

121/1 MARKING SCHEME

2011

ALTERNATIVE

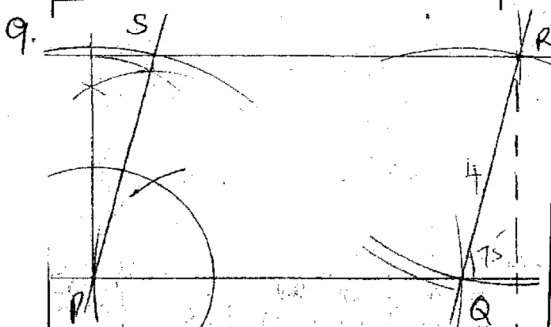
1.	$\frac{2\frac{1}{5} + (\frac{2}{3} \times \frac{15}{4}) - 4\frac{1}{6}}{1\frac{1}{4} - \frac{12}{5} \times \frac{3}{4} + 3\frac{3}{4}} = \frac{8/15}{3/5}$ $\frac{8}{15} \times \frac{5}{16} = \frac{1}{6}$	<p>M<sub>1</sub> M<sub>1</sub> A<sub>1</sub> <u>3</u></p>	<p>Numerator for some operations Denominator</p>
2.	$\sqrt{11.75^2 - 6.75^2} = 9.$ <p>Perimeter = 2(9 + 6.75) = 31.5</p>	<p>B<sub>1</sub> B<sub>1</sub> <u>2</u></p>	<p>Accompanied by some Working.</p>
3.	<p>Let d be distance covered.</p> $\frac{3d}{5} - \frac{d}{2} = \frac{d}{10}$ <p>% Change = <math>\frac{\frac{d}{10}}{\frac{d}{2}} \times 100\%</math></p> $\frac{d}{10} \times \frac{2}{d} \times 100 = 20\%$ <p>Alternative.</p>	<p>M<sub>1</sub> M<sub>1</sub> A<sub>1</sub> <u>3</u></p>	<p>difference of speeds. allow.</p> $\frac{d}{2} - \frac{3d}{5} = -\frac{d}{10}$ <p>6:5 1:1<math>\frac{2}{3}</math> 5:6 <math>\frac{1}{5} \times 100 = 20\%</math> if -20% A0. Allow 20 even without %.</p>
	$S_1 = \frac{x}{2}, \quad S_2 = \frac{x}{1\frac{2}{3}}$ $\frac{x}{2} = 100\%$ $\frac{\frac{x}{1\frac{2}{3}} \times 100}{\frac{x}{2}} = 120$ $120 - 100 = 20\%$		<p>Area</p>
4.	<p>Area of a slabs 60x42 = 2520. No. of slabs = x.</p> <p>Total area L<sup>2</sup> = 2520x 2520 = 2<sup>3</sup> × 3<sup>2</sup> × 5 × 7.</p> <p>To make the power divisible by 2 2 × 5 × 7    x = 70.</p>		<p>Area <math>\frac{70 \times 2520}{10} = 17.64 \text{ m}^2</math>.</p>

$60 = 2^2 \times 3 \times 5$ $42 = 2 \times 3 \times 7$ <p>Side of pavement LCM</p> $= 2^2 \times 3 \times 5 \times 7 = 420 \text{ cm}$ <p>least Area</p> $= 4.2 \times 4.2 \text{ m} = 17.64 \text{ m}^2$	$M_1$ $A_1$ $B_1$ <hr/> 3	
<p>5. <math>\sin(\alpha + 60^\circ) = \cos 2\alpha</math></p> $\alpha + 60 + 2\alpha = 90^\circ \rightarrow$ $3\alpha = 30$ $\alpha = 10^\circ$ <p><math>\tan(\alpha + 60^\circ) = \tan 70^\circ \rightarrow</math></p> $= 2.748 \text{ from tables}$ <p>4sf or 2.7475</p>	$M_1$ $M_1$ $A_1$ <hr/> 3	
<p>6. <math>\frac{4x - 9x^3}{3x^2 - 4x - 4} = \frac{x(2-3x)(2+3x)}{(3x+2)(x-2)}</math></p> $= \frac{x(2-3x)}{x-2}$	$M_1$ $M_1$ $A_1$ <hr/> 3	<p>Complete factorizing numerator</p> <p>Complete factorizing denominator</p> $\frac{2x - 3x^2}{x-2} \Big  \frac{(2x-3x^2)(2+3x)}{(3x+2)(x-2)}$ $= \frac{2x - 3x^2}{x-2}$
<p>7. Internal Dimensions: 40, 20 &amp; 15</p> <p>Volume unoccupied</p> $= 40 \times 20 \times 15 = 8000$ $= 4000$ <p>Height of unoccupied</p> $= \frac{4000}{40 \times 20}$ $= 5 \text{ cm.}$	$B_1$ $M_1$ $M_1$ $A_1$ <hr/> 4	<p>OR. EQUIVALENTS</p> <p>Vol. occupied <math>40 \times 20 \times h = 8000</math></p> $V = \frac{8000}{40 \times 20} = 10 \text{ cm height.}$ <p><math>M_1</math></p> $15 - 10 = 5 \text{ cm}$ <p>or</p> $H = 15.5 - (10 + 0.5) = 5 \text{ cm}$ <p><math>B_1, M_1</math></p>

8.  $2x^2y^2 - 5xy - 12$   
 $= 2x^2y^2 - 8xy + 3xy - 12$   
 $= 2xy(xy - 4) + 3(xy - 4)$   
 $= (2xy + 3)(xy - 4)$

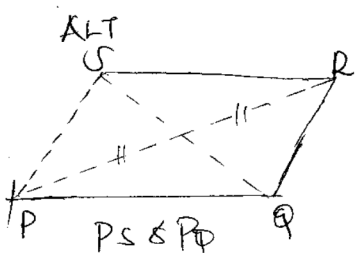
M<sub>1</sub>  
A<sub>1</sub>  
2

11. Sh.  $\frac{5880}{98} \times 100 \rightarrow$  M<sub>1</sub>  
 $= 6000$   
 Sh.  $\frac{6000}{120} \times 100 \rightarrow$  M<sub>1</sub>  
 $= \text{Sh} - 5000$  A<sub>1</sub>  
3



Construction of 75° at P.  
 Construction of adjacent sides  
 Completion of //gram  
 height = 3.9 ± 0.1 cm.  
 3.8, 3.9, 4.0.

