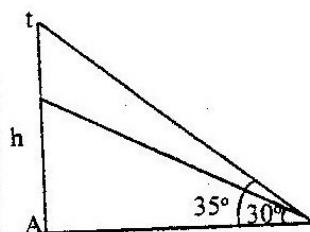


K.C.S.E 1998 MATHEMATICS PAPER 121/1 MARKING SCHEME

SOLUTION	MARKS	ALTERNATIVE METHOD
1. $\frac{100\sqrt{0.0064}}{100}$ $\frac{1000(0.08)}{10} \checkmark$ 1000×0.008 $= 8 \checkmark$	M1 A1 2	
2. $(a+b)(a-b) \checkmark$ $(2557 + 2547)(2557 - 2547) \checkmark$ 5104×10 $51040 \checkmark$	B1 M1 A1	
3. $6a + 4b = 72 \dots (i)$ $2a + 3b = 3.4 \text{ (ii)}$ $6a + 4b = 7.2$ $6a + 9b = 10.2$ $5b = -3 \checkmark$ $b = \frac{3}{5} \therefore 6a + \frac{4 \times 3}{5} = 7.2$ $6a = 4.8$ $a = 0.8$ One art book = 0.8 kg one Biology book = 0.6 kg \checkmark	M1 M1 A1 3	Forming inequalities Eliminating one variable Both answers correct
4. (a) $\angle CDF = 110^\circ - 60^\circ = 50^\circ$ (b) $\angle ABD = \angle BDE = 25^\circ \checkmark$ Both reasoning given and \checkmark Both reasoning given wrong - ow-1 One reason given (right or wrong) ow-1	A1 B1 IF	Sum of two interior opposite angles add up to exterior angle. <u>ALT. METHOD</u> $(180 - (60 + (180 - 110)) = (180 - 130)$ (A0)

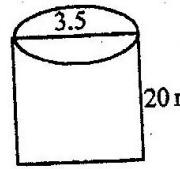
SOLUTION	MARKS	ALTERNATIVE METHOD
5. $\text{Commission} = \frac{2.4 \times 100,000}{100} + \frac{3.9 \times 180,000}{100}$ 2400 + 70.20 Sh. 5100 = Sh. 9420	M1	
6.  $\tan 35^\circ = \frac{(h+t)}{15}$ $h+t = 15 \tan 35^\circ$ 15×0.7002075 10.5031113 10.503 $\tan 30^\circ = \frac{h}{15}$ $h = 15 \tan 30^\circ$ $h = 15 \times 0.5773502$ $= 8.660254$ $h = 8.611$ (c) $10.503 - 8.661 = 1.842\text{m}$	B1 B1 B1 3	(Accept 8.66, 8.662) if log used (accept 1.84 1)
7. $\begin{pmatrix} x & 0 \\ 5 & y \end{pmatrix} \begin{pmatrix} 0 & 0 \\ 5 & y \end{pmatrix}$ $\begin{bmatrix} x^2 & 0 \\ 5x + 5y & y^2 \end{bmatrix}$ $x^2 = 0 \quad 0 = 0 \quad 5x + 5y = 0$ $5x + 5y = 0 \quad y^2 = 0 \quad 1 \text{ if } x = 1, y = 1$ if $x = -1, y = 1$ if $x = -1, y = -1$ then $x = 1, y = -1$ $x = -1, y = 1$	B1 B1 M1 A1 4	
8. $\log y = \log (10x)^n$ $= \log y = \log 10 + n \log x$ $n \log x = \log y - \log 10$ $n = \frac{\log y - \log 10}{\log x}$	M1 M1 A1	

