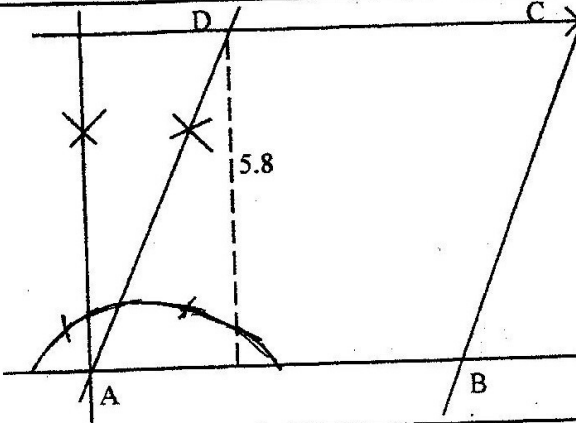


K.C.S.E 2001 MATHEMATICS PAPER 121/1 MARKING SCHEME

SOLUTION	MARKS	ALTERNATIVE METHOD												
1. Reciprocal of 0.342 = 2.924 $\sqrt{0.0625} = 0.25 \times 2.924$ $\frac{0.342}{0.342}$ = 0.731	B1 M1 A1 3 marks													
2. BO - OD = $\sqrt{15^2 - 12^2} = \sqrt{81} = 9$ Area = $1 \times 9 \times 12 \times 2 + 1 \times 9 \times 18 \times 2$ = 108 + 162 = 270cm ²	M1 M1 A1 3 marks													
3. <table style="display: inline-table; border-collapse: collapse;"> <tr> <td style="border-right: 1px solid black; padding: 2px;">No.</td> <td style="padding: 2px;">Log.</td> </tr> <tr> <td style="border-right: 1px solid black; padding: 2px;">3.256</td> <td style="padding: 2px;">0.5127</td> </tr> <tr> <td style="border-right: 1px solid black; padding: 2px;">0.0536</td> <td style="padding: 2px;">2.7292</td> </tr> <tr> <td style="border-right: 1px solid black; padding: 2px;"></td> <td style="padding: 2px;"><u>1.2419 : 3</u></td> </tr> <tr> <td style="border-right: 1px solid black; padding: 2px;"></td> <td style="padding: 2px;">$(\bar{3} + 2.2419) \div 3$</td> </tr> <tr> <td style="border-right: 1px solid black; padding: 2px;">0.5589</td> <td style="padding: 2px;">1.7473</td> </tr> </table>	No.	Log.	3.256	0.5127	0.0536	2.7292		<u>1.2419 : 3</u>		$(\bar{3} + 2.2419) \div 3$	0.5589	1.7473	M1 M1 M1 A1 4 marks	
No.	Log.													
3.256	0.5127													
0.0536	2.7292													
	<u>1.2419 : 3</u>													
	$(\bar{3} + 2.2419) \div 3$													
0.5589	1.7473													
4. $\frac{1}{3} \times \frac{22}{7} \times 6 \times 6 \times 9 + \frac{1}{2} \times \frac{4}{3} \times \frac{22}{7} \times 6 \times 6 \times 6$ = 339.4 + 452.6 = 792	M1 M1 A1 3 marks													
5. L1: $\frac{y-2}{x-1} = 5$ Y = 5x - 3 L2 at x = 4, y = 17 $\frac{y-17}{x-4} = \frac{-1}{5}$ $y = \frac{-1}{5}x + \frac{89}{5}$	B1 B1 M1 A1 4 marks	Y = 5x - 3 C = $\frac{89}{5}$ or 174 or 17.8 $y = -1 \times \frac{89}{5}$												
6. $\frac{(3x-y)(x-y)}{(3x-y)(3x-y)}$ = $\frac{x-y}{3x+y}$	M1 M1 A1 3 marks													
7. $x(x+4) = 32$ $x^2 + 4x - 32 = 0$ $(x-4)(x+8) = 0$ $x = 4$ or $x = -8$ length of room is $4 + 4 = 8m$	M1 M1 M1 A1													