B<sub>1</sub>  
B<sub>1</sub>  
B<sub>1</sub>  
B<sub>1</sub>  
4

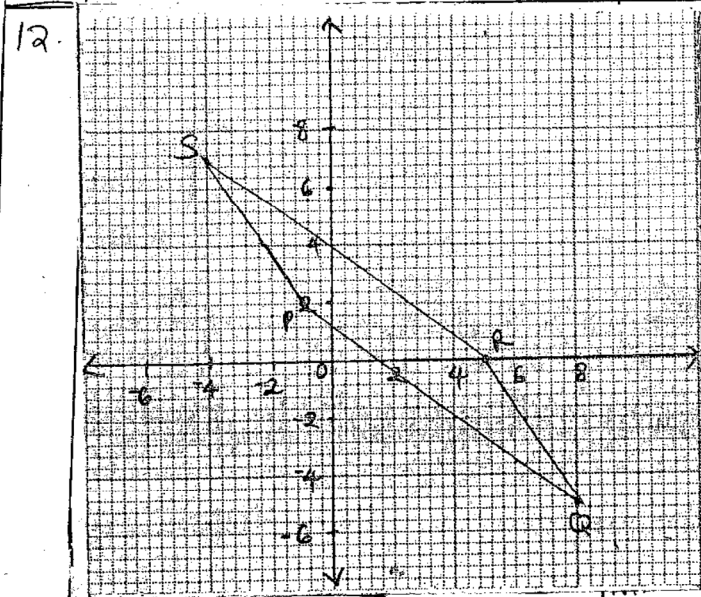


PS & PQ we need not see the ~~point~~ arcs  
 Point R arcs must be seen from a constructed //gram with arcs.  
 If the height is calculated correct give the mark.  
 $4 \sin 75^\circ = 3.864 \text{ cm.}$

B<sub>1</sub>  
B<sub>1</sub>  
B<sub>1</sub>  
4

10. Mid points:  
 42, 47, 52, 57, 62, 67, 72  
 $f_x = 42, 94, 162, 241, 350, 494$   
 $B_4, 72$   
 $\bar{x} = \frac{\sum f_x c}{\sum f_x} = \frac{1660}{30} = 55 \frac{1}{3} \text{ kg}$   
 $= 55.33 \text{ kg}$

M<sub>1</sub>  
A<sub>1</sub>  
3



12.

$QS = \sqrt{2^2 + 2^2}$   
 $= 16.97 \text{ units.}$

A<sub>1</sub>  
3

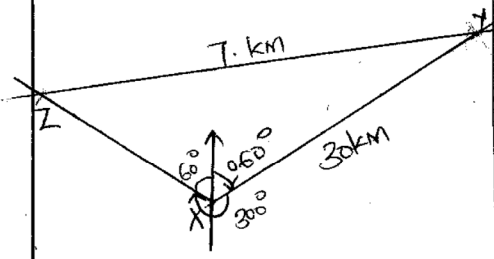
13.  $\frac{1}{6}x + \frac{1}{5}y = 14,820$   
 $\frac{1}{8}x + \frac{1}{12}y = 8675$   
 $50x + 6y = 444,600$   
 $30x + 2y = 208,200$   
 $5x + 6y = 444,600$   
 $9x + 6y = 624,600$  M<sub>1</sub>  
 $4x = 180,000$  M<sub>1</sub>  
 $x = 45,000$  A<sub>1</sub>

M<sub>1</sub>  
M<sub>1</sub>  
M<sub>1</sub>  
A<sub>1</sub>  
4

14. a)  $10,500 = 2^3 \times 3 \times 5^3 \times 7$   
 b)  $P \times 10,500 = 2^3 \times 3^3 \times 5^3 \times 7^3$   
 Smallest Value of P =  $2 \times 3^2 \times 7^2$   
 $= 882.$