	SOLUTION	MARKS	ALTERNATIVE METHOD
9.	$T = a + b\sqrt{S}$ or $T = b + a\sqrt{S}$ ✓ $a + b\sqrt{16} = 24$ $a + b\sqrt{36} = 32$ ✓ $a + 4b = 24$ $a + 2x - 10 = 10$ $a + 6b = 32$ ✓ $a - 20 = 10$ $-2b = -8$ $b = 4$ $a = 30$ ✓	B1 B1 M1 A1	For substitution & elimination Both answers correct
10.	$S_{14} = \frac{15}{2}(2a + (n-1)d)$ $= \frac{15}{2}(2 \times 30 + (14 \times -10))$ ✓ $\frac{15}{2}(60 - 140)$ $- 600$ ✓	M1	(a) $a, a+d, a+3d, a+d$ $a+2r-10=10$ $a+2d=10$ } $a=30$ $a+4d=-10$ } ml $-2d=20$ $d=-10$ 1st term = 30 $d = -10$
11.	Volume = $\pi r^2 h = \pi 15 \times 15 \times 1.2$ ✓ 270π ✓ (b) $\frac{1}{3}\pi \times r \times 9 = 270\pi$ ✓ $\frac{1}{3}\pi \times r^2 = 270$ $r^2 = \frac{270 \times 3}{9} = 90$ $r = \sqrt{90} = 9.49$ ✓	M1 A1 M1 A1	
12.	cum.freq 3 11 30 44 50 ✓ $M = \frac{L_1 + (n/2 - cfa)i}{f_m}$ $8 + \frac{(25 - 11) \times 4}{19} = 10.947$ ✓	B1 A1 3	$mdn = L + \frac{(n-1 - fc)}{fn} i$ $7.5 + \frac{(255 - 11) \times 4}{19}$ = 10.553 A1

SOLUTION	MARKS	ALTERNATIVE METHOD
<p>13. $1600(1 + \frac{r}{100})^2 = 2,5000 \quad \checkmark$</p> $(1 + \frac{r}{100})^2 = \frac{25000}{16000}$ $1 + \frac{r}{100} = \sqrt{\frac{25000}{16000}} = 1.25 \quad \checkmark$ $\frac{r}{100} = 0.25 \quad \checkmark$ $r = 25\% \quad \checkmark$	m1 m1 m1 m1	$\frac{25}{16} = 1 + \frac{2R}{100} + \frac{R^2}{10,000} \quad m1$ $16r^2 + 13200r + 90,000 = 0$ $r^2 + 200r + 5625 = 0 \quad m1$ $r = 200 + 250 \quad m$ $r = \frac{50}{2} = 25\% \quad m$
<p>14. $\cos(30\theta + 120^\circ) - \frac{1.732}{2} = 0.8660$</p> $30 + 120^\circ = 390^\circ \quad 30 + 120 = 330 \quad \checkmark$ $3\theta = 270 \quad 3\theta = 210 \quad \checkmark$ $\theta = 90 \quad \checkmark \quad \theta = 70^\circ \quad \checkmark$	B1 B1 B1 A1	Both answers correct
<p>15. $C = 2 \times 2.8 \times \frac{22}{7} = 17.6 \text{ cm}$</p> $\frac{C}{\pi} = \frac{17.6}{\frac{22}{7}} = 5.6 \quad \checkmark$ $3.142 \times 2.8 \times 2 = 17.595$ $3.142 \times 5.5 = 17.281 \quad \checkmark$ $3.142 \times 5.7 = 19.909$ <p>Limits: $17.28 + 17.91 \quad \checkmark$</p>	M1 M1 A1	working limit Lower limit Upper limit 17.27 - 17.91 logs used
<p>16.</p> <p>Distance covered by Bus A at 10 a.m. $= 90 \times 2 = 180 \text{ km}$</p> <p>Bus B Time between 2 stops $72 = 1.2 \text{ hrs (1hr 12 min)}$</p> <p>Bus B leaves L at 9.17 a.m.</p> <p>Distance between 9.17 - 10 a.m. = $60 \times \frac{43}{60} = 43 \text{ km}$</p> <p>At 10 a.m. Bus B has covered $(72 + 43) = 115 \text{ km}$</p> <p>Distance between Bus A & B at 10 a.m. $360 - (180 + 115) = 65 \text{ km}$</p>	B1 B1 B1	