SOLUTION	MARKS	ALTERNATIVE METHOD
<p>8. </p>	<p>B1 B1 B1 B1 4 marks</p>	
<p>9. $\frac{5}{100} \times 540 = 27$ $\frac{80}{100} \times 180 = 144$ $P(\text{sick}) = \frac{171}{720} = \frac{19}{80} = 0.2375$</p>	<p>M1 M1 A1 3 marks</p>	<p>$\frac{540}{720}$ or $\frac{3}{4}$ $\frac{3}{4} \times 0.05 + 1 \times 0.8$ $= 0.2375$</p>
<p>10. $S^2 = W^2(a^2 - x^2)$ $\frac{S}{W} = \sqrt{a^2 - x^2}$ $W^2 x^2 = w^2 a^2 - S^2$ $\frac{S^2}{W^2} = a^2 - x^2$ $x^2 = \frac{w^2 a^2 - S^2}{W^2}$ $x^2 = \frac{a^2 - S^2}{W^2}$ $x = \sqrt{\frac{w^2 a^2 - S^2}{W^2}}$ $x = \sqrt{\frac{a^2 - S^2}{W^2}}$</p>	<p>M1 M1 A1 3 marks</p>	<p>+ $\sqrt{\frac{W^2 a^2 - S^2}{W^2}}$ OR + $\sqrt{\frac{W^2 a^2 - S^2}{W^2}}$ $\sqrt{\frac{W a - S}{W^2} \frac{W a + S}{W^2}}$</p>
<p>11. Distance = $\frac{5}{2} \{(2.6 + 2(2.1 + 5.3 + 5.1 + 6.8 + 6.7 + 4.7))\}$ $= \frac{5}{2} (2.6 + 61.4)$ $= 160 \text{ m}$</p>	<p>M1 M1 A1 3 marks</p>	<p>$\frac{5}{2} (64)$</p>
<p>12. $\cos 2x = \sin(90^\circ - 2x)$ $\sin(x + 30^\circ) = \sin(90^\circ - 2x)$ $x + 30^\circ = 90^\circ - 2x$ $3x = 60^\circ$ $x = 20^\circ$ $\cos 3x = \cos^2 60^\circ$ $= (\frac{1}{2})^2$ $= \frac{1}{4}$ or 0.25</p>	<p>M1 A1 B1 3 marks</p>	

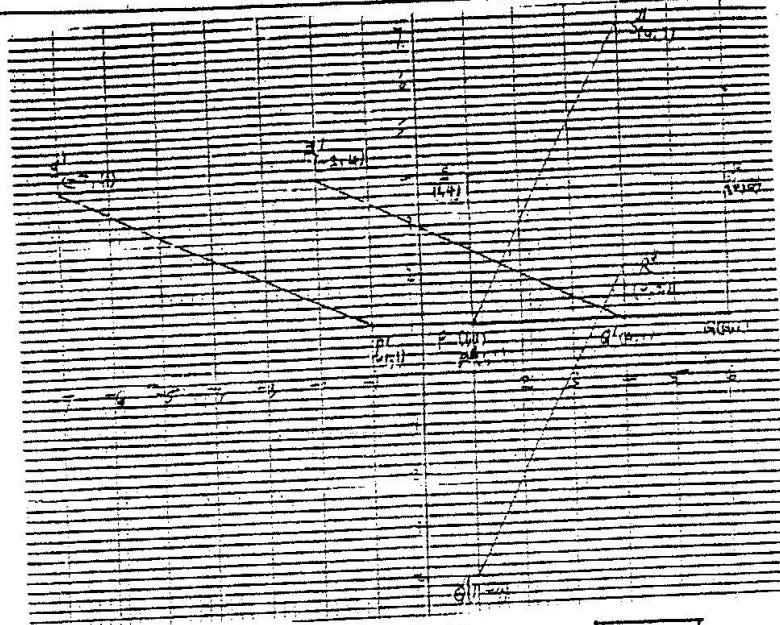
SOLUTION	MARKS	ALTERNATIVE METHOD
13. $\begin{pmatrix} 2 & 3 \\ 1 & 2 \end{pmatrix} \begin{pmatrix} 2 & -3 \\ -1 & 2 \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$ $\begin{pmatrix} x \\ y \end{pmatrix} \begin{pmatrix} 2 & 3 \\ 1 & 2 \end{pmatrix} \begin{pmatrix} 5 \\ -3 \end{pmatrix}$ $\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 1 \\ -1 \end{pmatrix}$ $x = 1 \quad y = -1$	B1 M1 M1 A1 4 marks	
14. $2x + \frac{1}{2}x + 40^\circ + 110^\circ + 130^\circ + 160^\circ - 720^\circ$ $\frac{7x}{2} = 280^\circ$ $x = \frac{280 \times 2}{7} = 80^\circ$ Smallest angle $\frac{1}{2}x = 40^\circ$		
15. Let x be speed of zebra $3.5x = 1.5(x + 20) + 340$ $3.5x = 1.5x + 30 + 340$ $2x = 370$ $x = 185\text{km/h}$ Buffalo's speed is $185 + 20 = 205\text{km/h}$	M1 M1, A1 3 marks	$3.5(x - 20) = 1.5x + 240$ $2x = 410$ $x = 205$ $\frac{340 + x}{3} + 20 = \frac{2x}{3}$ $3 \frac{1}{2}$ Speed + $\frac{2460 \times 2}{8 \times 3}$ $= 205$
16. $PQ = 3i - 4i - 6j + 6k - 2k$ $= i - 9j + 4k$ or $4k - 7j - i$ OR $-9j + 4k - i$ Length = $\sqrt{(-1)^2 + (-9)^2 + 4^2}$ $= \sqrt{98}$ $= 7\sqrt{2}$ $ PQ = \sqrt{1^2 + 9^2 + 4^2}$ $= 7\sqrt{2}$	B1 M1 marks	Column vector BO $PQ = -i - 3j - 3k$ $PQ = \sqrt{1^2 + 8^2 + 3^2}$