M<sub>1</sub>  
A<sub>1</sub>

SECTION II

<p>15. Scale of 1:200m</p>  <p>distance <math>XZ = 30 \text{ km} = 30 \text{ km} \pm 1 \text{ km}</math></p>	<p>B<sub>1</sub> B<sub>1</sub> B<sub>1</sub> B<sub>1</sub> 4</p>	<p>17. a) (i) Surface area of solid  <math>\pi \times 6 \times 10 + \frac{1}{2} \times \pi \times 6^2</math>  <math>= 414.69</math></p> <p>(ii) height of cone  <math>= \sqrt{100 - 36} = 8</math></p> <p>Volume of solid  <math>\frac{1}{3} \times \pi \times 6^2 \times 8 + \frac{1}{2} \times \frac{1}{3} \times \pi \times 6^3</math>  <math>= 753.98 \text{ cm}^3</math></p> <p>b) Mass of solid in kg  <math>= \frac{1.3 \times 753.98}{1000}</math>          Accept 0.98 kg</p>	<p>M<sub>1</sub> M<sub>1</sub> A<sub>1</sub> B<sub>1</sub> M<sub>1</sub> M<sub>1</sub> A<sub>1</sub> A<sub>1</sub> 0</p>
<p>16. L.S.F = 8:24 = 1:3          a) V.S.F = 1:27          Volume of frustum  <math>= 160 \times 27 - 160</math>  <math>= 4160 \text{ cm}^3</math></p>	<p>B<sub>1</sub> M<sub>1</sub> A<sub>1</sub> 3</p>	<p>18. a) (i) Let distance covered by bus be <math>b</math> km.  <math>\therefore</math> time by train = <math>\frac{700-b}{50}</math>          time by bus = <math>\frac{b}{75}</math></p> <p><math>\therefore \frac{700-b}{50} + \frac{b}{75} = 11\frac{1}{2} - \frac{1}{2}</math>  <math>\frac{2100 - 3b + 2b}{150} = 11</math>  <math>2100 - b = 11 \times 150</math>  <math>b = 2100 - 1650</math>  <math>= 450</math></p> <p>(ii) time taken by train  <math>= \frac{700 - 450}{50} = 5 \text{ h.}</math></p> <p>total time before departure of bus  <math>= 5 \text{ h } 30 \text{ min}</math></p> <p><math>\therefore</math> departure time for bus  <math>= 8:00 + 5 \text{ h } 30 \text{ min}</math>  <math>= 1:30 \text{ pm}</math></p> <p>No mark for or 1330 hrs.          1330 or 13:30</p>	<p>M<sub>1</sub> M<sub>1</sub> M<sub>1</sub> A<sub>1</sub> M<sub>1</sub> M<sub>1</sub> A<sub>1</sub></p>
<p>b) <math>\frac{1}{3} \pi h (R^2 + Rr + r^2)</math>  <math>\sqrt[3]{160} = \frac{8}{24} = \frac{1}{3} B_1</math>  <math>\sqrt[3]{\text{Volume}} = \frac{8}{24}</math>  <math>V = 4320 - 160</math>  <math>= 4160</math>          ALT  <math>V = \frac{1}{3} \pi r^2 h</math>  <math>r^2 = \frac{3 \times 160}{\pi h}</math>  <math>r = 4.370</math>  <math>\frac{r}{8} = \frac{R}{24}</math>  <math>R = 13.11 B_1</math>  <math>V = \frac{1}{3} \times \frac{32^2}{7} \times 13.11</math>  <math>= 4320.177</math> if 3.142 is used  <math>V_f = 4320.177 - 160</math>  <math>= 4160.177</math></p>	<p>M<sub>1</sub> A<sub>1</sub></p>		

<p>19. a) <math display="block">\begin{pmatrix} 0 &amp; 1 \\ 2 &amp; p \end{pmatrix} \begin{pmatrix} -15 &amp; -0.5 \\ p &amp; p-2 \end{pmatrix}</math> <math display="block">= \begin{bmatrix} p &amp; p-2 \\ -3+p^2 &amp; p^2-2p \end{bmatrix}</math> <math display="block">p+p^3-2p^2 = p^3-2p^2-3p+6</math> <math display="block">-p = -3p+6</math> <math display="block">2p = 6</math> <math display="block">p = 3</math></p>	<p>M<sub>1</sub> A<sub>1</sub> M<sub>1</sub> A<sub>1</sub> B<sub>1</sub></p>	<p>b) (i) <math>h = 5.8 \sin 60</math>  <math>= 5.0 \text{ cm}</math>  (ii) area of <math>\Delta ABC</math>  <math>= \frac{1}{2} \times 8 \times 5.0</math>  <math>= 20 \text{ cm}^2</math>  (iii) size of <math>\angle ACB</math>  <math>\frac{\sin C}{5.8} = \frac{\sin 120}{12}</math> <math>\longrightarrow</math>  <math>\angle C = \sin^{-1} \frac{5.8 \times 0.866}{12}</math>  <math>\angle C = 24.7^\circ</math></p>	<p>M<sub>1</sub> A<sub>1</sub> M<sub>1</sub> A<sub>1</sub> M<sub>1</sub> A<sub>1</sub></p>
<p>b) (i) <math>x+30y = 50,000</math>  <math>x+40y = 56,000</math>  (ii) <math display="block">\begin{pmatrix} 1 &amp; 30 \\ 1 &amp; 40 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 50,000 \\ 56,000 \end{pmatrix}</math> <math display="block">\frac{1}{10} \begin{pmatrix} 40 &amp; -30 \\ -1 &amp; 1 \end{pmatrix} \begin{pmatrix} 1 &amp; 30 \\ 1 &amp; 40 \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \frac{1}{10} \begin{pmatrix} 46 &amp; -30 \\ 1 &amp; 1 \end{pmatrix} \begin{pmatrix} 50,000 \\ 56,000 \end{pmatrix}</math> <math display="block">\begin{pmatrix} x \\ y \end{pmatrix} = \frac{1}{10} \begin{pmatrix} 320,000 \\ 6,000 \end{pmatrix}</math> <math display="block">\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 32,000 \\ 600 \end{pmatrix}</math> <math>x = 32,000</math>  <math>y = 600</math>  (iii) <math>32,000 + 600 = 68,000</math>  <math display="block">\frac{68,000 - 32,000}{600} = 60</math></p>	<p>M<sub>1</sub> B<sub>1</sub> M<sub>1</sub> A<sub>1</sub> M<sub>1</sub> A<sub>1</sub> M<sub>1</sub> A<sub>1</sub> M<sub>1</sub> A<sub>1</sub> M<sub>1</sub> A<sub>1</sub></p>	<p>21. a) Ordinates  <math>x=0 \quad y_1=1</math>  <math>x=1 \quad y_2=6</math>  <math>x=2 \quad y_3=9</math>  <math>x=3 \quad y_4=10</math>  <math>x=4 \quad y_5=9</math>  <math>x=5 \quad y_6=6</math>  <math>x=6 \quad y_7=1</math>  Area <math>= \frac{1}{2} \times 1 \times \int_1^6 (1+2(6+9+10+9+6))</math>  <math>= \frac{1}{2} \{ 2+2(40) \}</math>  <math>= \frac{1}{2} (82) = 41</math>  b) (i) <math>\int_0^6 -x^2+6x+1 = \left[ -\frac{1}{3}x^3 + \frac{6x^2}{2} + x \right]_0^6</math>  <math>= 72+108+6</math>  <math>= 144-72=42</math></p>	<p>A<sub>1</sub> 10 B<sub>3</sub> M<sub>1</sub> A<sub>1</sub> M<sub>1</sub> A<sub>1</sub> M<sub>1</sub> A<sub>1</sub></p>
<p>20 a) <math>12^2 = x^2 + 8^2 - 2 \times 8 \times x \cos 120^\circ</math>  <math>x^2 + 8x - 80 = 0</math>  <math>x = \frac{-8 \pm \sqrt{64 - 4 \times 1 \times -80}}{2 \times 1}</math>  <math>= 5.8 \text{ or } -13.8</math>  <math>\therefore x = 5.8</math></p>	<p>M<sub>1</sub> M<sub>1</sub> M<sub>1</sub> A<sub>1</sub></p>	<p>(ii) <math>\frac{42-41}{42} \times 100\%</math>  <math>= 2.38\%</math></p>	<p>M<sub>1</sub> A<sub>1</sub> 10</p>