	SOLUTION	MARKS	ALTERNATIVE METHOD
17.	<p>(a) $3.5 \times 50 = 1.75$ $\frac{100}{}$</p> <p>$4.75 \times 30 = 1.425 \checkmark$</p> <p>Total = 3.175 kg. \checkmark</p> <p>$3.175 \times 100 = 3.9688 \checkmark$</p> <p>3.969 \checkmark</p> <p>No of fat Kg = $x \times 100 = 4$ $\frac{50}{}$</p> <p>$x = 2$ kg fat</p> <p>Kg of A $\frac{3.5}{100} y + 4.75 \frac{(50-y)}{100} = 2$</p> <p>(50-y) Kg of B: $3y + 237.5 - 4.75y = 200$ $1.25 = 37.5$</p> <p>$y = \frac{37.5}{1.25}$</p> <p>$y = 30$</p> <p>A = 30 Kg</p> <p>B = 20 Kg</p> <p>B \geq 20 Kg</p>	M1 A1 M1 A1 M1 M1 M1 B1 B1 B1 8	
18.	<p>(a) Taxable pay = $\frac{2000}{20} \times \frac{115}{100} - \frac{700}{20} \checkmark$</p> <p>$1000 \times \frac{115}{100} - 35 \checkmark$</p> <p>$1150 - 35 = £1115$</p> <p>Taxable income</p> <p>$342 \times 2 + 342 \times 3 + 342 \times 4 + 39 \times 5$</p> <p>$34.2 + 51.3 + 68.4 + 22.25 = 176.15$</p> <p>Net tax = $35.23 - 600$</p> <p>Sh. 2923 (£146.15)</p>	M1 M1 M1 M1 M1 A1	M1 must mult. by 39 B1/8

SOLUTION	MARKS	ALTERNATIVE METHOD
<p>19. (B) $\begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} 4 & 2 & 6 & 4 \end{bmatrix} = \begin{bmatrix} 4 & 4 & 6 & 2 \\ 4 & 2 & 6 & 4 \end{bmatrix}$</p> <p>A'(4,4) B'(4,2) C'(6,6) D'(2,5)</p> <p>C) (i)</p> $\begin{pmatrix} 1 & -1 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} 4 & 4 & 6 & 2 \\ 4 & 2 & 6 & 4 \end{pmatrix} = \begin{pmatrix} -4 & 0 & -6 & -6 \\ 4 & 2 & 6 & 4 \end{pmatrix}$ <p>A''(-4,4), B''(0,2) C''(-6,6) D''(-6,4)</p> <p>d)</p> $\begin{bmatrix} 1 & -2 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & -1 \\ 1 & 0 \end{bmatrix} = \begin{bmatrix} 2 & -1 \\ 1 & 0 \end{bmatrix}$	B1 M1 A1 M1 A1	
<p>20. Longitudinal difference $70 - 10 = 60^\circ$</p> <p>(b) Dist betw x and y</p> $\frac{60 \times 22 \times 26371 \cos 45^\circ}{360}$ $\frac{1}{6} \times \frac{22}{7} \times 26371 \times 0.7071$ <p>4718 km</p> <p>(ii) Distance between x and y</p> $\frac{4919.45}{1.85} = 2551.05 \text{ mm}$ <p>(c) Time diff = $60 \times 4 = 240 \text{ min} = 4 \text{ hrs}$ Local time at x = 5 pm</p>	B1 M1 A1 B1 B1/8	$r = 6371 \cos 45$ <p>(Accept 4719, 4720, 4715)</p>

