $\frac{5}{3} \times \frac{98}{100} \times \frac{360,000}{100} \checkmark$ $= \text{Sh. } 5880 \checkmark$</p>	<p>B1</p> <p>B1</p> <p>A1</p> <p>3</p>	<p>Accept 5891, 5891.80 When logs are used</p>

	SOLUTION	MARKS	ALTERNATIVE METHOD
8.	(a) Mode = 934 (b) take any no = a $a = 934 - 9 = 925$ (ii) $x = 925 + \frac{115}{20}$ $x = 930.75$	B1 B1 M1 A1	
9.	$\begin{pmatrix} 1 & 3 \\ 5 & 3 \end{pmatrix} \begin{pmatrix} 3 & 1 \\ 5 & -1 \end{pmatrix} \begin{pmatrix} 3 & 1 \\ 5 & -1 \end{pmatrix} \begin{pmatrix} p & 0 \\ 0 & q \end{pmatrix}$ $18 = 3P$ $5P = 30$ $P = 6$ $P = 6$	3 B1 B1 B1 3	
10.	$\frac{dy}{dx} = 3ax^2 - 6x - 2$ $3ax^2 - 6x - 2 = 1$ $3a - 6 - 2 = 7$ at $x = 1$ $3a = 15$ $a = 5$	M1 M1 A1	
11.	$\sin \theta = \frac{4}{5}$ or -0.8 3rd Quadrant $180 + 53.13 = 233.13$ 4th Quadrant $360 - 53.5 = 306.87$	B1 B1 B1 2	
12.	Let the buying price be x Profit = $(1040 - x)$ Loss = $(x - 880)$ $1040 - x = 3(x - 880)$ $4x = 3680$ $x = \text{Sh. } 920$	B1 M1 A1 3	
13.	$y(cx^2 - a) = b - bx^2$ $bx^2(b + yc) = b + ya$ $x^2 = \frac{b + ya}{b + yc}$ $x = \sqrt{\frac{b + ya}{b + yc}}$	M1 M1 A1 3	

SOLUTION	MARKS	ALTERNATIVE METHOD
<p>14. (a) $\frac{300}{t-1}$</p> <p>(b) Speed of the bus = $\frac{500}{t-1}$</p> <p>$\frac{500}{t-1} : \frac{300}{t-1} = 5:3$</p>	<p>B1</p> <p>B1</p> <p>A1</p> <hr/> <p>3</p>	
<p>15. Let the cost be sh c - cup s - spoons</p> <p>$3x + 4s = 324$ $5c - 2s = 228$</p> <p>$15c + 20s = 1620$ $15c - 6s = 684$ <hr/>$26s = 936$</p> <p>$s = 36$ $c = 60$</p>	<p>M1</p> <p>M1</p> <p>A1</p>	
<p>16(a) $R = \frac{1}{0.000016} = \frac{1}{1.6} \times 10^5$</p> <p>$= 62500$</p> <p>(b) (i) Approximate value = $\frac{1}{0.00315 - 0.00313}$</p> <p>$= \frac{1}{0.00002} = \frac{1}{2} \times 10^5$</p> <p>$= 50000$</p> <p>(ii) Error = $62500 - 50000$ $= 12500$</p>	<p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>B1</p> <hr/> <p>3</p>	