23

a) (i)

$$\begin{aligned} \tilde{BC} &= \tilde{bd} + \tilde{dc} \\ &= -\tilde{d} - \tilde{q} + 2\tilde{q} \\ &= \tilde{q} - \tilde{d} \end{aligned}$$

$$(ii) \tilde{Ax} = k\tilde{Ac} \Rightarrow \tilde{Ax} = k(2\tilde{q} - \tilde{d})$$

$$(iii) \tilde{bx} = h\tilde{dB} \Rightarrow \tilde{bx} = h(\tilde{d} + \tilde{q})$$

$$\begin{aligned} b) \tilde{Ax} &= -\tilde{d} + h\tilde{d} + h\tilde{q} \\ \Rightarrow \tilde{Ax} &= \tilde{d}(h-1) + h\tilde{q} \end{aligned} \quad \left. \begin{array}{l} \\ \\ \end{array} \right\} \rightarrow M_1$$

$$\text{Also } \tilde{Ax} = 2k\tilde{q} - k\tilde{d}$$

$$\therefore h = 2k \text{ and } h-1 = -k$$

$$h = -k + 1 \Rightarrow 2k = -k + 1$$

$$3k = 1$$

$$k = \frac{1}{3}$$

$$\begin{aligned} h = 2k &\Rightarrow h = 2 \times \frac{1}{3} \\ &= \frac{2}{3} \end{aligned}$$

c) (a)

b) (i) Meridian class : 200-300

(ii) meridian line : (258-260)

$$\alpha = \frac{220}{3.8} = 57.89$$

$$\begin{aligned} \text{hence } L &= 200 + 57.89 \\ &= 257.89 \end{aligned}$$

$$\begin{aligned} c) & 900 + 50 \times 0.5 \\ &= 925 \end{aligned}$$

B<sub>1</sub>B<sub>1</sub>B<sub>2</sub>B<sub>1</sub>B<sub>1</sub>B<sub>1</sub>B<sub>1</sub>M<sub>1</sub>M<sub>1</sub>A<sub>1</sub>

10

M<sub>1</sub>A<sub>1</sub>M<sub>1</sub>A<sub>1</sub>B<sub>1</sub>M<sub>1</sub>M<sub>1</sub>A<sub>1</sub>B<sub>1</sub>

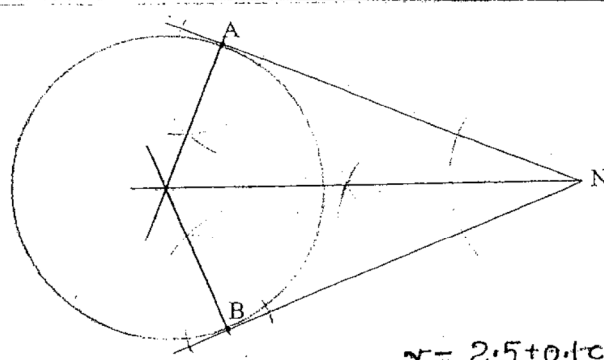
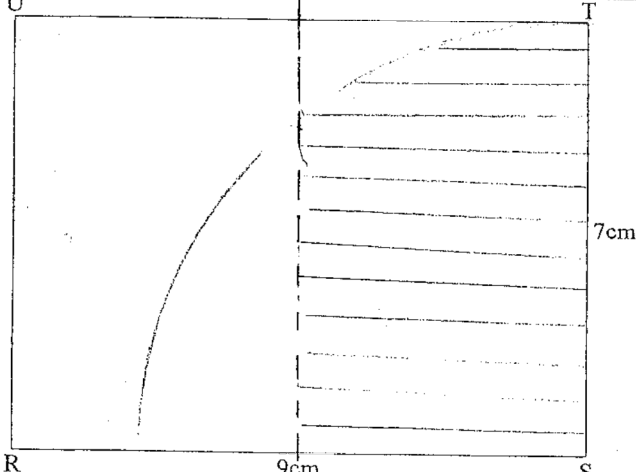
10