SOLUTION	MARKS	ALTERNATIVE METHOD
<p>21. (a) Area of the circular based $\frac{22}{7} \times 3.5 \times 3.5 = 38.5 \quad \checkmark$</p> <p>(b) Area of the curved S.A. $\frac{22}{7} \times 2 \times 3 \times 3.5 \times 20 \quad \checkmark$ $440 \text{ cm}^2 \quad \checkmark$</p> <p>(c) $\frac{4}{2} \pi r^2 = 2\pi^{22/7} \times 3.5^2 \quad \checkmark$ $44 \times 0.5 \times 3.5$ 22×3.5 $77 \text{ cm}^2 \quad \checkmark$</p> <p>(d) $38.5 + 440 + 77 \quad \checkmark$ 555.5 cm^2</p>	A1 M1 A1 M1 A1 M1 M1 A1 8	
<p>22. (i) $a + b \quad \checkmark$ $AD = AB + BD \quad \checkmark$</p> <p>$a + (\frac{-2}{3})b$ $a - \frac{2}{3}a \quad \checkmark$</p> <p>(b) $\frac{-2}{3}AD + (-4H) \quad \checkmark$ $\frac{2}{3}(a - \frac{2}{3}b + \frac{-4}{3}b)$ $\frac{2a}{3} - \frac{4b}{9} - \frac{4b}{3}$ $\frac{-2a}{3} - \frac{8b}{9} = 2(-a - \frac{4b}{3}) \quad \checkmark$</p>	B1 M1 A1 M1 A1	

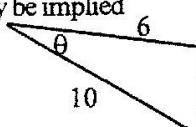
SOLUTION	MARKS	ALTERNATIVE METHOD
$\vec{PR} = \frac{1}{9}\vec{b} - \frac{8}{3}\vec{a}$ $\vec{px} = K\left(\frac{1}{9}\vec{b} - \frac{8}{3}\vec{a}\right)$ $\vec{BX} = h(-\vec{a}) = h\vec{a}$ $BX = -\frac{2}{3}\vec{a} - \frac{8}{9}\vec{b} + K\left(\frac{1}{9}\vec{b} - \frac{8}{3}\vec{a}\right)$ $= 2\vec{a} + \frac{K}{3}\vec{8a} - \frac{8}{3}\vec{b} + \frac{1}{9}k\vec{b}$ $= \left(-\frac{2}{3} - \frac{8K}{3}\right)\vec{a} + \left(\frac{8}{9} + \frac{1}{9}k\right)\vec{b}$ $-h = \frac{2}{9} + \frac{8K}{3}$ $\frac{-8}{9} + \frac{1}{9}k = 0$ $\frac{1}{9}k = \frac{8}{9}$ $K = 8$ $+h = +2 + \frac{8}{3} \times k$ $= +2 + 64 = \frac{66}{3}$	M1	
$PX = \frac{1}{9}\vec{b} - \frac{1}{3}\vec{a}$ $(\frac{8}{9}\vec{b} - \frac{64}{3}\vec{a}) : (\frac{1}{9}\vec{b} - \frac{1}{3}\vec{a}) = \frac{7}{9}\vec{b} - \frac{56}{3}\vec{a}$ $= 7(1\vec{b} - 8\vec{a}) : PR:RX = 1:7$	M1	
$h = 6$ * $h = 22$ $Px = 8(1\vec{b} - 8\vec{a}) = 8\vec{b} - 64\vec{a}$ $9 \quad 3 \quad 9 \quad 3$ $PR : RX = 1:7$	A1	
23.. $CD = 5.4$ cm Not to scale	B1 B1 B1 B1 B1 B1 B1 B1	x Const of 20o B1 (Check for const marks) x Length of AB Completed ABC Const. of 1 from A to BC produced * Length CD = $5.4 + 0.1 \times B1 (60)$ * Location of A (DA = 5.4 cm and 5) X Location of A Line through A parallel to T... accept equivalent statement