SOLUTION	MARKS	ALTERNATIVE METHOD
<p>17. a) Total earnings $\frac{40480}{20} = \text{f}2024$</p> <p>$435 \times 2 = 870$ $435 \times 3 = 1305$ $435 \times 4 = 1740$ $435 \times 5 = 2175$ $284 \times 6 = 1704$ <u>7794</u></p> <p>b) Net tax Sh 7794 - Sh 800 = Sh 6994</p> <p>c) New earnings</p> <p>$.15 \times 2024 = 3036$ $\text{f}3036 - \text{f}2024 = 1012$ excess tax = 1012×6 = Sh 6072</p> <p>% age excess = $\frac{6072}{7794} \times 100\%$ = 77.91%</p>	<p>M1</p> <p>M1 M1</p> <p>A1</p> <p>B1</p> <p>M1 M1</p> <p>A1</p> <p>8 marks</p>	<p>$\frac{1012 \times 6 \times 100\%}{7794}$</p>
<p>18.</p> $\begin{bmatrix} 1 & -2 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} P & Q & R & S \\ 1 & 1 & 4 & 4 \end{bmatrix} = \begin{bmatrix} P^1 & Q^1 & R^1 & S^1 \\ 1 & 1 & 4 & 4 \end{bmatrix}$ <p>$P^1(-1, 1) \quad Q^1(4, 1) \quad R^1(-2, 4) \quad S^1(-7, 4)$</p> <p>ii) object drawn Image $P^1 Q^1 R^1 S^1$ drawn</p> <p>(iii) $\begin{bmatrix} 1 & 1 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} P & Q & R & S \\ 1 & 4 & -2 & -7 \\ 1 & 1 & 4 & 4 \end{bmatrix} = \begin{bmatrix} P^{11} & Q^{11} & R^{11} & S^{11} \\ 1 & 1 & 4 & 4 \\ 1 & -4 & 2 & 7 \end{bmatrix}$</p> <p>$\begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix}$ Negative Quarter turn about the origin</p>	<p>A1</p> <p>B1</p> <p>B1</p>	

SOLUTION

MARKS

ALTERNATIVE METHOD



18 (b) Single matrix in the inverse of $\begin{bmatrix} 1 & 2 & -1 \\ 1 & 1 & 0 \end{bmatrix}$

$$\begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix} \begin{bmatrix} 1 & -2 \\ 0 & 1 \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ 1 & 2 \end{bmatrix} \text{ Which is } \begin{bmatrix} 2 & -1 \\ 1 & 0 \end{bmatrix}$$

19. a) i) $\underline{OQ} = \underline{P} + \underline{r}$
 ii) $\underline{OQ} = \underline{OQ} + 1/5 \underline{RQ}$
 $= \underline{r} + 1/5 \underline{P}$

b) i) $\underline{OS} = m \underline{OQ} = m(\underline{p} + \underline{r})$
 $= m\underline{p} + m\underline{r}$

(ii) $\underline{OS} = \underline{OQ} + n \underline{TP}$
 $= (\underline{r} + 1/5 \underline{P}) + n(\underline{r} - 1/5 \underline{P} + \underline{P})$
 $= \underline{r}(1-n) + \underline{P}(1/5 + 4/5n)$

(iii) $m\underline{p} + m\underline{r} = \underline{r}(1-n) + \underline{P}(1/5 + 4/5n)$
 $m = 1/5 + 4/5n \dots\dots\dots(1)$
 $m = 1-n \dots\dots\dots(2)$
 $5m = 1 + 4n = 1 + 4(1-m)$
 $9m = 5$
 $m = 5/9$

iv) $\underline{OS} = 5/9 \underline{p} + 4/9 \underline{r}$
 divides OQ in the ratio 5:4