24



26 (a)	<table border="1"> <tr><td>+</td><td>7</td><td>8</td><td>9</td><td>10</td><td>11</td></tr> <tr><td>4</td><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td></tr> <tr><td>5</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td></tr> <tr><td>6</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td></tr> <tr><td>7</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td></tr> <tr><td>8</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td></tr> </table>	+	7	8	9	10	11	4	11	12	13	14	15	5	12	13	14	15	16	6	13	14	15	16	17	7	14	15	16	17	18	8	15	16	17	18	19	B1	✓ probability space (C.A.O)
+	7	8	9	10	11																																		
4	11	12	13	14	15																																		
5	12	13	14	15	16																																		
6	13	14	15	16	17																																		
7	14	15	16	17	18																																		
8	15	16	17	18	19																																		
b)	$P(\text{sum of ages at least 17}) = \frac{6}{25}$	B1																																					
		2																																					
17 (a)	$\vec{T} = \begin{pmatrix} 6 \\ -2 \end{pmatrix} - \begin{pmatrix} 4 \\ 1 \end{pmatrix} = \begin{pmatrix} 2 \\ -3 \end{pmatrix}$	B1																																					
b)	$\vec{OA}' = \begin{pmatrix} 1 \\ 2 \end{pmatrix} + \begin{pmatrix} -2 \\ -3 \end{pmatrix} = \begin{pmatrix} -1 \\ -1 \end{pmatrix}$ $A'(3, -1)$ $\vec{OB}' = \begin{pmatrix} 3 \\ 5 \end{pmatrix} + \begin{pmatrix} -2 \\ -3 \end{pmatrix} = \begin{pmatrix} 1 \\ 2 \end{pmatrix}$ $B'(5, 2)$	B1																																					
		B1																																					
		3																																					
3	$\sin 45^\circ = \frac{1}{\sqrt{2}}$ $\frac{\sqrt{8}}{1 + \sin 45^\circ} = \frac{\sqrt{8}(1 - \frac{1}{\sqrt{2}})}{(1 + \frac{1}{\sqrt{2}})(1 - \frac{1}{\sqrt{2}})}$ $= \frac{\sqrt{8} - \frac{\sqrt{8}}{\sqrt{2}}}{1 - \frac{1}{2}}$ $= 2\sqrt{8} - 4$	B1																																					
		M1	Rational denominator with the numerator expanded																																				
		A1	accept other forms $\frac{4\sqrt{2}-4}{2(\sqrt{2}-1)}$																																				
		3																																					
	$\text{Max}_A = 4\pi(7.5)^2 \quad \text{Min}_A = 4\pi(6.5)^2$	M1	$\frac{0.5}{7}$ ----- M1 --- R.E.																																				
	$\text{Absolute error} = \frac{4\pi(7.5^2 - 6.5^2)}{2}$	M1	$\frac{0.5}{7} \times 2$ ----- M1 Absolute Error																																				
	$\% \text{ Error} = \frac{28\pi}{4\pi \times 7^2} \times 100\%$ $= 14.29\%$	M1	allow for use of $\begin{cases} \text{Max} - \text{Min} \\ \text{Max} - \text{Actual} \\ \text{Actual} - \text{min} \end{cases}$																																				
		A1	14.29% A1																																				
		A																																					



<p>Q10 (a)</p>	 <p><math>r = 2.5 \pm 0.1 \text{ cm}</math></p>	<p>BI ✓ location of centre by construction - draw <math>\perp</math> at A or B or bisect angle ANB and draw <math>\perp</math> at A or B Circle drawn Use of trig &amp; Error <math>\pm 0.1</math></p>
<p>Q11</p>	$\left(a + \frac{1}{2}\right)^4 = a^4 + 4a^3\left(\frac{1}{2}\right) + 6a^2\left(\frac{1}{2}\right)^2 + 4a\left(\frac{1}{2}\right)^3 + \left(\frac{1}{2}\right)^4$ $= a^4 + 2a^3 + \frac{3a^2}{2} + \frac{1}{2}a + \frac{1}{16}$ $\left(a - \frac{1}{2}\right)^4 = a^4 + 4a^3\left(-\frac{1}{2}\right) + 6a^2\left(-\frac{1}{2}\right)^2 + 4a\left(-\frac{1}{2}\right)^3 + \left(-\frac{1}{2}\right)^4$ $= a^4 - 2a^3 + \frac{3a^2}{2} - \frac{1}{2}a + \frac{1}{16}$ $\left(a + \frac{1}{2}\right)^4 + \left(a - \frac{1}{2}\right)^4 = 2a^4 + 3a^2 + \frac{1}{8}$	<p>MI MI AI</p>
<p>Q12</p>		<p>BI <math>\perp</math> bisector of TU drawn Continuous or dotted.</p> <p>BI Arc radius 7 Centre S drawn Continuous or dotted.</p> <p>BI ✓ Region shaded with bisector dotted and arc full line</p>
<p>Q13</p>	$\vec{PQ} = -(6i + j) + (-2i + 5j)$ $= -8i + 4j$ $\vec{PN} = \frac{3}{4}(-8i + 4j)$ $= -6i + 3j$	<p>MI <math>\vec{ON} = \frac{3}{4}(-2i + 5j) + \frac{1}{4}(6i + j)</math> <math>= 4j</math></p> <p>MI <math>\vec{PN} = -(6i + j) + 4j</math></p> <p>AI</p>

Q14  
(a)

Let longitude difference be  $\theta$

$$\theta \times 60 \cos 60^\circ = 630$$

$$\theta = \frac{630}{60 \cos 60^\circ} = 21^\circ$$

(b)  $21^\circ$  East of longitude  $18^\circ E$  is  $39^\circ E$   
N( $60^\circ N$ ,  $39^\circ E$ )