	SOLUTION	MARKS	ALTERNATIVE METHOD
23.	<p>Line parallel to BC and 4.5 away from it $BC = 5 \text{ cm}$ $AD = 6 \text{ cm}$ $\frac{3}{4} \times 6 = 4.5$</p> <p>(c) Location of A' - line parallel to BC and 4.5 cm away from BC</p>	B1	
24.	<p>(a) (i) treated with the drug $\frac{20}{36} = \frac{5}{9}$</p> <p>(ii) treated with the drug $\frac{16}{36} = \frac{4}{9}$</p> <p style="text-align: center;">1 mark</p> <p>(b) (i) treated with the drug and will die $\frac{5}{9} \times \frac{1}{10} = \frac{5}{90} = \frac{1}{18}$</p> <p style="text-align: center;">2 marks</p> <p>(ii) $\frac{4}{9} \times \frac{1}{10} = \frac{28}{90} = \frac{14}{45}$</p> <p style="text-align: center;">2 marks</p> <p>(iii) $\frac{4}{9} \times \frac{3}{10} = \frac{12}{90} = \frac{6}{45} = \frac{2}{15}$</p> <p style="text-align: center;">2 marks</p>	B1 B1 M1 A1 M1 A1 M1 A1 8	

K.C.S.E 1998 MATHEMATICS PAPER 121/2 MARKING SCHEME

SOLUTION	MARKS	ALTERNATIVE METHOD														
<p>1.</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <thead> <tr> <th>NO</th> <th>LOG</th> </tr> </thead> <tbody> <tr> <td>55.9</td> <td>1.7474</td> </tr> <tr> <td>0.2621</td> <td>1.4185</td> </tr> <tr> <td>0.01177</td> <td>2.0708 3.4893</td> </tr> <tr> <td></td> <td>$5 + \frac{2.4893}{5} = \frac{1.4979}{2.2495}$</td> </tr> <tr> <td>$1.776 \times 10^2$</td> <td></td> </tr> <tr> <td></td> <td>$= 177.6$</td> </tr> </tbody> </table>	NO	LOG	55.9	1.7474	0.2621	1.4185	0.01177	2.0708 3.4893		$5 + \frac{2.4893}{5} = \frac{1.4979}{2.2495}$	1.776×10^2			$= 177.6$		
NO	LOG															
55.9	1.7474															
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	$5 + \frac{2.4893}{5} = \frac{1.4979}{2.2495}$															
1.776×10^2																
	$= 177.6$															
	m1	All three logs ✓														
	m1	✓ attempt to divide by 5														
	A1															
	4															
<p>2. $\frac{3(x-1)-(2x+1)}{3x} = \frac{3x-3-2x-1}{3x}$</p> $= \frac{x-4}{3x}$ $\frac{x-4}{3x} = \frac{2}{3}$ $3x - 12 = 6x$ $x = 4$	B1															
	M1	Equating & removal of den														
	A1															
	3															
<p>3. $\frac{\sqrt{14} + \sqrt{2} \cdot 3 - \sqrt{14} - 2\sqrt{3}}{(14)^2 - (2 \cdot 3)^2} = \frac{4\sqrt{3}}{2}$</p> $= 2\sqrt{3}$	M1 <u>A1</u> 2	Single term with denominates expanded														
<p>4. a) $AC = \sqrt{\frac{4^2 + (4\sqrt{3})^2}{3}} = \sqrt{\frac{16 + 16}{3}} = \sqrt{\frac{64}{3}}$</p> $= \frac{8}{\sqrt{3}} \text{ or } 4.618$	M1															
	A1															
<p>b) $BC = \frac{4.618}{\tan 30} = \frac{4.618}{0.5774}$</p> $= 8$	M1	$\frac{8}{\sqrt{3}}$ if A is lost														
	A1	$\frac{8}{\sqrt{3}}$														
<p>5. 1995 value = $50,000 \times 1.2$ ✓</p> $= 60,000$ <p>1997 value = $60000 \times (1.1)^2$ ✓</p> $= 7260$	A1 M1 A1	(7,996, 7,997, 7,998, 7,999)														