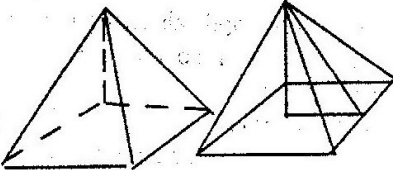
SOLUTION	MARKS	ALTERNATIVE METHOD																								
17. (a) (i) $(0.8 \times 1.2) + (1.2) \times 2 + (0.8 \times 1.2) + 1/2 \times 0.8 \times 0.3 \times 2$ $= 0.96 + 2.4 + 1.6 + 0.24 \checkmark$ $= 5.2 \text{ m}^2 \checkmark$ (ii) $0.6 \times 1.2 \times 2 \checkmark$ $= 1.44 \checkmark$ (b) $300 \times 144 \checkmark$ 350×5.2 $= 432 + 1830 = \text{Sh. } 225^2 \checkmark$ (c) $432 (1.5)^2 \checkmark$ $= \text{Sh. } 972 \checkmark$	A1 M1 M1 A1 M1 A1 <hr/> 8	M1																								
18. (a) (i) $120 \times 27 \checkmark$ $= 3240 \checkmark$ (ii) $120 \times 27 \times 1.853 = 6003.72 \text{ km} \checkmark$ (b) Speed in km/h $\frac{6003.72}{120} = 50.031 \text{ km/h} \checkmark \checkmark$ (c) $\frac{\theta \times 2 \times 22 \times 6370 \cos 5}{360 \times 7} = 6003.72$ $\theta = \frac{6003.72 \times 360 \times 7}{2 \times 22 \times 6370 \cos 5}$ $= 54.19^\circ$ Position $(5^\circ \text{N}, 99.19^\circ \text{E}) \checkmark$	M1 A1 M1 M1/A1 A1 <hr/> 8	(c) <u>ALT. METHOD</u> $\theta \times 600 \cos 5^\circ = 3240 \quad \text{M1}$ $\theta = \frac{32409}{60 \cos 5^\circ}$ $(50^\circ \text{N}, 99.21^\circ \text{E}) \quad \text{A1}$																								
20. <table border="1" style="margin: 10px auto;"> <tr> <td>x</td> <td>-4</td> <td>-3</td> <td>-2</td> <td>-1</td> <td>0</td> <td>-0.5</td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> </tr> <tr> <td>y</td> <td>-14</td> <td>-6</td> <td>0</td> <td>4</td> <td>6</td> <td>0.25</td> <td>6</td> <td>4</td> <td>0</td> <td>-6</td> <td>-14</td> </tr> </table> B1 for all values correct Line graph: $y=2-2x \checkmark$ (b) $x=1 \quad x=4 \checkmark$ (c) $6 + x^2 - x = 2-2x$ $x^2 - 3x - 4 = 0 \checkmark$ Suitable scale plotting Smooth curve $x = -1$ or	x	-4	-3	-2	-1	0	-0.5	1	2	3	4	5	y	-14	-6	0	4	6	0.25	6	4	0	-6	-14	L1	B1 B1 L1 B1 B1 B1 - should be correctly read from the table - working be shown ∴ Nil Turning points of the curve must be well drawn.
x	-4	-3	-2	-1	0	-0.5	1	2	3	4	5															
y	-14	-6	0	4	6	0.25	6	4	0	-6	-14															

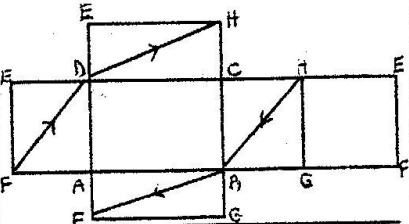
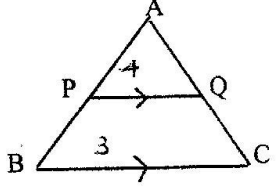
SOLUTION	MARKS	ALTERNATIVE METHOD
21.(a) 0.9×0.8 $= 0.72$ (b) 0.1×0.2 $= 0.02$ (c) $0.9 \times 0.2 + 0.8 \times 0.1$ or $(0.9 \times 0.2 + (0.8 \times 0.1))$ $= 0.26$ (d) $1 - 0.02$ $= 0.95$	M1 A1 M1 A1 M1 A1 M1	
22. (a) (i) $\underline{AB} = \underline{OB} - \underline{OA} = b - a$ (ii) $\underline{CD} = \underline{CB} + \underline{BD}$ $= (a - b) + \frac{1}{2} b$ $= a - \frac{2}{3} b$ (b) (i) $\underline{DE} = K \underline{CD}$ $= K(a - \frac{2}{3} b)$ (ii) In $\triangle ODE$ $\underline{OD} + \underline{DE} = \underline{OE}$ $\frac{4}{3} b + K(a - \frac{2}{3} b) = a + ma$ $(\frac{4}{3} - \frac{2}{3}K)b = 0$ $K = 2$ $Ka = a + ma$ $K = 1 + m$ $2 = 1 + m$ $m = 1$	B1 B1 B1 B1 M1 A1 M1 A1 8	
23. (a) $\pm 180^\circ$ rotation centre origin Matix $M = \begin{bmatrix} -1 & 0 \\ 0 & -1 \end{bmatrix}$ $\begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} 2 & 4 & 4 \\ 0 & 1 & 3 \end{bmatrix} = \begin{bmatrix} 2 & 4 & 4 \\ 0 & -1 & -3 \end{bmatrix}$ $\begin{bmatrix} 2a + 0 & 4a + b & 4a + 8b \\ 2c + 0 & 4c + d & 4c + d \end{bmatrix} = \begin{bmatrix} -2 & 4 & 4 \\ 0 & -1 & -3 \end{bmatrix}$ $2a = -2$ $4c + d = -1$ $a = -1$ $d = -1$ $4a + b = 4$ $m \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$ $b = 4 - 4$ $b = 0$ $2c - 0 = 0$ $c = 0$	B1 B1 B1 B1	