B1
B1

B1

B1

M1

M1

A1

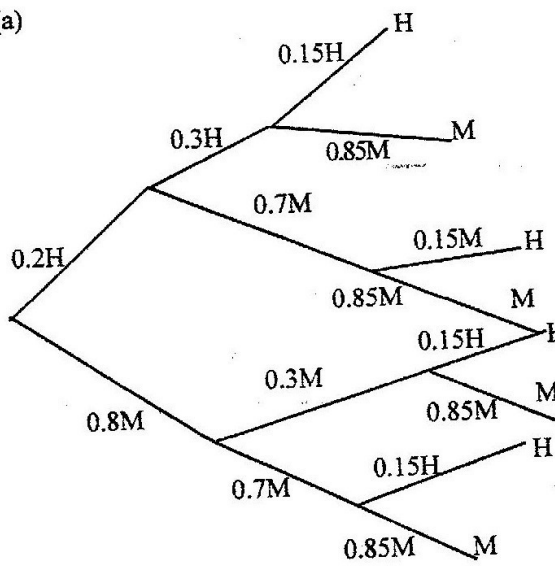
F1

8 marks

SOLUTION										MARKS	ALTERNATIVE METHOD
x	-3	-2.5	-1.5	-1	-0.5	0	0.5	1	1.5	B2	all 6
x^3			15.06					1			B1 at best
$2x^2$			12.5					2			4 entries
$y=x^3+2x^2$			-3.25					3			PA - 1 if values minded off
										S1	If Bo, Po.
										P1	If B250 tr B8 S0m B15, Uscale be linear
										C1	(CAO
										B1	$y = x + 2$
										L1	Line drawn
$x = -2.11$										B2 S1 P1 C1 B2 S0 P1 C0 B1 S0 P1 C0 B1 S1 P1 C0 B0 S0 P0 C0 B0 S0 P0 C0 B2 S1 P1 C0	

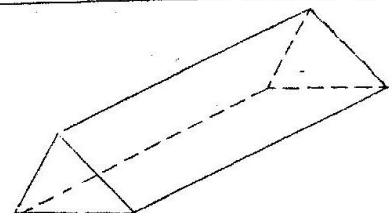
K.C.S.E 2001 MATHEMATICS PAPER 121/1 MARKING SCHEME

SOLUTION	MARKS	ALTERNATIVE METHOD
<p>20 a) i) $\angle CBD = 90^\circ - 42^\circ = 48^\circ$ Subtended by diameter</p> <p>ii) $\angle BOD = 180^\circ - 42^\circ = 138^\circ$ cyclic quadrilateral</p> <p>Reflex $BOD = 360^\circ - 130^\circ = 222^\circ$</p> <p>b) In $\triangle BAD$ $\angle BAD = \frac{1}{2} \times 138^\circ = 69^\circ$ $\angle ADB = 180^\circ - 42^\circ + \frac{1}{2} \times 138^\circ$ $= 180^\circ - 111^\circ$ $= 69^\circ$</p>	<p>B1 B1</p> <p>B1 B1</p> <p>B1</p> <p>B1 B1 B1</p> <p>8 marks</p>	<p>$\angle BPD = 138^\circ$ $\angle AOB$ $= 360^\circ - (138 + 84)$ $= 360^\circ - 222$ $= 138^\circ$</p>
<p>21. (a) $\int (2x^2 - 5) dx = \frac{2}{3} x^3 - 5x + C$</p> <p>$y = \frac{2}{3} x^3 - 5x + C$</p> <p>$3 - \frac{2}{3} \times 2^3 - 5 \times 2 + C$</p> <p>$C = \frac{72}{3} \text{ or } \frac{23}{3}$</p> <p>$y = \frac{2}{3} x^3 - 5x + 7 \frac{2}{3}$</p>	<p>M1</p> <p>M1</p> <p>A1</p> <p>3 marks</p>	