M1

Case where list is in  
kms follow through

A1

B1  
3

Q15

$$x^2 - 6x + 9 + y^2 - 10y + 25 = -30 + 9 + 25$$

$$\pm 2a = \pm 6 \quad \text{or} \quad (x-3)^2 = (x-a)^2$$

$$\pm 2b = \pm 10 \quad \text{or} \quad (y-5)^2 = (y-b)^2$$

$$a = 3 \quad \text{and} \quad b = 5$$

B1

allow for  $(x-3)^2$  seen

B1

allow for  $(y-5)^2$  seen

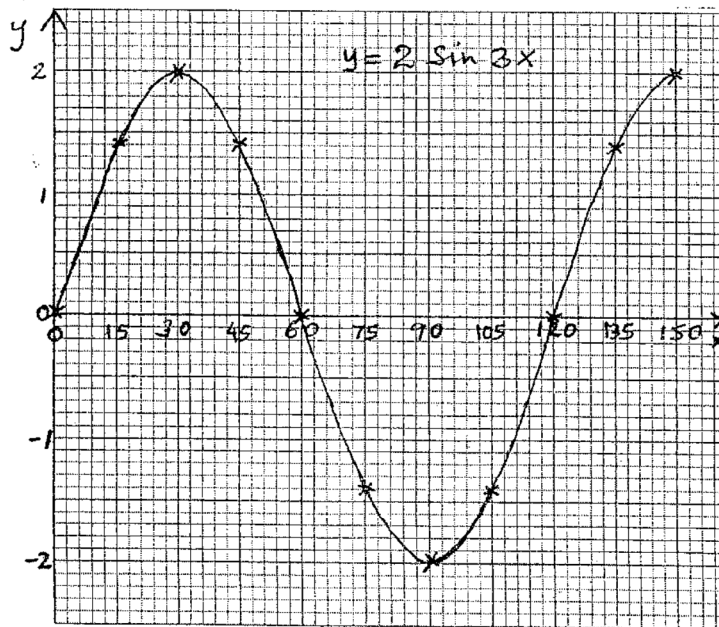
B1

allow if  $(3, 5)$

3

Q16

(a)



(b)

$$\text{Period} = 120^\circ$$

P1

✓ plotting

C1

Smooth Sine Curve

B1

if curve drawn  
 $\frac{360}{3} = 120^\circ$  allow

3

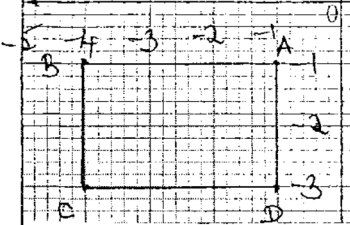
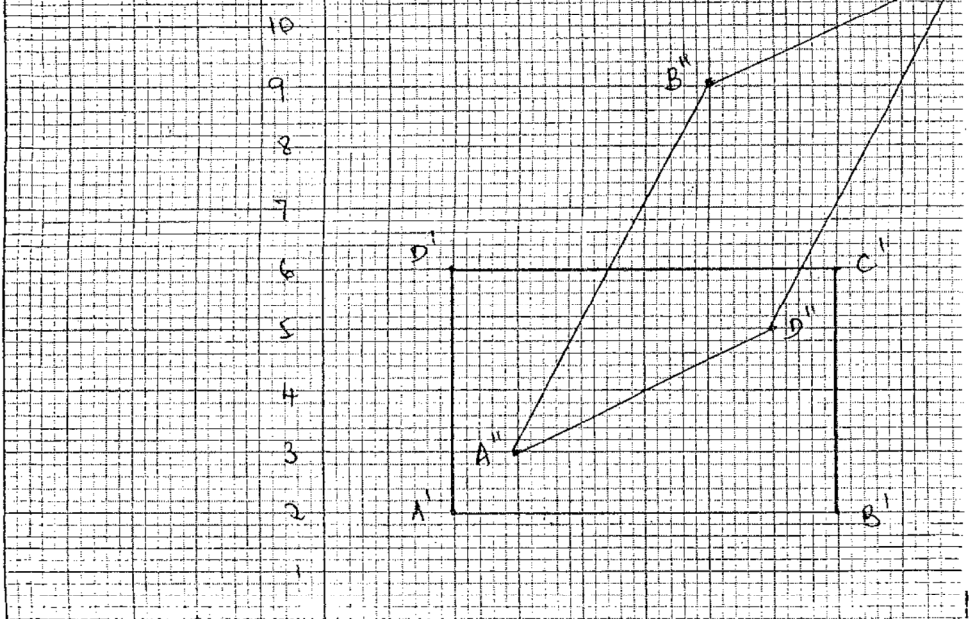
<p>17a) (i) The cost = Ksh (7500 + 11 x 6000) = Ksh 73500</p>	<p>MI AI</p>	
<p>(ii) The % increase = <math>\frac{73500 - 60000}{60000} \times 100</math> = 22.5%</p>	<p>MI AI</p>	
<p>(b) The amount paid = Ksh 60000 x 25 x 0.95 = Ksh 1425000</p>	<p>MI AI</p>	
<p>(c) Institution X; Ksh 73500 x 25 = Ksh 1837500</p>	<p>MI</p>	
<p>Institution Y; Ksh 60000 x 25 x <math>(1 + \frac{12}{100})^2</math> = Ksh 1881600</p>	<p>MI</p>	
<p>Difference = Ksh (1881600 - 1837500) = Ksh 44100</p>	<p>MI AI</p>	
	<p>10</p>	
<p>18a) (i) <math>r = \frac{64 + 4d}{64}</math>, <math>r = \frac{64 + 6d}{64 + 4d}</math></p>	<p>B1B1</p>	<p>or equivalent <math>64 + 4d = 64r</math> <math>64 + 6d = 64r^2</math></p>
<p>(ii) <math>\frac{64 + 4d}{64} = \frac{64 + 6d}{64 + 4d}</math></p>	<p>MI</p>	<p>or equivalent <math>64r^2 = 64 + 6(16r - 16)</math></p>
<p><math>16d^2 + 128d = 0</math></p>	<p>MI</p>	<p><math>2r^2 - 3r + 1 = 0</math></p>
<p><math>16d(d + 8) = 0</math></p>	<p>MI</p>	<p><math>(2r - 1)(r - 1) = 0</math></p>
<p><math>d = -8</math></p>	<p>AI</p>	<p><math>\therefore r = \frac{1}{2}</math> or <math>r = 1</math></p>
<p><math>\therefore r = \frac{64 + 4(-8)}{64}</math></p>		<p><math>\therefore r = \frac{1}{2}</math></p>
<p><math>= \frac{1}{2}</math></p>	<p>B1</p>	<p><math>- + d = \frac{32 - 64}{1} = -32</math></p>
<p>(b) (i) <math>S_{10} = \frac{10}{2} (2 \times 64 + 9 \times -8)</math> = 280</p>	<p>MI AI</p>	
<p>(ii) <math>S_{10} = \frac{64(1 - (\frac{1}{2})^{10})}{1 - \frac{1}{2}}</math> = 127.875</p>	<p>MI</p>	<p>- May substitute either value for r</p>
<p></p>	<p>AI</p>	<p>Accept 127 <math>\frac{7}{8}</math> and when rounded off to at least 4 s.f.</p>
	<p>10</p>	