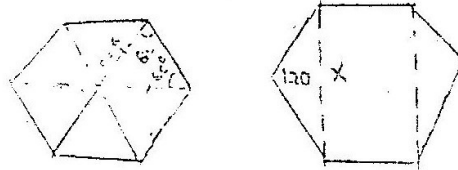
SOLUTION	MARKS	ALTERNATIVE METHOD
<p>(b) $\begin{bmatrix} 2 & 1 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} 2 & 4 & 4 \\ 0 & 1 & 3 \end{bmatrix} \begin{bmatrix} 4 & 9 & 11 \\ 2 & 5 & 7 \end{bmatrix}$ $\begin{bmatrix} 2 \times 2 + 0 \\ 2 \times 1 + 0 \end{bmatrix} \begin{bmatrix} 2 \times 4 + 1 \\ 1 \times 4 + 1 \end{bmatrix} \begin{bmatrix} 2 \times 4 + 3 \\ 4 + 3 \end{bmatrix} \begin{bmatrix} 4 & 9 & 11 \\ 2 & 5 & 7 \end{bmatrix}$ $A''(4.2) \quad B''(9.5) \quad C''(11.7)$</p> <p>(c) Area of $\triangle ABC = \frac{1}{2} \times 2 \times 2 = 2 \text{ cm}^2 \checkmark$ Determinant of $\begin{bmatrix} 2 & 1 \\ 1 & 1 \end{bmatrix} = 2 - 1 = 1 \checkmark$ Area of $\triangle A'' B'' C'' = 1 \times 2 = 2 \text{ cm}^2 \checkmark$</p>		
<p>24. (a) $OT = \frac{1}{3} \begin{bmatrix} 1 \\ -2 \end{bmatrix} + \frac{2}{3} \begin{bmatrix} 4 \\ 10 \end{bmatrix} = \begin{bmatrix} 3 \\ 6 \end{bmatrix} \quad \checkmark$ $T[3,6]$</p> <p>(b) Gradient PQ = 4 Gradient Normal = $-\frac{1}{4}$</p> <p>(ii) $\frac{y-6}{x-3} = -\frac{1}{4}$ $4(y-6) = -(x-3)$ $4y - 24 = -x + 3$ $4y = -x + 27$</p> <p>(iii) $(6\frac{3}{4} - 6)^2 + (3-0)^2$ $= \sqrt{9.5625}$ $= 3.092$ $= 3.09 \text{ (Sig. Fig)}$ or 3.093</p>	<p>M1</p> <p>A1</p> <p>2</p> <p>M1</p> <p>A1</p> <p>B1</p> <p>A1</p> <p>B1</p> <p>A1</p>	