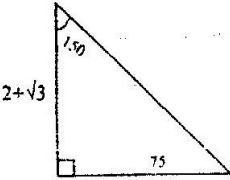
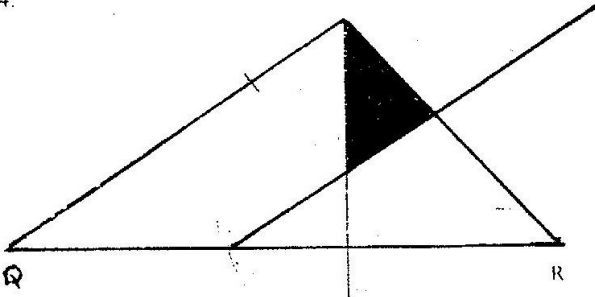
SOLUTION	MARKS	ALTERNATIVE METHOD
<p>21. (b) $\int (2t^3 + t^2 - 1) dt = \frac{2}{4}t^4 + \frac{t^3}{3} - t + C$</p> $\int (2t^3 + t^2 - 1) dt = \left[\frac{2}{4} \times 3^4 + \frac{3^3}{3} - 3 \right] - \left[\frac{2}{4} + \frac{1}{3} - 1 \right]$ $= \left(\frac{81}{2} + 9 - 3 \right) - \left(\frac{1}{2} + \frac{1}{3} - 1 \right)$ $= \frac{461}{2} \left(\frac{1}{6} \right)$ $= \frac{462}{3}$	<p>M1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>8 marks</p>	$\frac{2}{4}t^4 + \frac{1}{3}t^3 - t$ $\left[\frac{2}{4}t^4 + \frac{1}{3}t^3 - t \right]_1^3$
<p>22 (a)</p>  <p>b) (i) $0.2 \times 0.3 \times 0.15 = 0.009$ (ii) $0.2 \times 0.7 \times 0.85 = 0.119$ $0.8 \times 0.3 \times 0.85 = 0.204$ $0.8 \times 0.7 \times 0.15 = 0.084$ <u>0.407</u></p> <p>(iii) HHM $0.2 \times 0.3 \times 0.85 = 0.051$ HMH $0.2 \times 0.7 \times 0.15 = 0.021$ MHH $0.8 \times 0.3 \times 0.15 = 0.036$ HHH $0.2 \times 0.3 \times 0.15 = 0.009$ <u>0.117</u></p>	<p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>8 marks</p>	$1 - (0.407 + 0.476)$ $= 1 - 0.883$ $= 0.117$

K.C.S.E 2001 MATHEMATICS 121/2 MARKING SCHEME

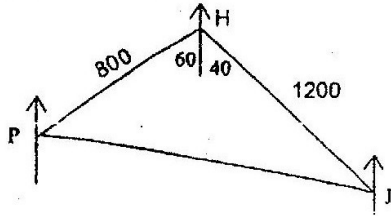
SECTION 1 (52 MARKS)

<p>1. $\frac{1}{3} \times \left(\frac{11}{4} - \frac{22}{4} \right) \times \frac{27}{7} \times \frac{4}{9}$</p> $\frac{1}{3} \times \frac{11}{4} \times \frac{27}{7} \times \frac{4}{9}$ $= -\frac{11}{7} \text{ or } -1\frac{4}{7}$	<p>M1 A1</p> <p>2 marks</p>	<p>All multiplication Simplified to lowest form</p>
<p>2. $2^{2(x-1)} \times 2^{3(x+4)} = 2^6 \times 2^x$</p> $5(x-5) + 3(x+4) = 6+x$ $5x - 25 + 3x + 12 = 6 + x$ $8x - 13 = 6 + x$ $7x = 19$ $x = \frac{19}{7}$	<p>M1 M1 A1</p> <p>3 marks</p>	<p>Mark for equating correct powers of 2 Mark for equating powers from above</p>
<p>3. Mliwa: $\frac{3}{8} \times \frac{2}{3}x = \frac{1}{4}x$</p> <p>Amina: $x - \left(\frac{1}{3} + \frac{1}{4} \right)x = \frac{5}{12}x$</p> $\frac{5}{12}x - \frac{1}{4}x = 40000$ $\frac{2}{12}x = 40000$ $x = 240000$	<p>B1 M1 A1</p> <p>3 marks</p>	<p>Or $\frac{5}{12}$</p> $40000 \times \frac{12}{2}$ <p>do not award for 60</p>
<p>4. $A = mB + n B$</p> $30 = 9m + 3n$ $16 = 14m + n \quad \times 14$ $420 = 126m + 42n$ $144 = 126m + 33.68n$ $276 = 8.32n$ $n = 33.17$ $9m = 30 - 99.51 = -69.51$ $m = -7.723$ <p>When $B = 36$, $A = -7.723 \times 36 + 33.17 \times 6$</p> $= -278.0 + 199.0$ $= -79$	<p>M1 M1 M1 A1</p> <p>4 marks</p>	<p>Mark for at least one equation</p> <p>Mark for attempt to solve equation</p> <p>Mark for substitution of pupils constants</p>
<p>5. a)</p>  <p>b) Four (4) planes of Symmetry</p>	<p>B2 B1</p> <p>2 marks</p>	<p>B1 If dotted lines omitted or fully drawn</p> <p>Accept either (lines to be dotted)</p>
<p>6. Kshs $(4320 + 3260 + 2080) = 9660$</p> $\text{Total bill} = 9660 \times \frac{115}{100}$ $= 11109 \text{ (long mult.) OR } 11110 \text{ (Table)}$	<p>M1 A1</p> <p>2 marks</p>	<p>Or equivalent</p>