19 (b) Rectangle ABCD drawn  
 $\begin{pmatrix} -2 & 0 \\ 0 & -2 \end{pmatrix} \begin{pmatrix} -1 & -4 & -4 & -1 \\ -1 & -1 & -3 & -3 \end{pmatrix}$   
 $= A' B' C' D'$   
 $= \begin{pmatrix} 2 & 2 & 2 & 2 \\ 2 & 2 & 6 & 6 \end{pmatrix}$

BI  
MI  
AI

At least 2 points must be ✓  
May be implied in the diagram

Rectangle A'' B'' C'' D'' drawn



$$\text{biv} \begin{pmatrix} \frac{1}{2} & \frac{1}{2} \\ 1 & 1 \end{pmatrix} \begin{pmatrix} 2 & 2 & 2 & 2 \\ 2 & 2 & 6 & 6 \end{pmatrix} = \begin{pmatrix} 3 & 6 & 10 & 7 \\ 3 & 9 & 11 & 5 \end{pmatrix}$$

$A''(3,3), B''(6,9), C''(10,11), D''(7,5)$

(c) Det of  $P = -3/4$

Area  $A''B''C''D'' = 3/4 \times 6 \times 4 = 18 \text{ sq unit.}$

MI ✓ attempt to multiply  
AI ✓ if A above is used  
BI ✓ attempt to solve  
BI ✓ or equivalent  
AI  
AI  
10

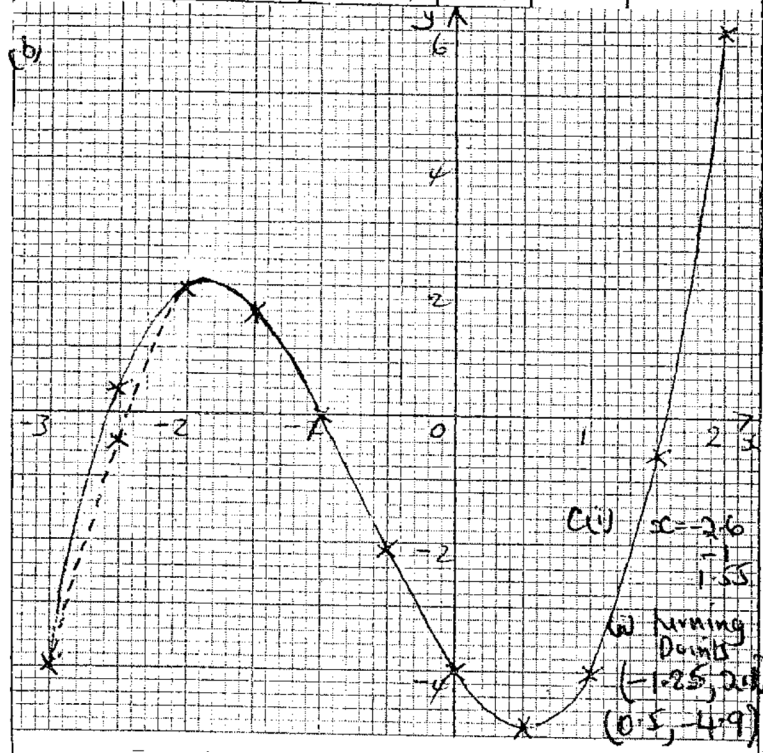
- 2009 (i)  $x-5$
- (ii)  $[x+(x-5)] \times 2 = 4x-10$
- (b) (i)  $(x+20), (x+15), (4x+10)$   
 $(x+20)(x+15) = 15(4x+10)$   
 $x^2 - 25x + 150 = 0$   
 $(x-10)(x-15) = 0$   
 $x = 10 \text{ or } x = 15$
- (ii)  $4 \times 10 - 10$  or  $4 \times 15 - 10 = 30$  or  $50$
- (iii)  $(10-5) + 20$  or  $(15-5) + 20 = 25$  or  $30$

BI  
BI  
BI  
MI  
AI  
MI  
AI  
MI  
AI  
10

implied  
allow when two ages are ✓  
for ✓ attempt to solve or equivalent  
for both ages  
for both ages.