K.C.S.E 1997 MATHEMATICS PAPER 121/2 MARKING SCHEME

SOLUTION	MARKS	ALTERNATIVE METHOD
<p>1. $\frac{19 \times 32}{20 \times 38}$</p> <p align="center">$= 0.8 = \frac{4}{5}$</p>	M1	for \checkmark removal of decimal points or 0.032 and 0.0038 stated in standard form.
<p>2. Let number of ten shillings coins be t</p> <p>\therefore number of five shillings coins = 2t</p> <p>Number of one shilling coins = 21-3t</p> <p>Value = 10t + 2t x 5 + (21 - 3t) x 1 = 72</p> <p>= 17t = 51</p> <p>t = 3</p>	<p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p>	<p><u>ALT. METHOD</u></p> <p>Let number of 5-sh coins be f</p> <p>Number of 10 sh. coins be $\frac{1}{2}f$</p> <p>Number of 1-sh coins = 21 - $1\frac{1}{2}f$</p> <p>$\frac{1}{2}f \times 10 + 5f + (21 - 1\frac{1}{2}f) \times 1 = 72$</p> <p>17f = 102</p> <p align="right">f = 6</p> <p>\therefore no of 10 sh coins = 3 A1</p>
<p>3. No. of yens $\frac{30000}{0.5446}$</p> <p>= 55086</p>	<p>M1</p> <p>A1</p> <p>2</p>	Allow 55080 from tables
<p>4. \checkmark Const. of \perp bisector of BC</p> <p>\checkmark Const of \perp bisector of AC or AB</p> <p>Locus of P drawn</p>	<p>B1</p> <p>B1</p> <p>B1</p> <p>3</p>	
<p>5. Area of the sector = $\frac{75^\circ}{360} \times \frac{22}{7} \times 14 \times 14$</p> <p align="center">= 128.3 cm</p> <p>Area of $\Delta = \frac{1}{2} \times 14 \times 14 \sin 75^\circ$</p> <p align="center">= $\frac{1}{2} \times 14 \times 14 \times 0.9659$</p> <p align="center">= (6.5)</p> <p align="center">= 94.64 cm</p> <p>Area of segment = 128-94.64</p> <p align="center">= 33.66</p> <p align="center">or (33.68)LM</p>	<p>m1</p> <p>m1</p> <p>m1</p> <p>A1</p> <p>4</p>	<p>simplified expression or equivalent</p> <p>Simplify on P</p> <p>Subtract at simplified numerical stage and at least one area is correctly obtained.</p>

SOLUTION	MARKS	ALTERNATIVE METHOD
<p>6. Labelled sketch of the pyramid (dimensions may be implied) $VN = 10^2 + 3^2 = 109$ $= 10.44 \text{ cm}$</p>	<p>B1 M1 A1 <hr/>3</p>	
<p>7. $\left(\frac{1}{3^3}\right)^m \times (3^4) - 1 = 3^5$ or $3^{-3m} \times 3^{-4} \times 3^4 = 3^5$ $= -3m - 4 = 5$ $m = -3$</p>	<p>m1 m1 A1</p>	<p>For equivalent in power of 3 at least one index</p> <p>Alternative method $-\ln \log 27 - 1 \times \log 81 = \log 243$ $-m \times 1.4314 \times 1.9085 = 23856$ M1 $-m = 4.2941$ M1 1.4314 $= -3.001$ A1</p>
<p>8. $3.55 \pm 0.05, 4.85 \pm 0.05, 5.7, 6.3, 6.7$ & 6.9 Area = $\frac{1}{2} \times 1(0+7+2(3.6+4.9+5.7+6.3+6.7+6.9))$ $= \frac{1}{2} \times 1(7+68.20)$ $= 37.6$</p>	<p>B1 M1 M1 A1 <hr/>A1 4</p>	<p>for any 4 middle ordinates interval of $\frac{1}{2}$ MR-2</p> <p>Use of formular all dividual trapezia area for simplification of inner brackets in a trapezoidal rule Mid ordinate rule use MR-2</p>
<p>9. $(1-3x)^5 = 1+5(-3x)+10(-3x)^2+10(-3x)^3$ $= 1-15x+90x^2-270x^3 + \dots$ $= 3x = 0.03$ or $x = 0,1$ $(0.97)^5 = 1-15(0.01)+90(0.01)^2-270(0.01)^3$ $= 1-0.15+0.009-0.00027$ $= 0.85873$ $= 0.8587$ to 4 d.p.</p>	<p>M1 A1 B1 M1 <hr/>A1 5</p>	<p>For complete expansion to the expansion accept only to x^3 incase of any (condone) error</p> <p>or $1+5t-0.03+10(0.03)^2+10(-0.03)^3$</p>