<p>7. $\begin{pmatrix} 5 \\ -4 \end{pmatrix} - \begin{pmatrix} 3 \\ 2 \end{pmatrix} = \begin{pmatrix} 2 \\ -6 \end{pmatrix}$</p> <p>$OQ = \begin{pmatrix} 2 \\ 5 \end{pmatrix} + \begin{pmatrix} 2 \\ -6 \end{pmatrix} = \begin{pmatrix} 4 \\ -1 \end{pmatrix}$</p> <p>$\therefore PQ = \begin{pmatrix} 4 \\ -1 \end{pmatrix} - \begin{pmatrix} 5 \\ -4 \end{pmatrix} = \begin{pmatrix} -1 \\ 3 \end{pmatrix}$</p> <p>$PQ = \sqrt{(-1)^2 + 3^2}$</p> <p>$= \sqrt{10}$</p>	<p>BI</p> <p>M1</p> <p>AI</p> <p>3 marks</p>	<p>OR $\sqrt{(4-5)^2 + (-1+4)^2}$</p>
<p>8. $\text{Log}\left(\frac{x+24}{3^2}\right) = \text{log}(9-2x)$</p> <p>$\frac{x+24}{9} = 9-2x$</p> <p>$19x = 57$</p> <p>$x = 3$</p>	<p>M1</p> <p>M1</p> <p>AI</p> <p>3 marks</p>	
<p>9. Moving average of order 3</p> <p>$x = 331 \times 3 - 670 = 323$</p> <p>$y = \frac{323 + 343 + 350}{3} = 338\frac{2}{3}$</p>	<p>BI</p> <p>BI</p> <p>BI</p> <p>3 marks</p>	
<p>10. $(2+x)^5 = 2^5 + 2^4 \times 5x + 2^3 \times 10x^2 + 2^2 \times 10x^3 + \dots$</p> <p>$= 32 + 80x + 80x^2 + 40x^3$</p> <p>$(2.03)^5 = 32 + 80 \times 0.03 + 80 \times (0.03)^2 + 40 \times (0.03)^3$</p> <p>$= 32 + 2.4 + 0.072 + 0.00108$</p> <p>$= 34.47308$</p> <p>$\approx 34.47$ (4 significant figures)</p>		
<p>11. (a) $\frac{dy}{dx} = 15x^2 - 14x + 3$</p> <p>Grad. $= 15 \times 1^2 - 14 \times 1 + 3 = 4$</p> <p>(b) $\frac{y-3}{x-1} = 4$</p>	<p>M1</p> <p>AI</p> <p>M1</p> <p>AI</p> <p>4 marks</p>	<p>OR $y = 4x - 1$</p>
<p>12. Area of pentagons</p> <p>$= \frac{1}{2} \times 4.25 \times 4.25 \sin 72^\circ \times 5 \times 2$</p> <p>$= \frac{1}{2} \times 4.25 \times 4.25 \times 0.9511 \times 5 \times 2$</p> <p>$= 18.06 \times 0.9511 \times 5$</p> <p>$= 85.88$ OR (85.9)</p> <p>Area of rectangle faces</p> <p>$= 5 \times 12 \times 5 = 300$</p> <p>Total area</p> <p>$= 300 + 85.88$</p> <p>$= 385.88$</p>	<p>M1</p> <p>AI</p> <p>M1</p> <p>AI</p> <p>4 marks</p>	<p>Allow from area of one pentagon</p> <p>$H = 11.81 = 3.43$</p> <p>Area $= \frac{1}{2} \times 5 \times 3.43$</p> <p>$= 8.59$</p> <p>Area $= \sqrt{6.75 \times 2.5^2} \times 1.75$</p>

<p>13.</p>  $\tan 15 = \frac{1}{2+\sqrt{3}}$ $\frac{1}{2+\sqrt{3}} \times \frac{2-\sqrt{3}}{2-\sqrt{3}}$ $= 2-\sqrt{3}$	B1 M1 A1	
3 marks		
<p>14.</p> 	B1 B1 B1	Angle bisector 1 bisector (mediator) of p mark for shading region
3 marks		
<p>15.</p> $4(1 - \cos^2 \theta) + 4 \cos \theta = 5$ $4 \cos 2\theta - 4 \cos \theta + 1 = 0$ $(2 \cos \theta - 1)(2 \cos \theta + 1) = 0$ $\cos \theta = \frac{1}{2}$ $\theta = 60^\circ, 300^\circ$	M1 M1 A1	
3 marks		
<p>16.</p>	B1 B1 B1 B1	Mark for shading Mark for labeling the region
4 marks		