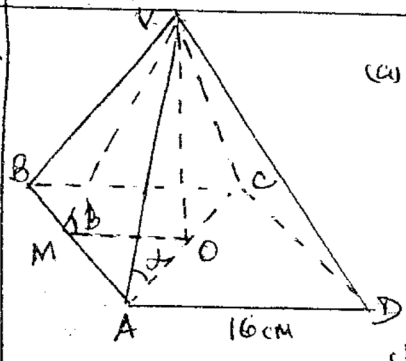
21 a)

x	-2	-0.5	1	1.5
y	2	-2.1	-4	-0.6



B2 BI for 3 ✓  
 S1 for ✓ scale  
 P1M for ✓ plotting  
 C1 for ✓ smooth curve  
 BI accept -2.45 for use of -0.4  
 BI  
 BI  
 BI Allow readings within 1 small square.  
 BI  
 BI  
 10

22.



(a)  $Ac^2 = 16^2 + 12^2 = 400$   
 $Ac = \sqrt{400} = 20 \text{ cm}$   
 $AO = 10 \text{ cm}$   
 $VO^2 = 26^2 - 10^2$   
 $VO = \sqrt{576} = 24 \text{ cm}$

(b) The angle between VA and ABCD is  $\alpha$   
 $\tan \alpha = \frac{24}{10}$   
 $\alpha = 67.38^\circ$   
 (9)

(c) The angle between the planes is  $\beta$   
 $\tan \beta = \frac{24}{8}$   
 $\beta = 71.57^\circ$   
 (5)

M1 w equivalent  
 M1  
 M1  
 A1  
 BI - implied  
 M1 or equivalent  
 A1  
 BI - implied  
 M1 w equivalent  
 A1 accept 71.6  
 10

23 a)  $c = an + \frac{b}{n}$   
 $135 = 2a + \frac{b}{2}$   
 $140 = 3a + \frac{b}{3}$   
 $270 = 4a + b$  (i)  
 $420 = 9a + b$  (ii)  
 $150 = 5a, a = 30$   
 Sub  $a = 30$  in (i),  
 $270 = 120 + b, b = 150$   
 $\therefore c = 30n + \frac{150}{n}$   
 b)  $c = 30 \times 10 + \frac{150}{10}$   
 $= \text{Rs } 315$   
 c)  $756 = 30n + \frac{150}{n}$   
 $5n^2 - 126n + 25 = 0$   
 $(5n - 1)(n - 25) = 0$   
 $n = \frac{1}{5}$  or  $n = 25$   
 $\therefore$  the number of items = 25

B1

M1

M1

A1

B1

M1

A1

M1

M1

A1

10

✓ attempt to solve the equations

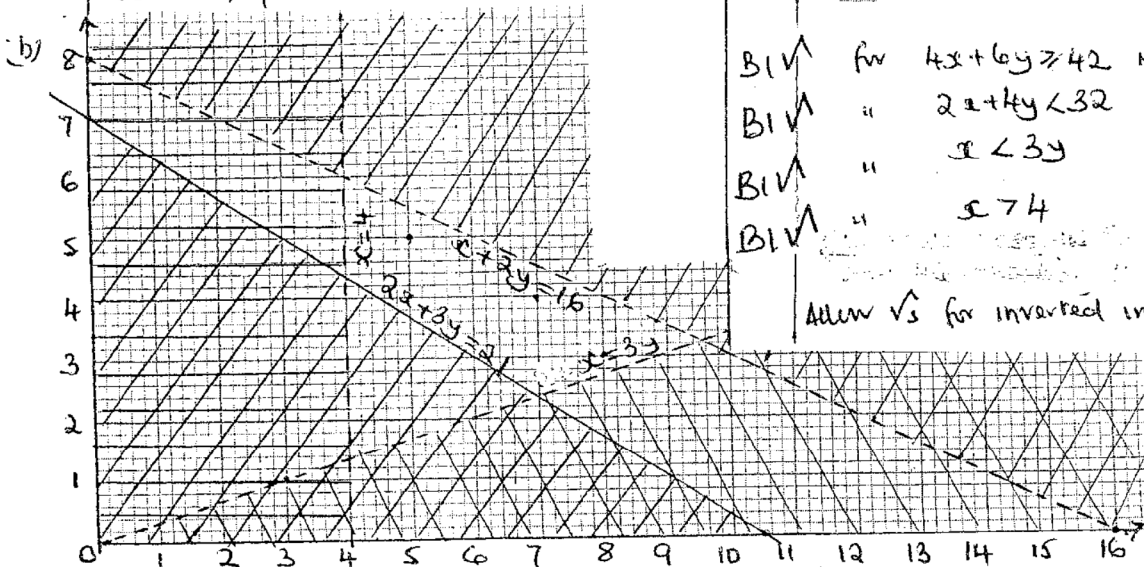
for both values  $a$  and  $b$ .

✓ if A above is lost

✓ attempt to solve the equation

✓ if A above is lost

24 a) (i)  $4x + 6y \geq 42$   
 (ii)  $2x + 4y \leq 32$   
 (iii)  $x \leq 3y$   
 (iv)  $x \geq 4$



B1

B1

B1

B1

B1

B1

B1

B1

B1

B1

B1

M1

A1

10

for  $4x + 6y \geq 42$  represented by

"  $2x + 4y \leq 32$  "

"  $x \leq 3y$  "

"  $x \geq 4$  "

Allow ✓s for inverted inequalities

e) when  $x=5, y=5, 5 \times 4 + 5 \times 6 = 50$  hrs  
 "  $x=8, y=3, 2 \times 4 + 3 \times 6 = 50$  hrs  
 "  $x=7, y=4, 7 \times 4 + 4 \times 6 = 52$  hrs  
 7 trips by P and 4 by Q

for at least two pts used (May be implied)