SOLUTION	MARKS	ALTERNATIVE METHOD
<p>10. Any/drawn and labelled net of a net of a cuboid (condone net of a cube) ✓path drawn All/directions (condone a net of cube award first B1. Diff net 12mm</p>	<p>E1 B1 B1 3</p>	
<p>11. (i) AQ : QC = 4:3 allow 8:6 (ii) $QC = \frac{3 \times 14}{7}$ = 6 cm</p>	<p>B1 B1 2</p>	
<p>12. $\frac{14(\sqrt{7} + \sqrt{2}) - 14(\sqrt{7} - \sqrt{2})}{(\sqrt{7} - \sqrt{2})(\sqrt{7} + \sqrt{2})}$ $= \frac{\sqrt{7} \cdot 2 + \sqrt{2} \cdot 7 - \sqrt{7} \cdot 2 + 2\sqrt{7}}{7-2}$ $\frac{4\sqrt{7}}{5}$ ∴ $a = \frac{4}{5}$ b = 0</p>	<p>M1 M1 A1 A1 4</p>	<p>single term or write common 2 terms with common denominator expansion of both numerator & denominator</p>
<p>13. $\frac{48.4+56.25+50.3+49.0}{4}$ = 50.99 $\frac{56.25 + 50.3+49.0+45.6}{4} = 50.29$ $\frac{50.3+49.0+45.6+57.65}{4} = 50.65$ }</p>	<p>M1 M1 A1</p>	<p>for one moving average any expression for the other two moving average for 50.99, 50.29, 50.64</p>

<p>14. Let Onduso take x days \Rightarrow Mogaka takes $x+5$ days $\therefore \frac{1}{x} + \frac{1}{x+5} = \frac{1}{6}$ $6(x+5) + 6x = x(x+5)$</p> <p>$x^2 - 7x - 30 = 0$ $(x-10)(x+3)$ $x = 10, -3$ \therefore Onduso takes 10 days</p>	<p>M1 M1 MI A1 4</p>	<p>or equivalent \checkmark equivalent (removal of all denominators) equivalent for factorization or use of formula.</p>
<p>15. Speed of slower athlete = $\frac{800}{108}$ \therefore Distance = $\frac{800 \times d}{108}$ $\frac{4}{4} = 29.63$</p>	<p>M1 A1 2</p>	<p><u>ALTE.METHOD</u> Slower speed $\frac{800}{108}$ Dist $\frac{800 \times 104}{108}$ R.V = $\frac{800 - 800}{104 \times 108}$ $= 0.2849 \therefore$ dis. $= 0.2849 \times 104 = 29.63$</p>
<p>16. (i) Area of Equi. $\Delta = \frac{1}{2} \times 6 \times 6 \sin 60^\circ$ $= \frac{1}{2} \times 6 \times 6 \times 0.8660$ $= 15.588 (15.59)$ X-section Area = $\frac{1}{2} \times 6 \times 6 \times 0.8660 \times 6$ $= 15.59 \times 6$ $= 93.54 (93.528)$</p> <p>(ii) Vol. of prism = 93.54×30 $= 2806.2 (2805.9)$</p>	<p>MI MI A1 MI A1 5</p>	 <p><u>ALT. METHOD</u> Area of 1 side $\Delta = \frac{1}{2} \times 6 \times 6 \times \sin 120^\circ$ $= \frac{1}{2} \times 6 \times 6 \times 0.8660$ $\frac{1}{2} \times 6 \times 6 \times \sin 30^\circ = 15.57 \Rightarrow x = 10.27$ X-sec area = $15.59 \times 2 + 6 \times 10.27$ $= 93.52$ A1 Vol = 93.52×30 M1 $= 2805.6$ A1 5</p>