17.



a) i) $PJ^2 = 800^2 + 1200^2 - 2 \times 800 \times 1200 \cos 100$
 $= 640,000 + 1,440,000 + 2 \times 960,000 \times 0.1736$
 $= 2413312$ (2413000)
 $= PJ = 1553 \text{ km}$

ii) $\frac{\sin \theta}{800} = \frac{\sin 100}{1553}$ $\sin \theta = \frac{800 \times 0.9848}{1553}$
 $= 0.5075$ $\theta = 30^\circ 29'$ ($30^\circ 30'$)
 Bearing = $360 - (40 + 30^\circ 29')$
 $= 289^\circ 31'$ ($289^\circ 30'$) **OR** 289.5°

b) Time for jet = $\frac{1553}{1035} = 1.501 \text{ h}$
 \therefore Time for helicopter = $1.501 + 0.2$
 $= \text{Speed} = \frac{800}{1.701} = 470.6$

ALT.

a)
 i) From scale drawing
 Bearing dist. PH - B1
 Bearing dist. HJ - B1
 PJ measured converted B1
 (15.5 ± 0.1 **OR** 7.75 ± 0.2)

ii) $\angle HJP = 30 \pm 1^\circ$
 Bearing = $360 - (40 + 30)$
 $= 290^\circ$

8 marks

18. a (i) $225 + 1196 + 144 = 169 + P^2 + 256 + 121 + 169 + 144 + 1289 = 1794$
 $P^2 + 1713 = 1794$
 $P^2 = 81$
 $P = 9$

a (ii) **Standard deviation**
 Mean = $(915 + 14 + 12 + 13 + 9 + 16 + 11 + 13 + 12 + 17) \div 10 = 13.2$

X	15	14	12	13	9	16	11	13	12	17
X - \bar{X}	1.8	0.8	-1.2	-0.2	-4.2	2.8	-2.2	-0.2	-1.2	3.8
(X - \bar{X}) ²	3.24	0.64	1.44	0.04	17.74	7.84	4.84	0.04	1.44	14.44

$\sum (X - \bar{X})^2 = 51.6$

s.d = $\sqrt{\frac{51.6}{10}}$ **OR** $\sqrt{\frac{1794}{10} - (13.2)^2}$
 $= 2.272$ **OR** 2.28