SOLUTION	MARKS	ALTERNATIVE METHOD
6. Sh to £ = $\frac{500\ 000}{102} = 4902 \checkmark$ £ to \$ = $\frac{500\ 000}{102} \times 1.7 = 8.333 \checkmark$ \$ to Sh. = $\frac{500\ 000}{102} \times 1.7 \times 60.6 \checkmark$ $= 505,000 \checkmark$	M1 M1 M1 A1 4	allow Sh. 505,100
7. Trade B.P. = $\frac{84}{120} \times 100 \checkmark$ = 70 \checkmark	M1 A1	
b) Cost of manufacturers $= 70 \times \frac{100}{140} = 50 \checkmark$	B1	
8. a) ✓ Const of 1 bisector of AB b) ✓ Const of 1 bisector of Ac or BC or $\angle OAB = 12^\circ \pm 1^\circ$ or $\angle OBA = 12^\circ \pm 1^\circ$ Drawn ✓ position of P on XY of AB	B1/3 B1 B1 3	Pts P and O must be on opp. sides
9. $3u = w + u + y \checkmark$ $2u = w + v \checkmark$	M1 A1 2	* if its $3u + u = v + w$ without evidence M1A1 OW - 1 vector egn. or equivalent
10. $3p^2 + \frac{2}{3}P = 1$ $p^2 + 2p - 3 = 0$ $(p-1)(p+3) = 0$ $\rightarrow p = 1 \text{ or } p = -3$ $\therefore 3^{1/2}$ $\rightarrow y = 0$	B1 M1 A1 B1	or equivalent at lost if all values given
11. Initial volume = $\frac{4}{3}\pi r^3 = \frac{32\pi}{3}$ New vol = $\frac{32\pi}{3} \times 337.5$ = 36π	M1	
12. $\log \frac{1}{125} x^3 = \log \frac{1}{125}$ $\frac{1}{125} x^3 = \frac{1}{125}$ $x^3 = 1$ $x = 1$	M1 M1 A1	For single logs for both sides For dropping logs must convert 3 logs 5 or $\log \frac{1}{125}$ M1 for solving x, condone $x \pm 1$ for A1

SOLUTION	MARKS	ALTERNATIVE METHOD
<p>13. $1 + 6x 15^2 + 15x^2 + 20x^3 + 6x^4 + x^5 \checkmark$ $1 + 6(0.03) + 15(0.03)^2 + 20(0.03)^3 \checkmark$ $= 1 + 0.18 + 0.135 + 0.0054$ $= 1.19404$ $= 1.194 \checkmark$</p>	B1 M1 A1 .3	Accept descending powers of x Allow more than 3 terms if used and if used and follow thro'
<p>14. a) $P(\text{all boys}) = \frac{5}{12} \times \frac{4}{11} \times \frac{3}{10}$ $= \frac{1}{77}$ b) (2 girls) $= \frac{5}{12} \times \frac{7}{11} \times \frac{6}{10} \times \frac{7}{12} \times \frac{5}{11} \times \frac{6}{10} \times \frac{7}{12} \times \frac{6}{11} \times \frac{5}{10}$ $= \frac{21}{44}$</p>	M1 A1 M1 A1 4	
<p>15. $\cos \theta = \frac{6}{10} = 0.6000$ $\theta = 53^\circ 8' (53.13^\circ)$</p>	B1 M1	For identification of the angle it may be implied  $\theta = 36.52^\circ$ or $126^\circ 55'$
<p>16. a) $BN^2 = 10^2 - 5^2 = 75$ $\Rightarrow BN = 8.65$ $EN^2 = 5^2 + 12^2 = 169$ $\Rightarrow EN = 13$ b) $\tan \alpha = \frac{8.66}{13} = 0.6662$ $\alpha = 33^\circ 40' (33.67^\circ)$</p>	B1 B1 ml A1	
<p>17. a) Vol = $\frac{22}{7} \times 3.5 \times 2.8 = 107.8$ capacity = $\frac{22}{7} \times 3.5 \times 3.5 \times 2.8 \times 100 = 107800$</p> <p>b) Water used per day $= 6x 15 + 80 + 60 = 230$ No of days = $\frac{107800}{230} = 468.7$ Complete days = 468</p> <p>Water saved in 90 days $= 2x 15 \times 90 + 20 \times 60 \times 90$ $= 2700 + 1080 = 3780$ litres No of extra days = $\frac{3780}{230} = 16.43$ Total no of days = $468.5 + 16.43$ $= 485.13$</p>	ml ml A1 A1	Conversion to litres <p>(✓) All M but AO</p> <p>ALT.METHOD</p> <p>c) Water used in 90 days $90(4x 15 \times 80 \times 60 \times 80)$ $= 90 \times 100 = 16920$ Water rem = $107800 - 16920 = 90880$ days rem = $\frac{90880}{230} = 395.13$</p>