SECTION II (48 MARKS)

17. (a) (i) $\text{Vol} = 135 \times 0.15 = 20.25 \text{ m}^3$
 (ii) $\text{mass} = 2500 \times 20.25$
 $= 50625 \text{ kg} (50630)$
 $= \text{mass of cement} = \frac{50625 \times 1}{9}$
 $= 5625 \text{ kg} (5625.56)$

(b) Bags of cement = $\frac{5625}{50}$
 112.5
 113

(c) No. of lorries of sand. $\frac{50625 \times 4}{7000 \times 9}$
 $= 3.214$
 $\approx 4 \text{ lorries.}$

B1 for evaluation
 B1 (✓)
 M1
 A1
 M1
 A1 (✓)
 M1
 A1 (✓)
 8

18.

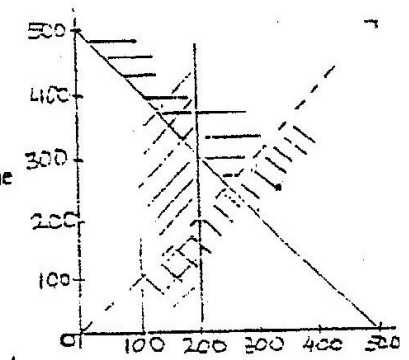
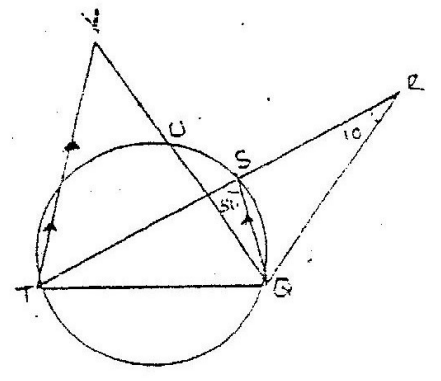
x	30	60	90	120	150	180	210	240	270	300	330	360
cos x	0.87		0	-0.5		-1.0		-0.5	0	0.5	0.87	1.0
2cos 1/2 x		1.73	1.41	1.0		0	0.52		1.41	1.73	1.93	

cos x ✓ row
 2cos 1/2 x row ✓

graph of cos x ✓
 Graph of 2 cos 1/2 x ✓
 for any error in fitting
 table the graph drawn should have
 < that 2 points out) B1 ✓
 period = 720°
 Amplitude = 2
 Enlargement of 2 about centre (0,0)

B1 Allow 1d.p. Apply PA once
 B1 allow B1 for any 12 ✓
 B1 (✓) all points must be correctly
 B1 (✓) plotted using given scale
 Apply Ow-1 if scale not
 used.
 B1
 B1
 B1
 8

*At least two
 of pts on the
 240° etc*

19.	$x+y \leq 500$ $y > x$ $x \geq 200$ (b) $x+y \leq 500$ drawn and shaded $y > x$ (c) (i) No. enrolled in technical=249 No =251 (ii) max. profit $249 \times 2500 + 251 \times 1000 = 873,500$	B1 B1 B1 L1(✓) L1(✓) B1 B1	 <p>broken line</p> <p>broken line</p> <p>Allow ✓s when inequality symbols are wrongly applied</p>
20.	(a) $\angle QTS = 40^\circ$ $\angle S$ in alt. segment (b) $\angle QRS = 10^\circ$ B1 Reasons: $\angle SQT = 90^\circ$ on semi-circle $\Rightarrow \angle TSQ = 50^\circ$ $\therefore \angle QRS = 50 - 40$ ext \angle of Δ (c) $\angle QVT = 35^\circ$ Reasons: $\angle QVT = \angle SQV$ alt \angle s (d) $\angle UTV = 15^\circ$ Reasons: $\angle QUT = \angle UTV + \angle QVT$ ext \angle of Δ $\therefore \angle UTV = 50 - 35^\circ$	B1 B1 B1 B1 B1 B1 B1 B1	
21.	(a) $V = k_1 r^2 + k_2 r^3$ $k_1 + k_2 = 54.6$ $4k_1 + 8k_2 = 226.8$ $4k_1 + 4k_2 = 218.4$ $4k_1 + 8k_2 = 226.8$ $\underline{-4k_1 + 4k_2 = -8.4}$	B1 M1 M1	Must use different constants (or implied in the equation)