b (i) New mean = 16.2

b (ii) New S.d = 2.272

8 marks

M1 Mark for all values added
 A1 Mark for correct value of P

M1 Or equivalent
 A1

M1 Mark for at least (X - \bar{X})
 A1
 B1
 B1

19. a) 5, 7, 9, 11

b) $S_m = \frac{50}{2} \{2 \times 5 + (50 - 1)2\} = 2700$

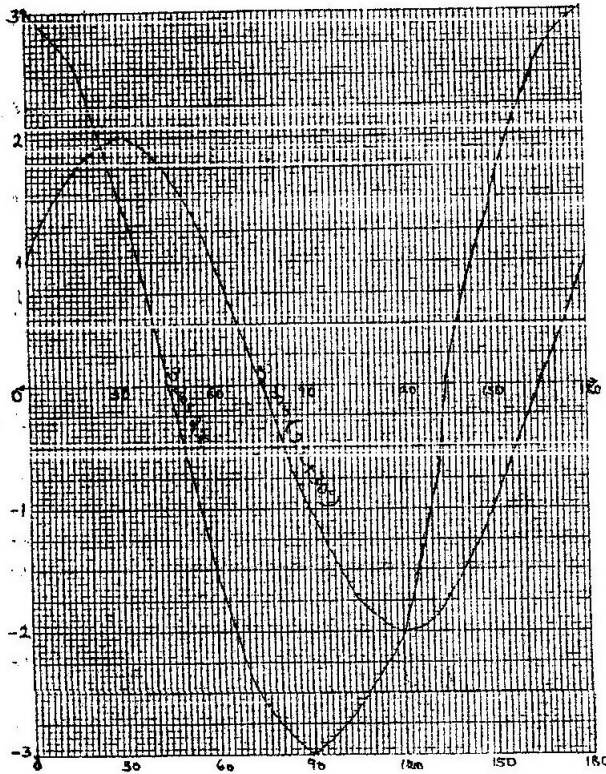
B2
 M1
 A1

OR
 $\frac{50}{2} \times 5 + 2 \times 50 \times 3$

<p>c) $S_n = \frac{n}{2} \{2 \times 5 + (n-1)2\}$ $= \frac{n}{2} (8 + 2n)$ $= 4n + n^2$</p> <p>$n^2 + 4n < 725$ $n^2 + 4n - 725 < 0$ $(n + 29)(n - 25) < 0$ $\therefore n = 24$</p>	<p>B1</p> <p>M1 A1 D1</p> <p>8 marks</p>	<p>Mark for following working</p> <p>Allow if - used for n=25</p>
<p>20. a) $RA = \frac{30}{\tan 26^\circ}$ or $= RA \ 30 \tan 64^\circ$ $= \frac{30}{0.4877}$ or 30×2.050 $= 61.51 \ (61.5)$</p> <p>$RB = \frac{30}{\tan 32^\circ}$ or $= 30 \tan 58^\circ$ $= \frac{30}{0.6249}$ or 30×1.600 $= 48.01 \ (48)$</p> <p>$AB = \sqrt{61.51^2 + 48.01^2}$ $= \sqrt{3783 + 2305} = \sqrt{6088}$ $= 78.03$</p> <p>b) $\tan \theta = \frac{48.01}{61.51}$ $= 0.7805$ $\theta = 37^\circ 58'$</p> <p>bearing $= 360 - 37^\circ 58'$ $= 322^\circ 2' \ (322.03)$</p>	<p>M1 A1</p> <p>M1 A1 M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>8 marks</p>	<p>OR $\sin \theta = \frac{48.01}{78.03}$</p>

21.

x°	15°	75°	150°	165°
$3\cos 2x^\circ$		-2.598	1.5	
$2\sin(2x + 30)$	1.732			0



B1

B1

S1 Mark for scale used

P1

Mark for all points

P1

CI Mark for all points

B1

Mark for smooth curves

B1

8 marks

Mark for 25° , 116° stated
Accept (24° - 27°)
From his graphs read within 1°
Mark for $25 \leq x \leq 116$

22.

a) $\frac{dx}{dt} = 3t^2 - 4t$

Velocity = $3 \times 2^2 - 4 \times 2$
 $= 4 \text{ m/s}$

b) (i) $3t^2 - 4t = 0 \Leftrightarrow t(3t - 4) = 0$

$\therefore t = \frac{4}{3}$

$x = \left(\frac{4}{3}\right)^3 - 2\left(\frac{4}{3}\right)^2 + 6$

$= \frac{64}{27} - \frac{32}{9} + 6 = \frac{64 - 96}{27} + 6$

$= 4\frac{22}{27} \quad (4.815)$

(ii) $\frac{d^2x}{dt^2} = 6t - 4$

$\therefore a = 6 \times \frac{4}{3} - 4$

$= 4 \text{ m/s}^2$

M1

M1

A1

M1

Mark for one term correct

M1

A1

M1

A1

8 marks

<p>23.</p> <p>a) i) Vol. cylindrical part</p> $= \frac{22}{7} \times 0.7 \times 0.7 \times 1$ $= 1.54\text{m}^3$ <p>ii) X-Section = $\frac{1}{2} \times 0.4^2 \times \sin 60^\circ \times 6$</p> $= \frac{1}{2} \times 0.4 \cdot 0.4 \cdot 0.866 \cdot 6$ $= 0.41568 (0.4157)$ <p>Vol. hexagonal part = 0.41568×4</p> $= 1.6628 (1.663)$ <p>b) Volume of pillar $(1.54 + 1.6628) - 0.25 \times 5$</p> $= 3.2028 - 1.25 = 1.9528 (1.953)$ <p>c) Mass = 1.953×2400</p> $= 4687.2\text{kg} (4687\text{kg})$	<p>MI</p> <p>AI</p> <p>MI</p> <p>MI</p> <p>AI</p> <p>MI</p> <p>MI</p> <p>MI</p> <p>AI</p> <p>AI</p>	
<p>24. a) $800x + 1600y \geq 8000 (x + 2y \geq 10)$</p> <p>$4x + 7y \leq 41$</p> <p>$x \geq 2$ and $y \geq 2$</p>	<p>8 marks</p> <p>BI</p> <p>BI</p> <p>BI</p> <p>BI</p> <p>BI</p> <p>BI</p> <p>BI</p> <p>BI</p> <p>BI</p> <p>8 marks</p>	<p>Mark for each line draw and shaded</p> <p>Mark for type A = 3 & type B = 4</p> <p>Mark for numbers of operators $3 \times 4 + 4 \times 7 = 40$</p>