SOLUTION	MARKS	ALTERNATIVE METHOD																																																								
	B2	Both columns																																																								
18.																																																										
<table border="1"> <tr> <td>x</td><td>0</td><td>30</td><td>45</td><td>60</td><td>90</td><td>120</td><td>135</td><td>150</td><td>180</td><td>225</td><td>270</td><td>315</td><td>360</td></tr> <tr> <td>2sinx</td><td>0</td><td>1</td><td>1.4</td><td>1.7</td><td>2</td><td>1.7</td><td>1.4</td><td>1</td><td>0</td><td>-1.4</td><td>-2</td><td>-1.4</td><td>0</td></tr> <tr> <td>Cosx</td><td>1</td><td>0.9</td><td>0.7</td><td>0.5</td><td>0</td><td>-0.5</td><td>-0.7</td><td>-0.9</td><td>-1</td><td>-0.7</td><td>-1</td><td>0.7</td><td>1</td></tr> <tr> <td>Y</td><td>1</td><td>1.9</td><td>2.1</td><td>2.2</td><td>2</td><td>2.8</td><td>0.7</td><td>0.1</td><td>-1</td><td>-2.1</td><td>-2</td><td>-0.7</td><td>1</td></tr> </table>	x	0	30	45	60	90	120	135	150	180	225	270	315	360	2sinx	0	1	1.4	1.7	2	1.7	1.4	1	0	-1.4	-2	-1.4	0	Cosx	1	0.9	0.7	0.5	0	-0.5	-0.7	-0.9	-1	-0.7	-1	0.7	1	Y	1	1.9	2.1	2.2	2	2.8	0.7	0.1	-1	-2.1	-2	-0.7	1	S1 P1 C1 B1 B1	allow B1 for one column (✓) for ✓ simplification of two limits accept $x < 140^\circ \pm 3^\circ$ accept $x > 348^\circ + 3^\circ$
x	0	30	45	60	90	120	135	150	180	225	270	315	360																																													
2sinx	0	1	1.4	1.7	2	1.7	1.4	1	0	-1.4	-2	-1.4	0																																													
Cosx	1	0.9	0.7	0.5	0	-0.5	-0.7	-0.9	-1	-0.7	-1	0.7	1																																													
Y	1	1.9	2.1	2.2	2	2.8	0.7	0.1	-1	-2.1	-2	-0.7	1																																													
Range $0 \leq x < 140^\circ \pm 3^\circ$																																																										
$348^\circ \pm 3^\circ < x < 360$	8																																																									
19. a) $\angle RST = 104$ b) $TSU = 180 - 104 = 76^\circ$ $\angle QTS = 180 - (90 + 37) = 53^\circ$ or $\angle QRU = 180 - 48 = 132^\circ$ $\angle SUT = (48 + 53)^\circ - 76$ quadrilateral OR $360 - (132 + 76 + 127)$ $= 25^\circ$ c) Obtuse $\angle RUT = 76 \times 2$ (implied) $= 152^\circ$ d) $\angle PST = 70 - 48$ or equiv $= 42^\circ$	B1 B1 M1 A1 A1 ml A1 8	for ✓ values of all is < necessary for application of properties of triangle or quadrilateral for ✓ use in Δ of quad or equivalent (may be implied) May be implied																																																								
20 a) $x^2 - 2x - 3 = 0 \Leftrightarrow (x - 3)(x + 1) = 0$ b) $\int (x^2 + 2x - 3) dx = \frac{x^3}{3} - x^2 - x + C$ c) $\left x^3 - x^2 - 3x \right _{-2}^3 = (\frac{27}{3} - 9 - 9) - (\frac{8}{3} - 4 - 6)$ $= \frac{12}{3}$ $\int x^3 - x^2 + 3x \Big _0^4 = (\frac{64}{3} - 16 - 12) - \frac{27}{3} - 9 - 9$ $= \frac{21}{3}$ sum of areas $= \frac{12}{3} + \frac{21}{3}$ ✓ $= \frac{12}{3} + \frac{21}{3}$	M1 A1 ml ml M1	at least two in the integral at least two terms in the integral allow for substitution in absolute value of $-\frac{12}{3}$																																																								