continuation		
21. $\Rightarrow K_2 = 2.1$ and $k_1 = 52.5$		
$\therefore V = 52.5r^2 + 2.1r^3$	AI	
(b) $V = 52.5 \times 4^2 + 2.1 \times 4^3$	MI	
$= 52.5 \times 16 + 2.1 \times 64$		
$= 840 + 134.4$		
$= 974.4$	AI	(✓) if error is formed in determining the constants)
(c) $52.5r^2 = 2.1r^3$		
$(2.1r - 52.5)r^2 = 0$	MI	
$\Rightarrow r = 25$	AI	(✓) condone division of both sides by r^2
	8	

class	14.5-18.5	18.5-22.5	22.5-26.5	26.5-30.5	30.5-34.5	34.5-38.5	38.5-42.5
frequency	2	3	10	14	13	6	2
c. freq	2	5	15	29	42	48	50

Cumulative frequencies	BI	
(a) Linear scale used	SI	Must accommodate all data(allow reading of varied scale.
plotting of against upper class limit	PI	✓
Complete of cf curve drawn	CI	Allow curves from cf against mid-points lower class limits upper class limits boundaries.
(b) (i) median = 29.5	BI	(✓) accept readings at cf= 25.0 Or 25½ within 1 small square
(ii) Reading at mass 25.28 = 11 and 20.	BI	(✓) Allow the two Vs above for reading from cf curves.
Probability = $\frac{20-11}{50} = 0.8$	AI	
	8	

3. (a) Bearing of 060° ✓ drawn	B1	
bearing of 210° ✓ drawn	B1	
Distance on scale drawing representing 1500 km representing 1800 km	B1) B1)	<p>either actual distance/scale is stated or implied.</p>
b(i) Actual distance		
$(16 \pm 0.1) \times 200$ or equivalent	M1	S or T must be clearly located
= 3200 km	A1	
(ii) Bearing of T from S		
= $224^\circ \pm 1^\circ$	B1	(✓)
(iii) Bearing of S from T		Apply ✓ if S or T is correctly located.
= $044^\circ \pm 1^\circ$	B1	(✓)

24. (a) $a+b, a+8d, a+24d$

B1

All the 3 terms written. Allow the terms in the form $a+(n-1)d$

(b) $\frac{a+8d}{a+2d} = \frac{a+24d}{a+8d}$

M1

$$a^2 + 16ad + 64d^2 = a^2 + 26ad + 48d^2$$

$$16d^2 = 10ad$$

$$d(16d - 10a) = 0$$

$$\Rightarrow d = \frac{5a}{8}$$

M1

condone $16d = 10a$

$$2(a+5d) + (a+6d) = 78$$

M1

$$3a + 16d = 78$$

$$3a + 16 \times \frac{5a}{8} = 78$$

M1

for the formation of equ in one variable.

$$13a = 78$$

$$\Rightarrow a = 6$$

A1

$$d = \frac{5}{8} \times 6 = 3.75$$

(ii) $S_9 = \frac{9}{2} \{ 2 \times 6 + (9-1) \frac{15}{4} \}$

M1

$$= \frac{9}{2} \times 42$$

$$= 189.$$

A1

✓ Only from an error numerical either a list.

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