SOLUTION	MARKS	ALTERNATIVE METHOD														
21. <table border="1"> <tr> <td>Log V</td><td>0.48</td><td>0.60</td><td>0.70</td><td>0.78</td><td>0.85</td><td>0.90</td></tr> <tr> <td>Log R</td><td>1.43</td><td>1.69</td><td>1.88</td><td>2.03</td><td>2.17</td><td>2.28</td></tr> </table>	Log V	0.48	0.60	0.70	0.78	0.85	0.90	Log R	1.43	1.69	1.88	2.03	2.17	2.28		
Log V	0.48	0.60	0.70	0.78	0.85	0.90										
Log R	1.43	1.69	1.88	2.03	2.17	2.28										
b) points if plotted Line of best fit drawn c) (I) gradient = 2 (ii) intercept = 0.48 ± 0.02 k = 3.02 $\Rightarrow R = 3.02$	P1 L1 B1 B1 B1 B1 B1	✓ Give one if he uses "his" scale At least 4 pts, 2 of which are ✓ pts used must be on the line ✓ ✓ ✓ ✓ allow rounding off														
22. a 600 km and 500 km seen or used ✓ scale used ✓ bearing and distance of P ✓ bearing and distance of Q b) $PQ = 10.6 \pm 0.1$ = $1060 \pm 10 \text{ km}$	B1 S1 B1 B1 B1 B1 his B1 B1 8	Apply MR if 1 hr is used ✓ measurement and conversion of ✓ Apply ✓ if one plane is ✓ by														
23. a) $PS = \sqrt{34^2 - 16^2} = \sqrt{900} \checkmark$ = 30 ✓ b) $\cos \text{POS} = \frac{17^2 + 17^2 - 30^2}{2 \times 17 \times 17} = \frac{322}{578} = 0.5572$ $\therefore \text{Pos} = 123^\circ 50' (123.86)$ c) Area of sector = $\frac{123.8}{360} \times 3.142 \times 17 \times 17 \checkmark$ Area of A = $\frac{1}{2} \times 17 \times 17 \sin 123^\circ 50'$ = $\frac{1}{2} \times 17 \times 17 \times 0.8307 \checkmark = 120$ Area of segment = $312.3 - 120 \checkmark$ = 192.3	M1 M1 A1 M1 M1 A1	$\tan \frac{1}{2} \theta = 15$ $\frac{1}{2} \theta = 61^\circ 55' = 125^\circ 50' \text{ at}$ $\frac{1}{2} = \frac{1}{2} \times 15 \times 8 = 60 \text{ M1}$ $\frac{1}{2} \text{ segment} = 156.2 - 60 \text{ M1}$ 96.2 Segment = $96.2 \times 2 = 192.4 \text{ A1}$														
24. (a) $x + y \leq 400$, $x, y; x \leq 300, y \geq 80$ (if A and B are used thro out) b) All 4 inequalities ✓ by drawn and shaded c) (i) $x = 300$ and $y = 100$ (ii) Max profit = $200 \times 300 + 400 \times 100$ = 220,000	B3	for all inequalities (allow B2 for 3✓ and B1 for 2 apply ✓ if linear equations) 														